Name Schlansky
Mr. Schlansky

Date ____________
Algebra 2

CCA2 Common Regents Homework

1. What is the completely factored form of $k^4 - 4k^2 + 8k^3 - 32k + 12k^2 - 48$? 18432 MC Strategy
1) $(k-2)(k-2)(k+3)(k+4)$ 11648
2) $(k-2)(k-2)(k+6)(k+2)$ 12288
3) $(k+2)(k-2)(k+3)(k+4)$ 17472
4) $(k+2)(k-2)(k+6)(k+2)$ 18432

2. What is the solution set of the equation $\frac{3x+25}{x+7} - 5 = \frac{3}{x}$? MC Strategy
1) $\left\{\frac{3}{2}, 7\right\}$
2) $\left\{\frac{7}{2}, -3\right\}$
3) $\left\{-\frac{3}{2}, 7\right\}$
4) $\left\{-\frac{7}{2}, -3\right\}$ $-\frac{7}{2}$ STO→X
-3 STO→X

3. Solve *graphically* for *x*: $\sqrt{x^2+x-1} + 11x = 7x + 3$ Intersect
41 42
$x = .\overline{6}$

4. Which factorizations are correct?
I. $a^3 + 27b^3 = (a+3b)(a^2 - 3ab + 9b^2)$ 91082.125 = 91082.125
II. $c^3 - 6c^2 + 8c + 5c^2 - 30c + 40 = (c-2)(c-4)(c+5)$ 61.875 = 61.875
III. $1 - x^4 = (1+x)^2(1-x)^2$ −149... = 1.26.. X
1) I, only
2) I and II only
3) II and III only
4) I, II, and III

$95.4x - 6x^2 - 0.18x^3 - 0.02x^2 - 4x - 180$
$-0.18x^3 - 6.02x^2 + 91.4x - 180$

5. Stone Manufacturing has developed a cost model, $C(x) = 0.18x^3 + 0.02x^2 + 4x + 180$, where *x* is the number of sprockets sold, in thousands. The sales price can be modeled by $S(x) = 95.4 - 6x$ and the company's revenue by $R(x) = x \bullet S(x)$. The company's profits, $R(x) - C(x)$, could be modeled by
1) $0.18x^3 + 6.02x^2 + 91.4x + 180$
2) $0.18x^3 - 5.98x^2 - 91.4x + 180$
3) $-0.18x^3 - 6.02x^2 + 91.4x - 180$
4) $0.18x^3 + 5.98x^2 + 99.4x + 180$

$P(x) = R(x) - C(x)$
$P(x) = x(95.4 - 6x) - 1(0.18x^3 + 0.02x^2 + 4x + 180)$
*you can use MC strategy at this point

6. Given $f(x) = 3x^2 + 7x - 20$ and $g(x) = x - 2$, state the quotient and remainder of $\frac{f(x)}{g(x)}$, in the form $q(x) + \frac{r(x)}{g(x)}$.

$$\begin{array}{c|ccc} 2 & 3 & 7 & -20 \\ & \downarrow & 6 & 26 \\ \hline & 3 & 13 & 6 \end{array}$$

$3x+13+\frac{6}{x-2}$

7. Is $x+2$ a factor of $p(x)=x^3-3x^2-8x+4$? Justify your answer.

$p(-2)=(-2)^3-3(-2)^2-8(-2)+4$

$p(-2)=0$

Yes, the remainder is 0

8. If $x-1$ is a factor of $x^3 - kx^2 + 2x$, what is the value of k?

$p(1)=0$

$0=(1)^3-k(1)^2+2(1)$

$0=1-k+2$

$0=-k+3$

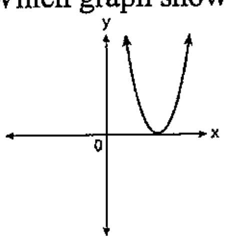
$-3 \quad\quad -3$

$\frac{-3}{-1}=\frac{-k}{-1}$

$3=k$

9. Which graph shows a quadratic function with two imaginary zeros? don't touch the x-axis

1)



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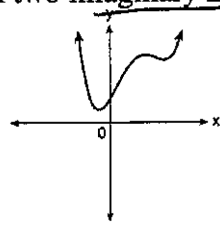

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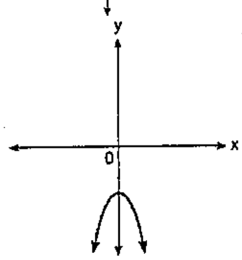
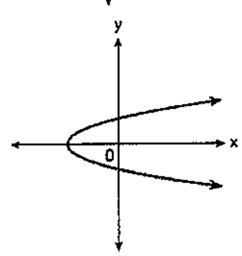
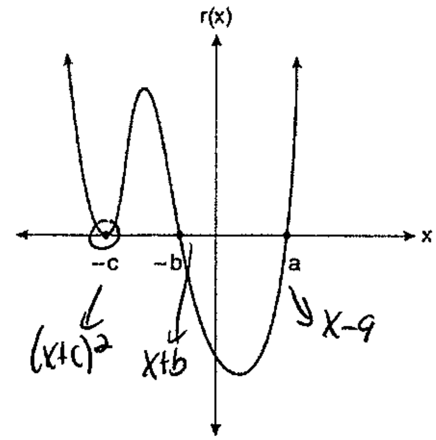


4)



10. A sketch of $r(x)$ is shown below.



An equation for $r(x)$ could be

1) $r(x) = (x-a)(x+b)(x+c)$
2) $r(x) = (x+a)(x-b)(x-c)^2$
3) $r(x) = (x+a)(x-b)(x-c)$
4) $r(x) = (x-a)(x+b)(x+c)^2$

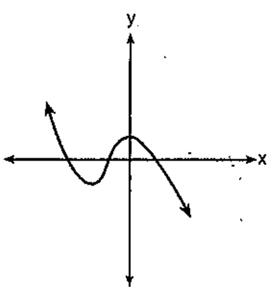
11. Which graph has the following characteristics?

- three real zeros
- as $x \to -\infty$, $f(x) \to -\infty$
- as $x \to \infty$, $f(x) \to \infty$

left down

right up

1)



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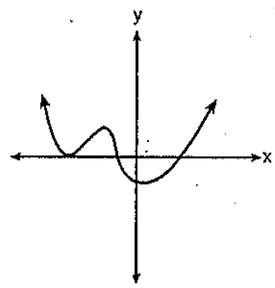
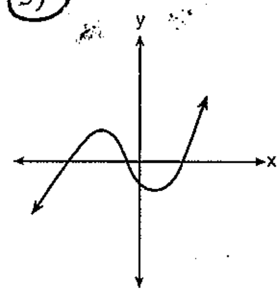
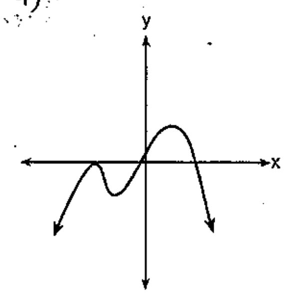


3)



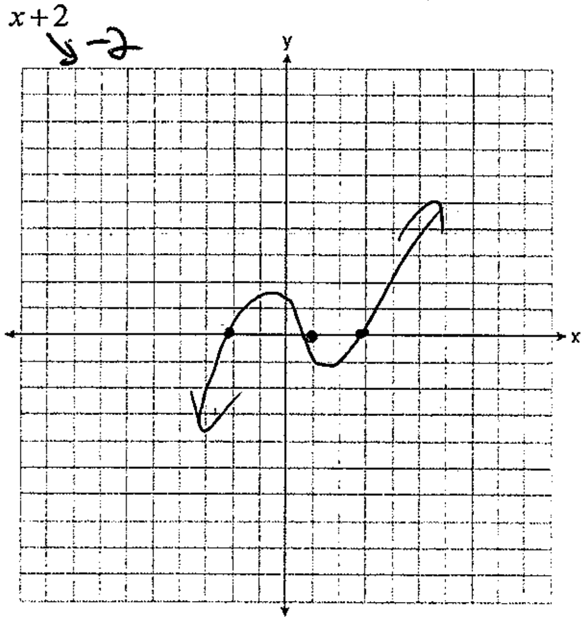
4)



12. On the grid below, sketch a cubic polynomial whose factors are $x-1$, $x-3$, and $x+2$

-2

1 3



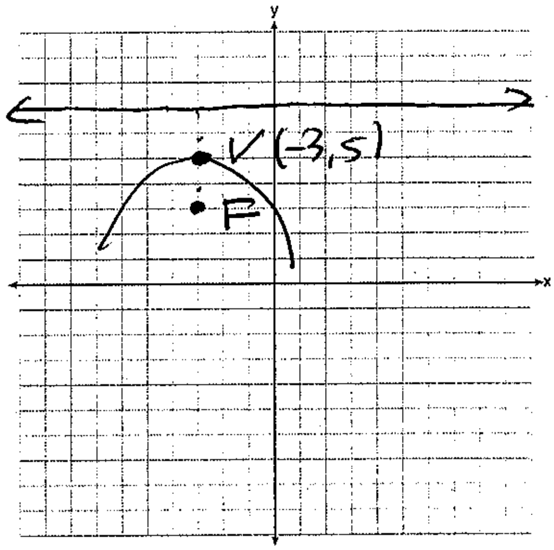
$i^2 = -1$
$i^3 = -i$

13. If x is a real number, express $2xi(i - 4i^2)$ in simplest $a + bi$ form.

$2xi^2 - 8xi^3$
$2x(-1) - 8x(-i)$
$-2x + 8xi$

14. Which equation represents the equation of the parabola with focus $(-3, 3)$ and directrix $y = 7$?

1) $y = \frac{1}{8}(x+3)^2 - 5$
2) $y = \frac{1}{8}(x-3)^2 + 5$
3) $y = -\frac{1}{8}(x+3)^2 + 5$
4) $y = -\frac{1}{8}(x-3)^2 + 5$



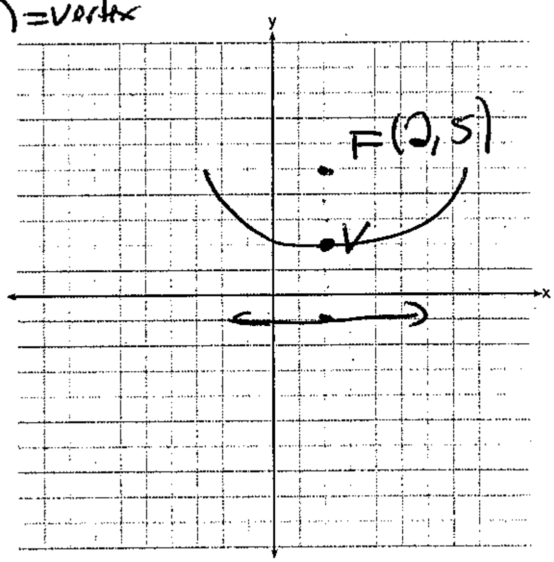
$y = \frac{1}{4p}(x-v)^2 + t$

$v = -3$ $\quad y = \frac{1}{4(-2)}(x+3)^2 + 5$
$t = 5$
$p = -2$ $\quad y = -\frac{1}{8}(x+3)^2 + 5$

$p = \frac{12}{4} = 3$

15. The parabola described by the equation $y = \frac{1}{12}(x-2)^2 + 2$ has the directrix at $y = -1$.
$(2,2)$ = vertex
The focus of the parabola is

1) $(2, -1)$
2) $(2, 2)$
3) $(2, 3)$
4) $(2, 5)$



16. If $f(x) = 3|x| - 1$ and $g(x) = 0.03x^3 - x + 1$, an approximate solution for the equation $f(x) = g(x)$ is → Y1 Y2 Intersect

1) 1.96
2) 11.29
3) ~~(−0.99, 1.96)~~
4) ~~(11.29, 32.87)~~

X only

* adjust window

2nd Trace, maximum

17. Which quadratic function has the largest maximum?

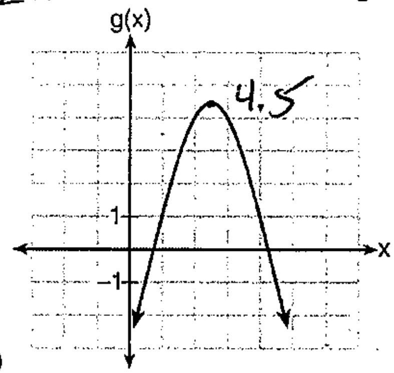
1) $h(x) = (3 - x)(2 + x)$ 6.25

3) $k(x) = -5x^2 - 12x + 4$ 11.2

2)

x	f(x)
−1	−3
0	5
1	9
2	9
3	5
4	−3

≈9.5

4) 

18. For $f(x) = x^3 + 3x^2 - x - 2$, find the zeros, relative minima, and relative maxima rounded to the *nearest tenth.*

Zeros	minimum value	maximum value
−3.1	−2.1	4.1
−.8		
.9		

19. What is the inverse of $f(x) = -6(x - 2)$?

1) $f^{-1}(x) = -2 - \frac{x}{6}$

2) $f^{-1}(x) = 2 - \frac{x}{6}$

3) $f^{-1}(x) = \frac{1}{-6(x-2)}$

4) $f^{-1}(x) = 6(x + 2)$

$y = -6(x-2)$

$\frac{x}{-6} = \frac{-6(y-2)}{-6}$

$-\frac{x}{6} = y - 2$

$+2 \quad +2$

$y = 2 - \frac{x}{6}$

or

$Y_1: -6(x-2)$

$Y_2: 2 - \frac{x}{6}$

$Y_3: x$

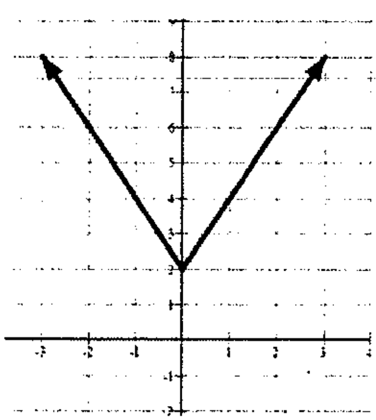
Symmetric to $y = x$

or

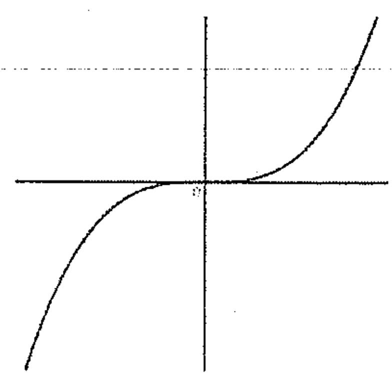
x	y
1	6
2	0
3	−6

x	y
6	1
0	2
−6	3

20. Determine graphically whether the following functions are even, odd, or neither

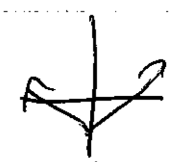


even because symmetric to the y-axis



odd because symmetric to the origin

$f(x) = |x| - 3$



even because symmetric to y-axis

21. Given the parent function $p(x) = \cos x$, which phrase best describes the transformation used to obtain the graph of $g(x) = \cos(x + a) - b$, if a and b are positive constants?

1) right a units, up b units
2) right a units, down b units
3) left a units, up b units
4) left a units, down b units

left a

down b

22. Which function shown below has a greater average rate of change on the interval [−2, 4]? Justify your answer.

$\frac{y_2-y_1}{x_2-x_1}$

x	f(x)
−4	0.3125
−3	0.625
−2	1.25
−1	2.5
0	5
1	10
2	20
3	40
4	80
5	160
6	320

$\frac{80-1.25}{4--2} = 13.125$

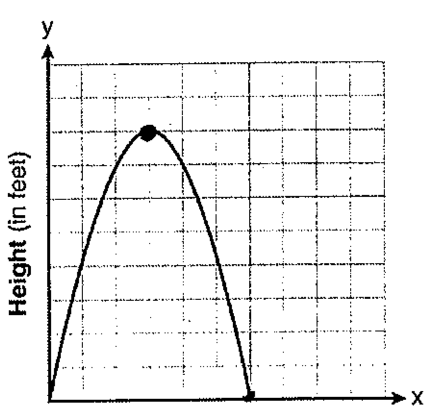
g(x)

$\frac{179--49}{4--2} = 38$

$g(x) = 4x^3 - 5x^2 + 3$

x	y
−2	−49
4	179

23. The graph below represents the parabolic path of a ball kicked by a young child. Find the average rate of change from 3 to 6 seconds. Explain its meaning in the context of the problem.



x	y
3	8
6	0

$\frac{y_2-y_1}{x_2-x_1}$ $\frac{0-8}{6-3} = \frac{-8}{3}$

On average, from 3 to 6 seconds the height of the ball decreases by $\frac{8}{3}$ ft per second.

24. Which value is *not* contained in the solution of the system shown below?

1) ~~−2~~
2) 2
3) ~~3~~
4) ~~−3~~

$$a + 5b - c = -20$$
$$4a - 5b + 4c = 19$$
$$-a - 5b - 5c = 2$$

$\begin{pmatrix} x \\ y \\ z \end{pmatrix} = A^{-1}B$

$\begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} -2 \\ -3 \\ 3 \end{pmatrix}$

25. Justify why $\dfrac{\sqrt[3]{x^2y^5}}{\sqrt[4]{x^3y^4}}$ is equivalent to $x^{\frac{-1}{12}}y^{\frac{2}{3}}$ using properties of rational exponents, where $x \neq 0$ and $y \neq 0$.

radicals are fractional exponents
get rid of parenthesis
negative exponents are fractions
Clean it up < multiply, divide, evaluate

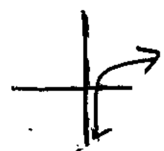
$\dfrac{(x^2y^5)^{\frac{1}{3}}}{(x^3y^4)^{\frac{1}{4}}}$ $\dfrac{x^{\frac{2}{3}}y^{\frac{5}{3}}}{x^{\frac{3}{4}}y^1}$ $x^{-\frac{1}{12}}y^{\frac{2}{3}}$

$\frac{2}{3} - \frac{3}{4} = -\frac{1}{12}$

$\frac{5}{3} - 1 = \frac{2}{3}$

26. Which statement about the graph of $c(x) = \log_6 x$ is *false*?

1) The asymptote has equation $y = 0$.
2) The graph has no y-intercept.
3) The domain is the set of positive reals.
4) The range is the set of all real numbers.

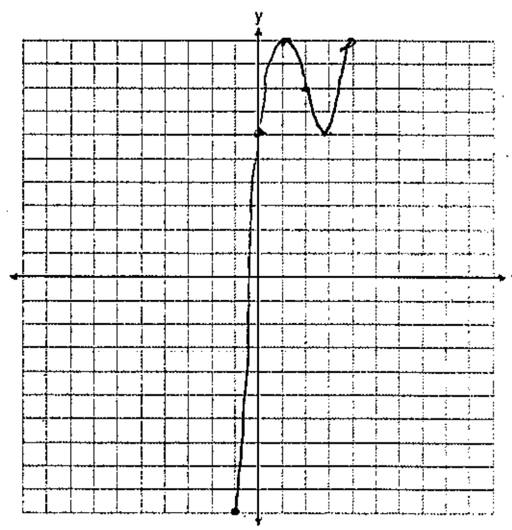


$x = 0$

27. $f(x) = x^3 - 6x^2 + 9x + 6$ on the domain $-1 \le x \le 4$

no arrows

x	y
−1	−10
0	6
1	10
2	8
3	6
4	10



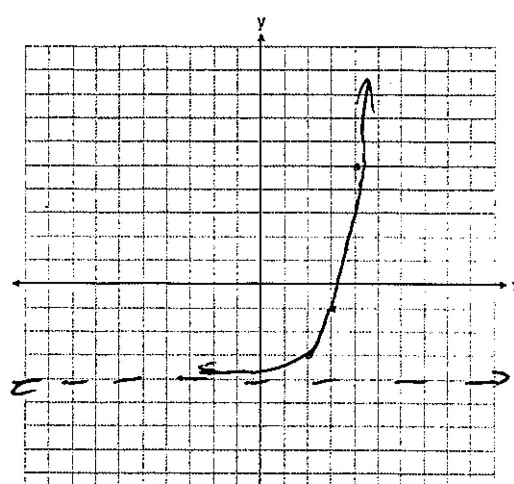
28. Graph $y = 3^{x-2} - 4$ on the axes provided and fill in the end behavior.

$x \to -\infty,\ f(x) \to -4$

$x \to \infty,\ f(x) \to \infty$

asymptote: $y = -4$

x	y
	−4
	−4
	−4
	−4
2	−3
3	−1
4	5



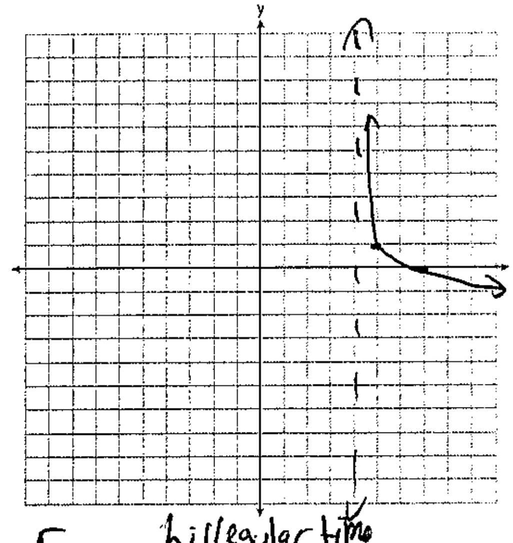
29. Graph $y = -\log_3(x-4)+1$ and fill in the end behavior

$x \to 4,\ f(x) \to \infty$

$x \to \infty,\ f(x) \to -\infty$

X	y
4	ERROR
5	1
7	0

asymptote: $x=4$



30. The population of Schlansky, Arizona increases by 18% every 3.2 years. If the population is currently 2750, what will be the population, to the nearest person, 12 years from now?

irregular time

$A = A$
$P = 2750$
$r = .18$
$t = 12$
$h = 3.2$

$A = P(1 \pm r)^{\frac{t}{h}}$
$A = 2750(1+.18)^{\frac{12}{3.2}}$
$A = 5116$

31. How much money is in a bank account opened 7.5 years ago with \$3125.67 that is compounded continuously with an interest rate of 5.26%?

Pert

$A = A$
$P = 3125.67$
$r = .0526$
$t = 7.5$

$A = Pe^{rt}$
$A = 3125.67e^{.0526(7.5)}$
$A = 4636.38$

32. A certain car depreciates at a rate of 15% each year. If the car was initially worth \$8125, what is the value of the car, rounded to the nearest cent, 11 years later?

no key words

$A = A$
$P = 8125$
$r = .15$
$t = 11$

$A = P(1 \pm r)^t$
$A = 8125(1-.15)^{11}$
$A = 1359.66$

half life

33. The half life of an element is 27 hours. If there were initially 4.2 kg of the substance, how much will remain after 50 hours? Round your answer to the nearest hundredth of a kg.

$A=A$
$P=4.2$
$t=50$
$h=27$

$A=P(\frac{1}{2})^{\frac{t}{h}}$
$A=4.2(\frac{1}{2})^{\frac{50}{27}}$
$A=1.16$

34. Sal has a savings account. He opened the account 6 years ago by putting in \$3000. If the interest is compounded daily at a rate of 5.6%, how much money is in the account now?

n formula $n=365$

$A=A$
$P=3000$
$r=.056$
$n=365$
$t=6$

$A=P(1+\frac{r}{n})^{nt}$
$A=3000(1+\frac{.056}{365})^{365(6)}$
$A=4197.91$

35. An equation to represent the value of a car after t months of ownership is $v=32,000(0.81)^{\frac{t}{12}}$. Which statement is *not* correct?

$V=32{,}000(.81^{\frac{1}{12}})^{t}$ $V=32{,}000(.98)^{t}$

1) The car lost approximately 19% of its value each month.
2) The car maintained approximately 98% of its value each month.
3) The value of the car when it was purchased was \$32,000.
4) The value of the car 1 year after it was purchased was \$25,920. $V=32{,}000(.81)^{\frac{12}{12}}=25{,}920$

$t=12$

36. A study of the annual population of the red-winged blackbird in Ft. Mill, South Carolina, shows the population, $B(t)$, can be represented by the function $B(t)=750(1.16)^{t}$, where the t represents the number of years since the study began. In terms of the monthly rate of growth, the population of red-winged blackbirds can be best approximated by the function

1) $B(t)=750(1.012)^{t}$
2) ~~$B(t)$~~ $=750(1.16)^{12t}$
3) $B(t)=750(1.012)^{12t}$
4) ~~$B(t)$~~ $=750(1.16)^{\frac{t}{12}}$

$1.16^{\frac{1}{12}}=1.012$

you get the monthly rate 12 times per year

37. The values below represent the cost of an ice cream sundae with one through four toppings. Write an explicit and recursive formula for a sequence that can be used to determine the cost of an ice cream cone with n toppings.

+.75 +.75 +.75

\$4.75 \$5.50 \$6.25 \$7.00

Explicit

$a_n=a_1+(n-1)d$
$a_n=4.75+(n-1).75$
$a_n=4.75+.75n-.75$
$a_n=.75n+4$

recursive

$a_1=4.75$
$a_n=a_{n-1}+.75$

38. The population of Jamesburg for the years 2010-2013, respectively, was reported as follows:
250,000 250,937 251,878 252,822
How can this sequence be recursively modeled?

$250,937 - 250,000 = 937$
$251,878 - 250,937 = 941$

$\frac{250,937}{250,000} = 1.00375$

$\frac{251,878}{250,937} = 1.00375$

this is correct but not recursive

1) $j_x = 250,000(1.00375)^{x-1}$
2) $j_x = 250,000 + 937^{(x-1)}$
3) $j_1 = 250,000$, $j_x = 1.00375 j_{x-1}$
4) $j_1 = 250,000$, $j_x = j_{x-1} + 937$

39. Find the first 4 terms of the recursive sequence $a_1 = -3$, $a_n = 4 - 3a_{n-1}$

$-3, 13, -35, 109$

$a_2 = 4-3(-3)$
$a_2 = 13$
$a_3 = 4-3(13)$
$a_3 = -35$
$a_4 = 4-3(-35)$
$a_4 = 109$

40. The sequence defined by $r_1 = 15$ and $r_n = 0.75r_{n-1}$ best models which scenario?

decreasing by 25%.

1) Gerry's $15 allowance is increased by $0.75 each week.
2) A store that has not sold a $15 item reduces the price by $0.25 each week until someone purchases it.
3) A 15-gram sample of a chemical compound decays at a rate of 75% per hour.
4) A picture with an area of 15 square inches is reduced by 25% over and over again to make a proportionally smaller picture.

41. Alexa earns $33,000 ($a_1$) in her first year of teaching and earns a 4% increase ($r = 1.04$) in each successive year. Find Alexa's total earnings for her first 15 years (n) of teaching, to the *nearest cent.*

$a_1 = 33000$
$r = 1.04$
$n = 15$

$S_n = \frac{a_1 - a_1(r)^n}{1-r}$

$S_{15} = \frac{33,000 - 33,000(1.04)^{15}}{1-1.04}$

$S_{15} = 660,778.39$

42. Kristin wants to increase her running endurance. According to experts, a gradual (a_1) mileage increase of 10% ($r = 1.10$) per week can reduce the risk of injury. If Kristin runs 8 miles in week one, which expression can help her find the total number of miles she will have run over the course of her 6-week (n) training program?

1) $\sum_{x=1}^{6} 8(1.10)^{x-1}$
2) $\sum_{x=1}^{6} 8(1.10)^{x}$
3) $\frac{8 - 8(1.10)^6}{0.90}$
4) $\frac{8 - 8(0.10)^x}{1.10}$

$a_1 = 8$
$r = 1.10$
$n = 6$

$S_n = \frac{a_1 - a_1(r)^n}{1-r}$

$\frac{8 - 8(1.10)^6}{1 - 1.10}$

$\frac{8 - 8(1.10)^6}{-.10}$

$S_n = \sum_{n=1}^{n} a_1(r)^{n-1}$

$\sum_{n=1}^{6} 8(1.10)^{n-1}$

43. Using the formula below, determine the monthly payment on a 5-year car loan with a monthly percentage rate of 0.625% for a car with an original cost of \$21,000 and a \$1000 down payment, to the *nearest cent.*

$$P_n = PMT\left(\frac{1-(1+i)^{-n}}{i}\right)$$

P_n = present amount borrowed T−D $21000-1000=20000$
n = number of monthly pay periods $12(5)=60$
PMT = monthly payment X
i = interest rate per month $.00625$

$$20{,}000 = x\left(\frac{1-(1+.00625)^{-60}}{.00625}\right)$$

$$\frac{20{,}000}{49.9..} = \frac{x(49.9..)}{49.9}$$

$400.76 = x$

The affordable monthly payment is \$300 for the same time period. Determine an appropriate down payment, to the *nearest dollar*.

Pmt

find P

$P_n = P$
$n = 60$
$PMT = 300$
$i = .00625$

$$P = 300\left(\frac{1-(1+.00625)^{-60}}{.00625}\right)$$

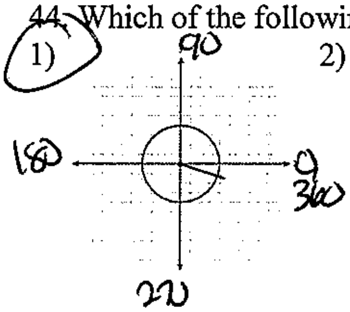
$P = 14971...$

21,000
−14,971..
\$6028

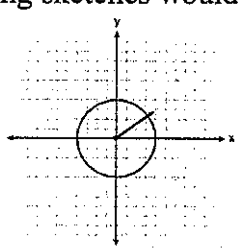
44. Which of the following sketches would represent 6 radians?

$6 \cdot \frac{180}{\pi} = 344$

1)



2)



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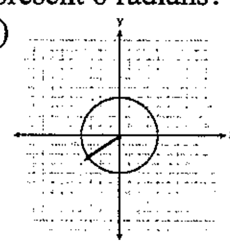
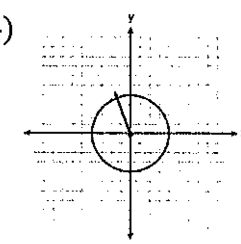


4)



45. Angle θ is in standard position and (-2,3) is a point on the terminal side of θ. Find:

a) cos ϑ $-\frac{2}{\sqrt{13}}$

b) sin ϑ $\frac{3}{\sqrt{13}}$

c) tan ϑ $-\frac{3}{2}$

d) sec ϑ $-\frac{\sqrt{13}}{2}$

e) csc ϑ $\frac{\sqrt{13}}{3}$

f) cot ϑ $-\frac{2}{3}$

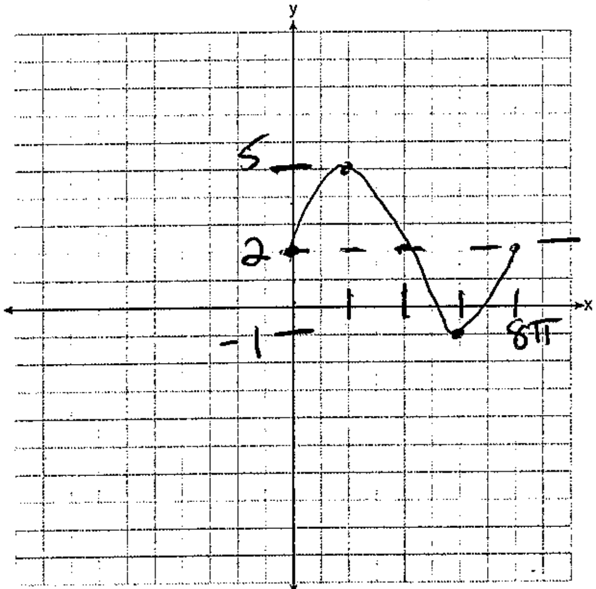
S A T C

3 2 $\sqrt{13}$

$a^2+b^2=c^2$
$2^2+3^2=c^2$
$4+9=c^2$
$\sqrt{13}=\sqrt{c^2}$

ampsinfreqxshift

46. Graph one cycle of $y=3\sin\frac{1}{4}x+2$ on the accompanying set of axes



amp=3
+sin
freq= $\frac{1}{4}$
shift=2

$P=\frac{2\pi}{\frac{1}{4}}$

$2\pi\cdot\frac{4}{1}=8\pi$

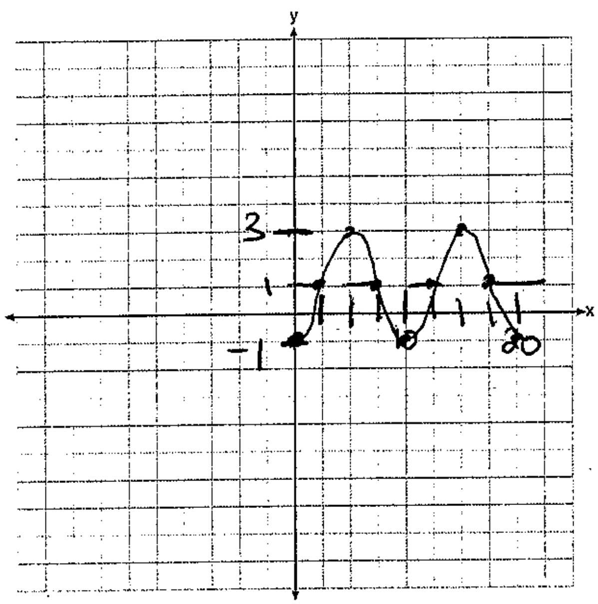
ampsinfreqxshift

47. Graph $y=-2\cos\frac{\pi}{5}x+1$ over the interval $[0,20]$

amp=2
-cos
freq= $\frac{\pi}{5}$
shift=1

Period = $\frac{2\pi}{\frac{\pi}{5}}$

$\frac{2\cancel{\pi}}{1}\cdot\frac{5}{\cancel{\pi}}=10$



48. The depth of the water at a marker 20 feet from the shore in a bay is depicted in the graph below.

If the depth, d, is measured in feet and time, t, is measured in hours since midnight, what is an equation for the depth of the water at the marker?

1) $d = 5\cos\left(\frac{\pi}{6}t\right) + 9$

2) $d = 9\cos\left(\frac{\pi}{6}t\right) + 5$

3) $d = 9\sin\left(\frac{\pi}{6}t\right) + 5$

4) $d = 5\sin\left(\frac{\pi}{6}t\right) + 9$

$\text{midline} = \frac{\min+\max}{2}$ $f = \frac{2\pi}{p}$

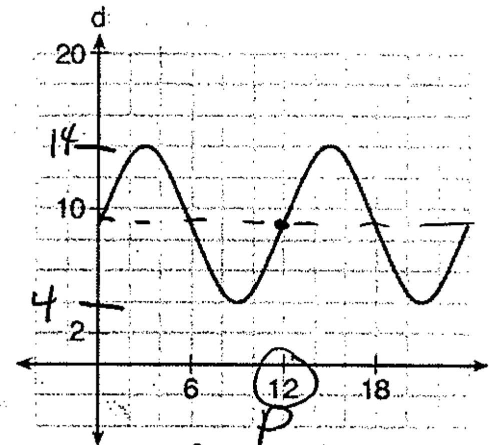
$\text{midline} = \frac{4+14}{2}$ $f = \frac{2\pi}{12}$

$\text{midline} = \frac{18}{2}$ $f = \frac{\pi}{6}$

$\text{midline} = 9$

$y = \text{amp}\sin \text{freq}\, x\, \text{shift}$

$y = 5\sin\frac{\pi}{6}x + 9$



amp sin freq x shift

49. Which statement is *incorrect* for the graph of the function $y = -3\cos\left[\frac{\pi}{3}(x-4)\right] + 7$?

1) The period is 6.
2) The amplitude is 3.
3) The range is [4,10].
4) The midline is $y = -4$.

10

7

4

6

amp = 3

– cos

freq = $\frac{\pi}{3}$

shift = 7

$p = \frac{2\pi}{\frac{\pi}{3}}$

$2\pi \cdot \frac{3}{\pi} = 6$

50. As θ increases from π to $\frac{3\pi}{2}$ radians, the graph of $y = \sin\theta$ will

$y = \sin x$

window:

Xmin: π

Xmax: $\frac{3\pi}{2}$

1) Decrease from 1 to 0
2) Decrease from 0 to -1
3) Increase from -1 to 0
4) Increase from 0 to 1

51. The probability of event A is .27. The probability of event B is .36. The probability of both events happening is .11. What is the probability that event A or event B happens?

and

$P(A\cup B) = P(A) + P(B) - P(A\cap B)$

$P(A\cup B) = .27 + .36 - .11$

$P(A\cup B) = .52$

52. The probability of event A happening is 14% and the probability of event B happening is 18%. The probability that event A or event B happens is 20%. What is the probability that event A and event B happens?

$P(A\cap B) = P(A) + P(B) - P(A\cup B)$

$P(A\cap B) = .14 + .18 - .20$

$P(A\cap B) = .12$

$P(B)$ $P(A)$

53. On a given school day, the probability that Nick oversleeps is 48% and the probability he has a pop quiz is 25%. Assuming these two events are independent, what is the probability that Nick oversleeps and has a pop quiz on the same day?

$P(A \cap B) = P(A) \cdot P(B)$

$P(A \cap B) = .48 \cdot .25$

$P(A \cap B) = .12$

54. A public opinion poll was taken to explore the relationship between age and support for a candidate in an election. The results of the poll are summarized in the table below.

Age	For	Against	No Opinion	
21–40	30	12	8	50
41–60	20	40	15	75
Over 60	25	35	15	75
	75	87	38	200

1 thing: $\frac{\quad}{\text{total total}}$

2 things: and $\frac{\quad}{\text{total total}}$

given: condition last

no and/given: condition first

What is the probability that someone is 41-60 given that they have no opinion?

condition

$\frac{15}{38}$

What is the probability that someone is over 60 and against the candidate?

$\frac{35}{200}$

What is the probability that someone is for the candidate?

$\frac{75}{200}$

What percent of the 21-40 age group was for the candidate?

condition

$\frac{30}{50} = .60(100)$

60%

55. The results of a poll of 200 students are shown in the table below:
For this group of students, do these data suggest that gender and preferred music styles are independent of each other? Justify your answer.

	B Preferred Music Style			
	Techno	Rap	Country	
A Female	54	25	27	106
Male	36	40	18	94
	90	65	45	200

$P(A \cap B) \neq P(A) \cdot P(B)$

$\frac{54}{200} \neq \frac{90}{200} \cdot \frac{106}{200}$

$\frac{27}{100} \neq \frac{477}{2000}$

not independent

normal cdf

56. The heights of women in the United States are normally distributed with a mean of 64 inches and a standard deviation of 2.75 inches. What is the percent of women whose heights are less than 60 inches rounded to the *nearest whole percent*? Out of 250 women, to the *nearest woman,* how many would be expected to be taller than 69 inches?

lower = 0
upper = 60
$\mu = 64$
$\sigma = 2.75$

.072...(100)

$\boxed{7\%}$

lower: 69
upper: 999999
μ: 64
σ: 2.75

.034...(250)

$\boxed{9}$

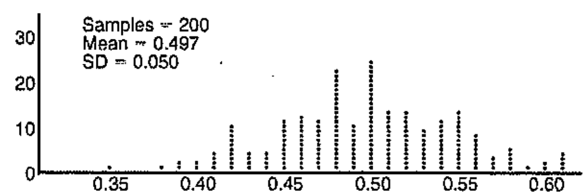
57. A doctor wants to test the effectiveness of a new drug on her patients. She separates her sample of patients into two groups and administers the drug to only one of these groups. She then compares the results. Which type of study *best* describes this situation?
1) census
2) survey
3) observation
4) controlled experiment

58. A survey is being conducted about American's favorite musicians. Which of the following survey methods would most likely produce a random sample?
1) Asking every 20th person at a Green Day concert
2) Asking every 10th person at a vintage record store
3) Asking every 10th person at the Westbury Public Library
4) Sending out surveys to random households across the country.

59. Anne has a coin. She does not know if it is a fair coin. She flipped the coin 100 times and obtained 73 heads and 27 tails. She ran a computer simulation of 200 samples of 100 fair coin flips. The output of the proportion of heads is shown below.

$\frac{73}{100} = .73$

Given the results of her coin flips and of her computer simulation, which statement is most accurate?
1) 73 of the computer's next 100 coin flips will be heads.
2) 50 of her next 100 coin flips will be heads.
3) Her coin is not fair.
4) Her coin is fair.



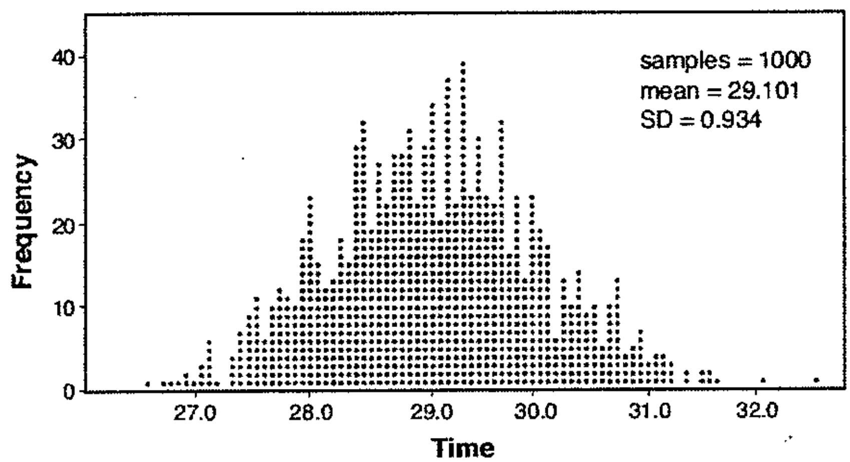
(.397, .597) CI = .497 + 2(.050) = .597
.497 − 2(.050) = .397

.73 is not an expected value for a fair coin.

60. A radio station claims to its advertisers that the mean number of minutes commuters listen to the station is 30. The station conducted a survey of 500 of their listeners who commute. The sample statistics are shown below.

$\bar{x}$	29.11
s_x	20.718

A simulation was run 1000 times based upon the results of the survey. The results of the simulation appear below.



Based on the simulation results, is the claim that commuters listen to the station on average 30 minutes plausible? Explain your response including an interval containing the middle 95% of the data, rounded to the *nearest hundredth*.

confidence interval

$$CI = 29.101 + 2(.934) = 30.97$$
$$29.101 - 2(.934) = 27.23$$

[27.23, 30.97]

Yes, 30 is inside the confidence interval.

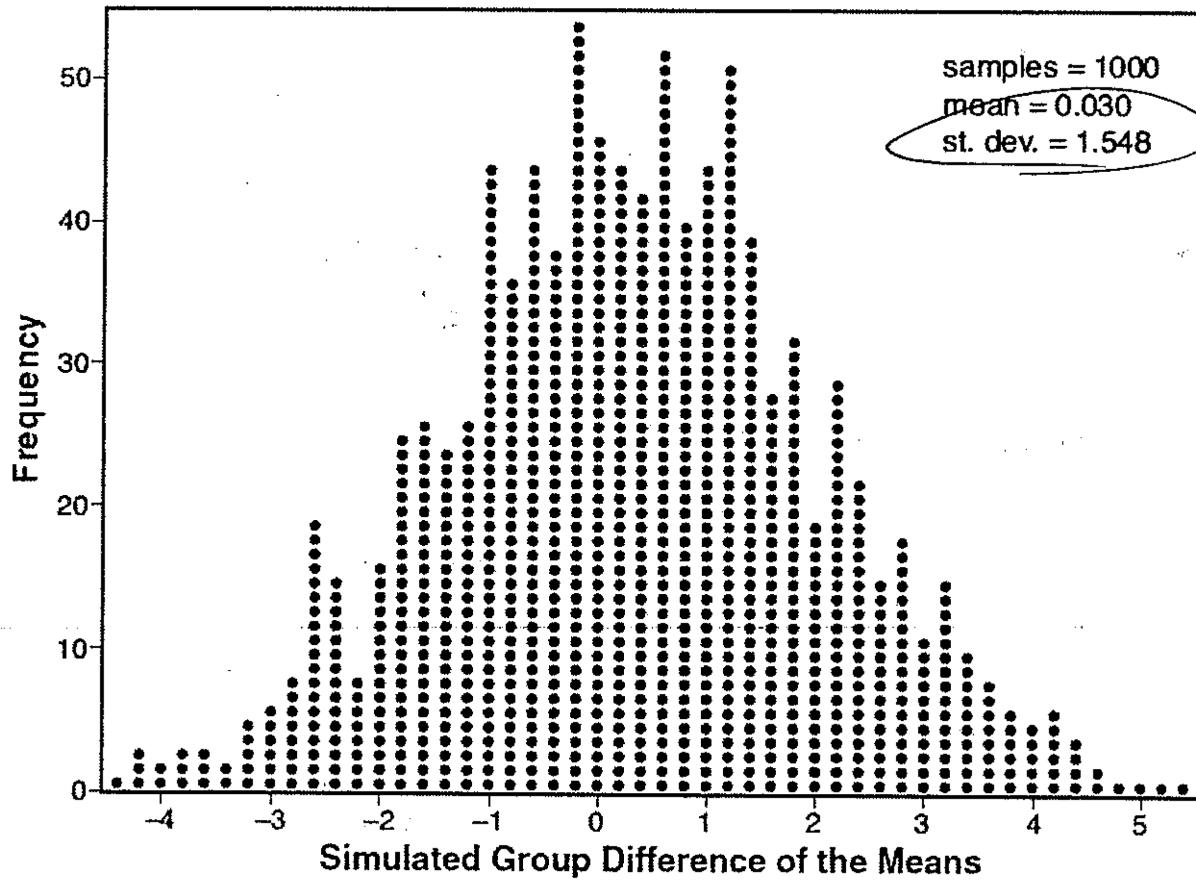
61. Joseph was curious to determine if scent improves memory. A test was created where better memory is indicated by higher test scores. A controlled experiment was performed where one group was given the test on scented paper and the other group was given the test on unscented paper. The summary statistics from the experiment are given below.

	Scented Paper	Unscented Paper
$\bar{x}$	23	18
s_x	2.898	2.408

$23-18=5$

on average, the scented paper group scored 5 points higher than the unscented paper group

Calculate the difference in means in the experimental test grades (scented -unscented). A simulation was conducted in which the subjects' scores were rerandomized into two groups 1000 times. The differences of the group means were calculated each time. The results are shown below.



Confidence interval

Use the simulation results to determine the interval representing the middle 95% of the difference in means, to the *nearest hundredth*. Is the difference in means in Joseph's experiment statistically significant based on the simulation? Explain.

$CI = .030 + 2(1.548) = 3.13$ $(-3.07, 3.13)$

$.030 - 2(1.548) = -3.07$

Yes, 5 is not an expected value due to random chance.

Yes, 5 is not in the confidence interval.

62. Jean invested \$380 in stocks. Over the next 5 years the value of her investment grew, as shown in the accompanying table.

Years Since Investment (x)	Value of Stock, in Dollars (y)
0	380
1	395
2	411
3	427
4	445
5	462

Write the exponential regression equation for this set of data, rounding all values to *two decimal places*. Using this equation, find the value of her stock, to the *nearest dollar*, 10 years after her initial purchase.

ExpReg

$y=a(b)^x$

$a=379.92$

$b=1.04$

$y=379.92(1.04)^x$

$y=379.92(1.04)^{10}$

$y=562$

63. After sitting out of the refrigerator for a while, a turkey at room temperature (68°F) is placed into an oven at 8 a.m., when the oven temperature is 325°F. Newton's Law of Heating explains that the temperature of the turkey will increase proportionally to the difference between the temperature of the turkey and the temperature of the oven, as given by the formula below. If the value of k is .066, determine the Fahrenheit temperature of the turkey, to the *nearest degree*, at 3 p.m.

T_0 T_a

$T=325+(68-325)e^{-.066(7)}$

$T = T_a + (T_0 - T_a)e^{-kt}$

T_a = the temperature surrounding the object $=325$

$T=163°$

T_0 = the initial temperature of the object $=68$

t = the time in hours $=$ 8Am − 3Pm = 7

T = the temperature of the object after t hours T

k = decay constant .066

Factor
GCF
2 terms DOTS or Cubes
3 terms Trinomial/Tricky Tri
4 or more Grouping
Can you factor further?

64. Factor the following

a) $\sqrt{36}-\sqrt{25}x^2$ DOTS

$(6+5x)(6-5x)$

b) $x^2 - 7x + 12$

$(x-4)(x-3)$

c) $\frac{3x^2+9x-12}{3}$ GCF

trinomial

$3(x^2+3x-4)$

$3(x+4)(x-1)$

GCF

d) $\frac{6x^2-54}{6 \quad 6}$

$6(x^2-9)$ DOTS

$6(x+3)(x-3)$

Tricky Tri

e) $2x^2+7x-4$

x^2+7x-8

$\frac{(x+8)(x-1)}{2 \quad\quad 2}$

$(x+4)(2x-1)$

$(2x^2+8x)(-1x-4)$

$\frac{2x^2+8x}{2x \quad 2x} \quad \frac{-1x-4}{-1 \quad -1}$

$2x(x+4)-1(x+4)$

$(2x-1)(x+4)$

f) $(x^3+3x^2)(-9x-27)$ Grouping

$\frac{x^3+3x^2}{x^2 \quad x^2} \quad \frac{-9x-27}{-9 \quad -9}$

$x^2(x+3)-9(x+3)$

$(x^2-9)(x+3)$

$(x+3)(x-3)(x+3)$

grouping

g) $3x^3 + x^2 - 12x^2 - 4x - 63x - 21$

$x^2 \quad x^2 \quad -4x \quad -4x \quad -21 \quad -21$

$x^2(3x+1) - 4x(3x+1) - 21(3x+1)$

Trinomial $(x^2-4x-21)(3x+1)$

$(x-7)(x+3)(3x+1)$

$a=y \quad b=5$ cubes

i) $y^3 - 125$

$a^3-b^3=(a-b)(a^2+ab+b^2)$

$y^3-125=(y-5)(y^2+5y+25)$

substitution trinomial

$y=x^2-2x$

h) $(x^2-2x)^2-11(x^2-2x)+24$

$y^2-11y+24$

$(y-8)(y-3)$ Trinomials

$(x^2-2x-8)(x^2-2x-3)$

$(x-4)(x+2)(x-3)(x+1)$

65. Express the following in simplest form: Factor

Cancel common factors

$\frac{10-5x}{x^2+2x-8}$ GCF Trinomial

$\frac{5\cancel{(2-x)}(-1)}{(x+4)\cancel{(x-2)}} \quad -\frac{5}{x+4}$

mr. x^2!

66. Solve $x^2+5x=2x+40$ algebraically

$-2x-40 \quad -2x-40$

Trinomial $x^2+3x-40=0$

$(x+8)(x-5)=0$

$x=-8 \quad x=5$

67. Solve the equation $x^2+2x=-8$ algebraically and express the answer in simplest $a+bi$ form.

$+8 \quad +8$

quadratic formula

$x^2+2x+8=0 \qquad x=\frac{-b\pm\sqrt{b^2-4ac}}{2a}$

$a=1$

$b=2$

$c=8$

$x=\frac{-2\pm\sqrt{(2)^2-4(1)(8)}}{2(1)}$

$x=\frac{-2\pm\sqrt{-28}}{2}$

$\sqrt{-28}$

$i\sqrt{28}$

$i\sqrt{4}\sqrt{7}$

$2i\sqrt{7}$

$x=\frac{-2\pm 2i\sqrt{7}}{2}$

$x=-1\pm i\sqrt{7}$

68. Solve $x^3 + 5x^2 = 4x + 20$ algebraically.

$-4x-20 \quad -4x-20$

$x^3+5x^2-4x-20=0$

$x^2 \quad x^2 \quad -4 \quad -4$

$x^2(x+5)-4(x+5)=0$

$(x^2-4)(x+5)=0$

$(x+2)(x-2)(x+5)=0$

$x=-2 \quad x=2 \quad x=-5$

69. Solve the following equation algebraically:

$\sqrt{2x-7}+x=5$

$-x \quad -x$

$(\sqrt{2x-7})^2=(5-x)^2$

	5	$-x$
5	25	$-5x$
$-x$	$-5x$	$+x^2$

$x^2-10x+25$

$2x-7=x^2-10x+25$

$-2x+7 \quad -2x+7$

$0=x^2-12x+32$

$(x-8)(x-4)$

~~$x=8$~~ $x=4$

70. Solve algebraically for x: $\left(\frac{3}{x}\right)+\left(\frac{x}{x+2}\right)=-\left(\frac{2}{x+2}\right)$

$x(x+2) \quad x(x+2) \quad x(x+2)$

$3(x+2)+x^2=-2x$

$3x+6+x^2=-2x$

$+2x \quad +2x$

$x^2+5x+6=0$

$(x+3)(x+2)=0$

$x+3=0 \quad x+2=0$

$-3 \quad -3 \quad -2 \quad -2$

$x=-3$ ~~$x=-2$~~

71. Solve algebraically for x:

$12+3(1.2)^{2x}=100$

$-12 \quad -12$

$\frac{3(1.2)^{2x}}{3}=\frac{88}{3}$

$\log(1.2)^{2x}=\log\frac{88}{3}$

$\frac{2x\log(1.2)}{2\log 1.2}=\frac{\log\left(\frac{88}{3}\right)}{2\log 1.2}$

$x=\frac{\log\left(\frac{88}{3}\right)}{2\log 1.2}$

$x=9.3$

72. Solve the following system of equations algebraically for x and y

$(x+2)^2+(y-4)^2=40$

$y=x+2$

$(x+2)^2+(x+2-4)^2=40$

$(x+2)^2+(x-2)^2=40$

$x^2+\cancel{4x}+4+x^2\cancel{-4x}+4=40$

$2x^2+8=40$

$-40\ \ -40$

$\begin{array}{c|cc} & x & +2 \\ \hline x & x^2 & +2x \\ +2 & +2x & +4 \end{array}$

x^2+4x+4

$\begin{array}{c|cc} & x & -2 \\ \hline x & x^2 & -2x \\ -2 & -2x & +4 \end{array}$

x^2-4x+4

$\frac{2x^2-32}{2}=\frac{0}{2}$

$x^2-16=0$

$(x+4)(x-4)=0$

$x=-4$ | $x=4$
$y=x+2$ | $y=x+2$
$y=-4+2$ | $y=4+2$
$y=-2$ | $y=6$
$(-4,-2)$ | $(4,6)$

73. Solve the following system of equations algebraically for all values of x, y, and z:

A $x+2y-3z=-2$

B $2x-2y+z=7$

C $x+y+2z=-4$

A and B

$x+2y-3z=-2$

$+\ 2x-2y+z=7$

D $3x-2z=5$

B and C

$1(2x-2y+z=7)$

$2(x+y+2z=-4)$

$2x-2y+z=7$

$+\ 2x+2y+4z=-8$

E $4x+5z=-1$

D and E

$5(3x-2z=5)$

$2(4x+5z=-1)$

$15x-10z=25$

$+\ 8x+10z=-2$

$\frac{23x}{23}=\frac{23}{23}$

$x=1$

$3(1)-2z=5$

$3-2z=5$

$-3\ \ \ \ -3$

$\frac{-2z}{-2}=\frac{2}{-2}$

$z=-1$

$x+y+2z=-4$

$1+y+2(-1)=-4$

$1+y-2=-4$

$y-1=-4$

$+1\ \ +1$

$y=-3$

74. A car that was bought for \$24,320 is worth \$9,200 after 7 years. To the *nearest percent*, what is the annual rate of depreciation?

$A=9200$

$P=24320$

$r=r$

$t=7$

$A=P(1\pm r)^t$

$\frac{9200}{24320}=\frac{24320(1-r)^7}{24320}$

$(.378\ldots)^{\frac{1}{7}}=((1-r)^7)^{\frac{1}{7}}$

$.87\ldots=1-r$

$-1\ \ \ \ -1$

$\frac{-.13\ldots}{-1}=\frac{-r}{-1}$

$.13=r$

$.13\ldots(100)=13\%$

P $\qquad\qquad\qquad\qquad$ $A=Pe^{rt}$

75. Susie invests \$500 in an account that is compounded continuously at an annual interest rate of 5%. Approximately how many years will it take for Susie's money to double?

r

$A=2(500)$

$A=2(500)$

$P=500$

$r=.05$

$t=t$

$A=Pe^{rt}$

$\frac{2(500)}{500}=\frac{500e^{.05t}}{500}$

$\log 2 = \log e^{.05t}$

$\frac{\log 2}{.05\log e}=\frac{.05t\log e}{.05\log e}$

$14=t$

76. One of the medical uses of Iodine–131 (I–131), a radioactive isotope of iodine, is to enhance x-ray images. The half-life of I–131 is approximately 8.02 days. A patient is injected with 20 milligrams of I–131. Determine, to the *nearest day*, the amount of time needed before the amount of I–131 in the patient's body is approximately 7 milligrams.

h $\quad P$ $\quad A$

$A=P\left(\frac{1}{2}\right)^{\frac{t}{h}}$

$A=7$

$P=20$

$t=t$

$h=8.02$

$\frac{7}{20}=\frac{20\left(\frac{1}{2}\right)^{\frac{t}{8.02}}}{20}$

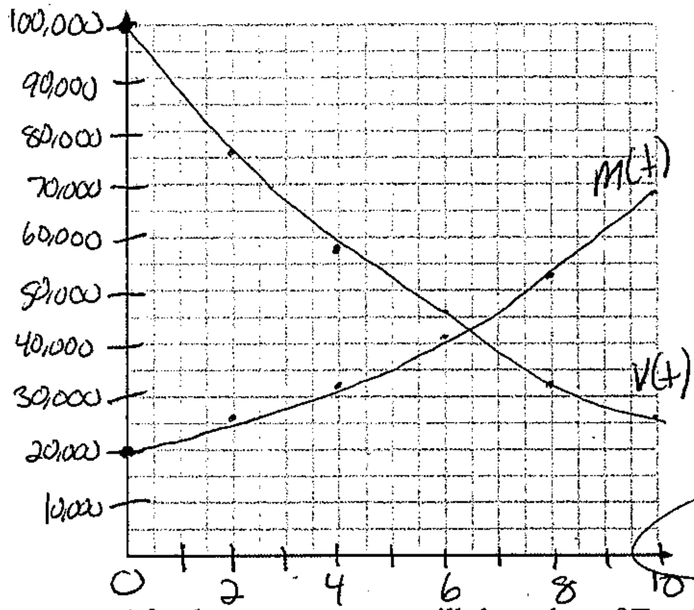
$\log\frac{7}{20}=\log\frac{1}{2}^{\frac{t}{8.02}}$

$8.02\left(\log\left(\frac{7}{20}\right)\right)=\left(\frac{t}{\cancel{8.02}}\log\left(\frac{1}{2}\right)\right)\cancel{8.02}$

$\frac{8.02\log\left(\frac{7}{20}\right)}{\log\left(\frac{1}{2}\right)}=\frac{t\log\left(\frac{1}{2}\right)}{\log\left(\frac{1}{2}\right)}$

$12=t$

77. The value of Tom's bank account is currently 100000 and is decreasing according to the equation $V(t) = 100000(.876)^t$. The amount of money he has paid for his mortgage can be represented by the equation $M(t) = 20000(1.1304)^t$. Graph and label $V(t)$ and $M(t)$ over the interval $[0,10]$.



V(t)

x	y
0	100000
2	76738
4	58887
6	45188
8	34676
10	26610

M(t)

x	y
0	20000
2	25556
4	32656
6	41728
8	53320
10	68132

$x \geq \frac{10}{20}$ $\quad y \geq 5000$ $\quad$ scale

$x = .5$ $\quad y = 5000$

After how many years will the value of Tom's bank account be equal to the amount of money he paid for his mortgage? Round your answer to the *nearest tenth of a year*. Tom will open a new bank account when the value of his account is \$30,000. After how many years, to the *nearest hundredth of a year*, will that happen?

intersection

$V(t) = 30{,}000$

41, 42 Intersect
6.3 years

$$\frac{30{,}000}{100{,}000} = \frac{100{,}000(.876)^t}{100{,}000}$$

$$\log .3 = \log .876^t$$

$$\frac{\log .3}{\log .876} = \frac{t \log .876}{\log .876}$$

$$9.09 = t$$

or

41, 42 Intersect

79. Griffin is riding his bike down the street in Churchville, N.Y. at a constant speed, when a nail gets caught in one of his tires. The height of the nail above the ground, in inches, can be represented by the trigonometric function $f(t) = -13\cos(0.8\pi t) + 13$, where t represents the time (in seconds) since the nail first became caught in the tire. Determine the period of $f(t)$. Interpret what the period represents in this context. On the grid below, graph *at least one* cycle of $f(t)$ that includes the y-intercept of the function.

amp sin freq x shift

$f(t) = -13\cos(0.8\pi t) + 13$

amp = 13

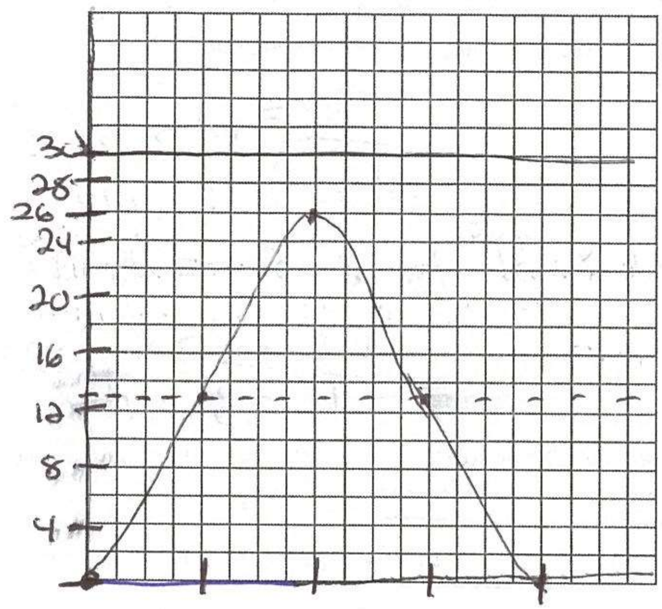
-cos

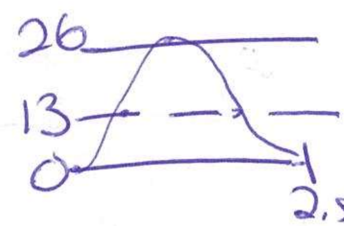
freq = 0.8π

shift = 13

$P = \frac{2\pi}{0.8\pi}$

$P = 2.5$





Does the height of the nail ever reach 30 inches above the ground? Justify your answer.

No, its maximum ~~value~~ height is 26.

79. The table below gives air pressures in kPa at selected altitudes above sea level measured in kilometers.

x	**Altitude** (km)	0	1	2	3	4	5
y	**Air Pressure** (kPa)	101	90	79	70	62	54

Write an exponential regression equation that models these data rounding all values to the *nearest thousandth*. Use this equation to algebraically determine the altitude, to the *nearest hundredth* of a kilometer, when the air pressure is 29 kPa.

ExpReg

$y = a(b)^x$

$y = 101.523(.883)^x$

$\frac{29}{101.523} = \frac{101.523(.883)^x}{101.523}$

$\log .2856... = \log .883^x$

$\frac{\log .2856}{\log .883} = \frac{x \log .883}{\log .883}$

$10.07 = x$

80. A Foucault pendulum can be used to demonstrate that the Earth rotates. The time, t, in seconds, that it takes for one swing or period of the pendulum can be modeled by the equation $t = 2\pi\sqrt{\frac{L}{g}}$ where L is the length of the pendulum in meters and g is a constant of 9.81 m/s^2. The first Foucault pendulum was constructed in 1851 and has a pendulum length of 67 m. Determine, to the *nearest tenth of a second*, the time it takes this pendulum to complete one swing. Another Foucault pendulum at the United Nations building takes 9.6 seconds to complete one swing. Determine, to the *nearest tenth of a meter*, the length of this pendulum.

t = t = time for one swing

67 = L = Length of Pendulum

9.81 g = Constant

$t = 2\pi\sqrt{\frac{67}{9.81}}$

$t = 16.4$ seconds

$t = 9.6$

$L = L$

$g = 9.81$

$\frac{9.6}{2\pi} = \frac{2\pi\sqrt{\frac{L}{9.81}}}{2\pi}$

$(1.527..)^2 = \left(\sqrt{\frac{L}{9.81}}\right)^2$

$9.81(2.33..) = \left(\frac{L}{\cancel{9.81}}\right)\cancel{9.81}$

$22.9 = L$