Name _____ Mr. Schlansky Date _____ Algebra 2

CCA2 Common Regents Homework

1. What is the completely factored form of $k^4 - 4k^2 + 8k^3 - 32k + 12k^2 - 48$?

- 1) (k-2)(k-2)(k+3)(k+4)
- 2) (k-2)(k-2)(k+6)(k+2)
- 3) (k+2)(k-2)(k+3)(k+4)
- 4) (k+2)(k-2)(k+6)(k+2)

2. What is the solution set of the equation $\frac{3x+25}{x+7} - 5 = \frac{3}{x}$?

- 1) $\left\{\frac{3}{2}, 7\right\}$ 2) $\left\{\frac{7}{2}, -3\right\}$ 3) $\left\{-\frac{3}{2}, 7\right\}$ 4) $\left\{-\frac{7}{2}, -3\right\}$
- 3. Solve graphically for x: $\sqrt{x^2 + x 1} + 11x = 7x + 3$
- 4. Which factorizations are correct?



- $I. a^{3} + 27b^{3} = (a+3b)(a^{2} 3ab + 9b^{2})$ $II. c^{3} - 6c^{2} + 8c + 5c^{2} - 30c + 40 = (c-2)(c-4)(c+5)$ $III. 1 - x^{4} = (1+x)^{2}(1-x)^{2}$
- 1) I, only
- 2) I and II only
- 3) II and III only
- 4) I, II, and III



5. Stone Manufacturing has developed a cost model, $C(x) = 0.18x^3 + 0.02x^2 + 4x + 180$, where x is the number of sprockets sold, in thousands. The sales price can be modeled by S(x) = 95.4 - 6x and the company's revenue by $R(x) = x \cdot S(x)$. The company's profits, R(x) - C(x), could be modeled by

1) $0.18x^3 + 6.02x^2 + 91.4x + 180$ 3) $-0.18x^3 - 6.02x^2 + 91.4x - 180$ 2) $0.18x^3 - 5.98x^2 - 91.4x + 180$ 4) $0.18x^3 + 5.98x^2 + 99.4x + 180$





6. Given $f(x) = 3x^2 + 7x - 20$ and g(x) = x - 2, state the quotient and remainder of $\frac{f(x)}{g(x)}$, in the form $q(x) + \frac{r(x)}{g(x)}$.







8. If x - 1 is a factor of $x^3 - kx^2 + 2x$, what is the value of k?





10. A sketch of r(x) is shown below.

An equation for r(x) could be

1) r(x) = (x-a)(x+b)(x+c)2) $r(x) = (x+a)(x-b)(x-c)^2$ 3) r(x) = (x+a)(x-b)(x-c)4) $r(x) = (x-a)(x+b)(x+c)^2$

11. On the grid below, sketch a cubic polynomial whose factors are x-1, x-3, and x+2

r(x)

a

-c

> X





12. Which graph has the following characteristics?







13. If x is a real number, express $2xi(i - 4i^2)$ in simplest a + bi form.



14. Which equation represents the equation of the parabola with focus (-3, 3) and directrix y = 7?

y = 7? 1) $y = \frac{1}{8}(x+3)^2 - 5$ 2) $y = \frac{1}{8}(x-3)^2 + 5$ 3) $y = -\frac{1}{8}(x+3)^2 + 5$ 4) $y = -\frac{1}{8}(x-3)^2 + 5$



15. The parabola described by the equation $y = \frac{1}{12}(x-2)^2 + 2$ has the directrix at y = -1.



The focus of the parabola is 1) (2,-1)

2) (2,2)

3) (2,3)
4) (2,5)



	16.	If $f(x) = 3 x - 1$ and $g(x) = 0.03x^3 - 1$	x + 1, an	approximate solution for the equation
ø	f(x)	= g(x) is		
Ē	1)	1.96	3)	(-0.99, 1.96)
	2)	11.29	4)	(11.29, 32.87)





18. At which x value is the graph of $f(x) = 2x^3 - 11x^2 - 14x + 26$ increasing? 1) -.5 3) 1.7 2) 3.9 4) 4.3



19. Graph $p(x) = x^3 + x^2 - 4x - 4$ on the grid provided and fill in the end behavior $x \to -\infty, f(x) \to x \to \infty, f(x) \to x$



20. What is the inverse of
$$f(x) = -6(x-2)$$
?
¹⁾ $f^{-1}(x) = -2 - \frac{x}{6}$
²⁾ $f^{-1}(x) = 2 - \frac{x}{6}$
³⁾ $f^{-l}(x) = \frac{1}{-6(x-2)}$
⁴⁾ $f^{-1}(x) = 6(x+2)$



21. Determine graphically whether the following functions are even, odd, or neither





22. Given the parent function $p(x) = \cos x$, which phrase best describes the transformation used to obtain the graph of $g(x) = \cos(x + a) - b$, if *a* and *b* are positive constants?

- 1) right *a* units, up *b* units
- 2) right *a* units, down *b* units
- 3) left *a* units, up *b* units
- 4) left *a* units, down *b* units



23. The graph below represents the parabolic path of a ball kicked by a young child. Find the average rate of change from 3 to 6 seconds. Explain its meaning in the context of the problem.





3)

24. Which value is *not* contained in the solution of the system shown below?

1)
$$-2$$

2) 2 $a + 5b - c = -20$

$$\begin{array}{cccc}
 & -3 & -3 & -a & -5b & +4c & = & 19 \\
 & -3 & -a & -5b & -5c & = & 2 \\
\end{array}$$

25. Express in simplest form with a rational exponent: $\frac{x\sqrt{x^3}}{\sqrt[3]{x^5}}$





27. Graph $y = 3^{x-2} - 4$ on the axes provided and fill in the end behavior.

 $x \rightarrow -\infty, f(x) \rightarrow$

$$x \to \infty, f(x) \to \infty$$





• 28. Graph $y = -\log_3(x-4) + 1$ and fill in the end behavior

$$x \to 4, f(x) \to x \to \infty, f(x) \to x \to \infty$$



- 29. Which statement about the graph of $c(x) = \log_6 x$ is *false*?
- 1) The asymptote has equation y = 0.
- 2) The graph has no *y*-intercept.
- 3) The domain is the set of positive reals.
- 4) The range is the set of all real numbers.



30. If a function is defined by the equation $f(x) = 4^x$, which graph represents the inverse of this function?







33. Using a microscope, a researcher observed and recorded the number of bacteria spores on a large sample of uniformly sized pieces of meat kept at room temperature. A summary of the data she recorded is shown in the table below.



Hours (x)	Average Number of Spores (y)
0	4
0.5	10
1	15
2	60
3	260
4	1130
6	16,380

Using these data, write an exponential regression equation, rounding all values to the *nearest thousandth*. The researcher knows that people are likely to suffer from foodborne illness if the number of spores exceeds 100. Using the exponential regression equation, determine the maximum amount of time, to the *nearest hundredth*, that the meat can be kept at room temperature safely.



34. The Fahrenheit temperature, F(t), of a heated object at time *t*, in minutes, can be modeled by the function below. F_s is the surrounding temperature, F_0 is the initial temperature of the object, and *k* is a constant.

$$F(t) = F_s + (F_0 - F_s)e^{-kt}$$

Coffee at a temperature of 195°F is poured into a container. The room temperature is kept at a constant 68°F and k = 0.05. Coffee is safe to drink when its temperature is, at most, 120°F. To the *nearest minute*, how long will it take until the coffee is safe to drink?



35. The population of Schlansky, Arizona increases by 14% every 5.1 years. If the population is currently 2150, write an equation for p(t), the population after *t* years. Using your equation, what will be the population, to the *nearest person*, 11 years from now?

36. A bank account is opened with \$2200 and interest is compounded continuously at a rate of 2.76% per year. Write an equation for b(t), the balance of the account after *t* years. Using your equation, what will be the balance of the account after 7 years?

37. A certain car depreciates at a rate of 12% each year. If the car was initially worth \$22,100, write an equation for v(t), the value of the account after t years. Using your equation, to the *nearest tenth of a year*, how long will it take for the value of the car to reach \$2,500?

38. The half life of an element is 71 minutes. If there were initially 6.4 kg of the substance, write an equation for a(t), the amount of the substance remaining after t minutes. Using your equation, to the *nearest hundredth of a kg*, how much will remain after 102 minutes?



39. A bank account is opened with \$2000 and interest is compounded quarterly at an interest rate of 3.5%. Write an equation for b(t), the balance of the account after *t* years. Using your equation, to the *nearest year*, how long will it take for the balance of the account to double?



• 40. Jack bought a new car in 2010 for \$16100. In 2018, the car is now worth \$6125. What is the annual rate of decrease to the *nearest percent*?



- 41. An equation to represent the value of a car after t months of ownership is
- $v = 32,000(0.81)^{\frac{1}{12}}$. Which statement is *not* correct?
- 1) The car lost approximately 19% of its value each month.
- 2) The car maintained approximately 98% of its value each month.
- 3) The value of the car when it was purchased was \$32,000.
- 4) The value of the car 1 year after it was purchased was \$25,920.

42. A study of the annual population of the red-winged blackbird in Ft. Mill, South Carolina, shows the population, B(t), can be represented by the function $B(t) = 750(1.16)^{t}$, where the *t* represents the number of years since the study began. In terms of the monthly rate of growth, the population of red-winged blackbirds can be best approximated by the function

1) $B(t) = 750(1.012)^{t}$

3) $B(t) = 750(1.012)^{12t}$ 2) $B(t) = 750(1.16)^{12t}$ 4) $B(t) = 750(1.16)^{\frac{t}{12}}$



43. The value of a home after t years can be modeled by the function $A = 525000(1.36)^{t}$ after t years. Which function would represent the monthly rate of increase after m months?

1) $A = 525000(1.36)^m$ 3) $A = 525000(1.026)^m$ 4) $A = 525000(1.026)^{12m}$ 2) $A = 525000(1.36)^{12m}$

44. The values below represent the cost of an ice cream sundae with one through four toppings. Write an explicit and recursive formula for a sequence that can be used to determine the cost of an ice cream cone with *n* toppings.

> \$4.75 \$5.50 \$6.25 \$7.00



45. The population of Jamesburg for the years 2010-2013, respectively, was reported as follows:

250,000 250,937 251,878 252,822 How can this sequence be recursively modeled? 1) $j_n = 250,000(1.00375)^{n-1}$ 2) $j_n = 250,000 + 937^{(n-1)}$ 3) $j_1 = 250,000$ 4) $j_1 = 250,000$ $j_n = 1.00375 j_{n-1}$ $j_n = j_{n-1} + 937$







- 47. The sequence defined by $r_1 = 15$ and $r_n = 0.75r_{n-1}$ best models which scenario?
 - 1) Gerry's \$15 allowance is increased by \$0.75 each week.
 - 2) A store that has not sold a \$15 item reduces the price by \$0.25 each week until someone purchases it.
 - 3) A 15-gram sample of a chemical compound decays at a rate of 75% per hour.
 - 4) A picture with an area of 15 square inches is reduced by 25% over and over again to make a proportionally smaller picture.

48. Alexa earns \$33,000 in her first year of teaching and earns a 4% increase in each successive year. Find Alexa's total earnings for her first 15 years of teaching, to the *nearest cent*.



49. Kristin wants to increase her running endurance. According to experts, a gradual mileage increase of 10% per week can reduce the risk of injury. If Kristin runs 8 miles in week one, which expression can help her find the total number of miles she will have run over the course of her 6-week training program?

1)
$$\sum_{n=1}^{6} 8(1.10)^{n-1}$$

2) $\sum_{n=1}^{6} 8(1.10)^{n}$
3) $\frac{8-8(1.10)^{6}}{0.90}$
4) $\frac{8-8(0.10)^{n}}{1.10}$



50. Using the formula below, determine the monthly payment on a 5-year car loan with a monthly percentage rate of 0.625% for a car with an original cost of \$21,000 and a \$1000 down payment, to the *nearest cent*.

$$P_n = PMT\left(\frac{1 - (1 + i)^{-n}}{i}\right)$$

 P_n = present amount borrowed n = number of monthly pay periods PMT = monthly payment i = interest rate per month





b 53. Angle θ is in standard position and (-2,3) is a point on the terminal side of θ . Find: **a**) cos θ **b**) sin θ **c**) tan θ

d) sec \mathcal{G}

f) $\cot \theta$







55. Graph $y = -2\cos\frac{\pi}{5}x + 1$ over the interval [0,20]



56. The depth of the water at a marker 20 feet from the shore in a bay is depicted in the graph below.

If the depth, d, is measured in feet and time, t, is measured in hours since midnight, what is an equation for the depth of the water at the marker?

1)
$$d = 5\cos\left(\frac{\pi}{6}t\right) + 9$$

2)
$$d = 9\cos\left(\frac{\pi}{6}t\right) + 5$$

3)
$$d = 9\sin\left(\frac{\pi}{6}t\right) + 5$$



$$d = 5\sin\left(\frac{\pi}{6}t\right) + 9$$



57. Griffin is riding his bike down the street in Churchville, N.Y. at a constant speed, when a nail gets caught in one of his tires. The height of the nail above the ground, in inches, can be represented by the trigonometric function $f(t) = -13\cos(0.8\pi t) + 13$, where t represents the time (in seconds) since the nail first became caught in the tire. Determine the period of f(t). Interpret what the period represents in this context. On the grid below, graph *at least one* cycle of f(t) that includes the y-intercept of the function.



58. Which statement is *incorrect* for the graph of the function $y = -3\cos\left|\frac{\pi}{3}(x-4)\right| + 7?$

- 1) The period is 6.
- 2) The amplitude is 3.
- 3) The range is [4,10].
- 4) The midline is y = -4.



59. As θ increases from π to $\frac{3\pi}{2}$ radians, the graph of $y = \sin \theta$ will 1) Decrease from 1 to 0 3) Increase from -1 to 0 2) Decrease from 0 to -1 4) Increase from 0 to 1



60. The probability of event A is .27. The probability of event B is .36. The probability of both events happening is .11. What is the probability that event A or event B happens?

61. The probability of event A happening is 14% and the probability of event B happening is 18%, The probability that event A or event B happens is 20%. What is the probability that event A and event B happens?



62. On a given school day, the probability that Nick oversleeps is 48% and the probability he has a pop quiz is 25%. Assuming these two events are independent, what is the probability that Nick oversleeps and has a pop quiz on the same day?



63. A public opinion poll was taken to explore the relationship between age and support for a candidate in an election. The results of the poll are summarized in the table below.

Age	For	Against	No Opinion
21-40	30	12	8
41-60	20	40	15
Over 60	25	35	15

What is the probability that someone is 41-60 given that they have no opinion?

What is the probability that someone is over 60 and against the candidate?

What is the probability that someone is for the candidate?

What percent of the 21-40 age group was for the candidate?

64. The results of a poll of 200 students are shown in the table below: For this group of students, do these data suggest that "female" and "techno" are independent of each other? Justify your answer.

	Preferred Music Style		
	Techno	Rap	Country
Female	54	25	27
Male	36	40	18



65. A fast-food restaurant analyzes data to better serve its customers. After its analysis, it discovers that the events D, that a customer uses the drive-thru, and F, that a customer orders French fries, are independent. The following data are given in a report:

 $P(R^{\uparrow} = 0.8)$

		2 (2) = 0.0
Given this information, $P(F D)$ is		D(m - D) = 0.464
1) 0.344	3) 0.57	$P(P \cap D) = 0.450$
2) 0.3648	4) 0.8	



66. The heights of women in the United States are normally distributed with a mean of 64 inches and a standard deviation of 2.75 inches. Out of 250 women, to the *nearest woman*, how many would be expected to be taller than 69 inches?



67. A doctor wants to test the effectiveness of a new drug on her patients. She separates her sample of patients into two groups and administers the drug to only one of these groups. She then compares the results. Which type of study best describes this situation? 1) census

2) survey

- 3) observation
- 4) controlled experiment



- 68. A survey is being conducted about American's favorite musicians. Which of the following survey methods would most likely produce a random sample? Asking every 20th person at a Green Day concert
 Asking every 10th person at a vintage record store

 - 3) Asking every 10th person at the Westbury Public Library
 - 4) Sending out surveys to random households across the country.



69. A radio station claims to its advertisers that the mean number of minutes commuters listen to the station is 30. The station conducted a survey of 500 of their listeners who commute. The sample statistics are shown below.

x	29.11
s x	20.718

A simulation was run 1000 times based upon the results of the survey. The results of the simulation appear below.



Based on the simulation results, is the claim that commuters listen to the station on average 30 minutes plausible? Explain your response including an interval containing the middle 95% of the data, rounded to the nearest hundredth.

70. Fifty-five students attending the prom were randomly selected to participate in a survey about the music choice at the prom. Sixty percent responded that a DJ would be preferred over a band. Members of the prom committee thought that the vote would have 50% for the DJ and 50% for the band. A simulation was run 200 times, each of sample size 55, based on the premise that 60% of the students would prefer a DJ. The approximate normal simulation results are shown below.

Using the results of the simulation, determine the margin of error rounded to the *nearest hundredth*.





71. A game spinner is divided into 6 equally sized regions, as shown in the diagram below. For Miles to win, the spinner must land on the number 6. After spinning the spinner 10 times, and losing all 10 times, Miles complained that the spinner is unfair. At home, his dad ran 100 simulations of spinning the spinner 10 times, assuming the probability of winning each spin is $\frac{1}{6}$. The output of the simulation is shown in the

diagram below.



Is there strong evidence to suggest that the spinner is unfair? Explain your answer.

72. Joseph was curious to determine if scent improves memory. A test was created where better memory is indicated by higher test scores. A controlled experiment was performed where one group was given the test on scented paper and the other group was given the test on unscented paper. The summary statistics from the experiment are given below.



	Scented Paper	Unscented Paper
\bar{x}	23	18
Sx	2.898	2.408

Calculate the difference in means in the experimental test grades (scented -unscented). A simulation was conducted in which the subjects' scores were rerandomized into two groups 1000 times. The differences of the group means were calculated each time. The results are shown below.



Use the simulation results to determine the interval representing the middle 95% of the difference in means, to the *nearest hundredth*. Is the difference in means in Joseph's experiment statistically significant based on the simulation? Explain.



73. Factor the following

a)
$$36-25x^2$$
 b) $x^2-7x+12$ c) $3x^2+9x-12$





g)
$$3x^3 + x^2 - 12x^2 - 4x - 63x - 21$$
 h) $(x^2 - 2x)^2 - 11(x^2 - 2x) + 24$

i) $y^3 - 125$



74. Express the following in simplest form: $\frac{10-5x}{x^2+2x-8}$



75. Solve $x^2 + 5x = 2x + 40$ algebraically

76. What are the solutions to $4x^2 - 7x - 2 = -10$ 1) $-\frac{1}{4}, 2$ 2) $\frac{7}{8} \pm \frac{\sqrt{79}}{8}i$ 3) $\frac{7}{8} \pm \frac{\sqrt{241}}{8}i$ 4) $\frac{7}{8} \pm \frac{\sqrt{143}}{8}i$



77. Solve the equation $x^2 + 2x = -8$ algebraically and express the answer in simplest a + bi form.



78. Solve $x^3 + 5x^2 = 4x + 20$ algebraically.



79. Solve the following equation algebraically: $\sqrt{2x-7} + x = 5$

$$\frac{3}{x} + \frac{x}{x+2} = -\frac{2}{x+2}$$

80. Solve algebraically for x:



81. To solve the equation $\frac{7}{x+7} + \frac{4x}{x-7} = \frac{3x+7}{x-7}$, Joan's first step is to multiply both sides by the least common denominator. Which statement is true?

- -14 is an extraneous solution.
 7 and -7 are extraneous solutions.
 7 there are no extraneous solutions.



82. Solve the following system of equations algebraically for x and y $(x+2)^2 + (y-4)^2 = 40$ y = x+2



83. Solve the following system of equations algebraically for all values of x, y, and z: x+2y-3z=-2





84. The value of Tom's bank account is currently 100000 and is decreasing according to the equation $V(t) = 100000(.876)^t$. The amount of money he has paid for his mortgage can be represented by the equation $M(t) = 20000(1.1304)^t$. Graph and label V(t) and M(t) over the interval [0,10].



After how many years will the value of Tom's bank account be equal to the amount of money he paid for his mortgage? Round your answer to the *nearest tenth of a year*. Tom will open a new bank account when the value of his account is \$30,000. After how many years, to the *nearest hundredth of a year*, will that happen?

85. A Foucault pendulum can be used to demonstrate that the Earth rotates. The time, t, in seconds, that it takes for one swing or period of the pendulum can be modeled by the

equation $t = 2\pi \sqrt{\frac{L}{g}}$ where L is the length of the pendulum in meters and g is a constant of

9.81 m/s². The first Foucault pendulum was constructed in 1851 and has a pendulum length of 67 m. Determine, to the *nearest tenth of a second*, the time it takes this pendulum to complete one swing. Another Foucault pendulum at the United Nations building takes 9.6 seconds to complete one swing. Determine, to the *nearest tenth of a meter*, the length of this pendulum.