

Dilating Functions

State the transformations that were performed on $f(x)$ to produce $g(x)$

1. $g(x) = 2f(x)$

vertical stretch by a scale factor of 2

2. $g(x) = f(2x)$

horizontal shrink/compression by a scale factor of $\frac{1}{2}$

3. $g(x) = \frac{1}{3}f(x)$

vertical shrink by a scale factor of $\frac{1}{3}$

4. $g(x) = f\left(\frac{1}{3}x\right)$

horizontal stretch by a scale factor of 3

5. $g(x) = f(4x)$

horizontal compression by a scale factor of $\frac{1}{4}$

6. $g(x) = \frac{2}{5}f(x)$

vertical shrink by a scale factor of $\frac{2}{5}$

7. $g(x) = f\left(\frac{1}{5}x\right)$

horizontal stretch by a scale factor of 5

8. $g(x) = 7f(x)$

vertical stretch by a scale factor of 7

9. $g(x) = f(3x)$

horizontal compression by a scale factor of $\frac{1}{3}$

10. $g(x) = 2f(x-1) - 3$

vertical stretch by a scale factor of 2, right 1, down 3

11. $g(x) = f(2(x+1)) - 4$ → down 4

horizontal compression by a scale factor of $\frac{1}{2}$, left 1

$$12. g(x) = -f\left(\frac{1}{3}(x-5)\right) + 1$$

\nwarrow reflection over x-axis
 \swarrow horizontal stretch by scale factor 3
 \searrow right 5
 \nearrow up 1

$$13. g(x) = -\frac{1}{2}f(x+5)$$

\nwarrow reflection over x-axis
 \swarrow vertical shrink by scale factor $\frac{1}{2}$
 \searrow left 5

$$14. g(x) = 3f(-2(x+1)) - 5$$

\nwarrow vertical stretch by scale factor 3
 \swarrow horizontal compression by scale factor of 2
 \searrow left 1
 \nearrow reflection over y-axis
 \nearrow down 5

$$15. g(x) = -f(4(x+3)) + 1$$

\nwarrow reflection over x-axis
 \swarrow horizontal compression by a scale factor of $\frac{1}{4}$
 \searrow left 3
 \nearrow up 1

State the transformations that were applied to the parent function $f(x) = x^2$

$$16. f(x) = -2(3)^{x+1} - 4$$

\nwarrow reflection over x-axis
 \swarrow vertical stretch by a scale factor of 2
 \searrow left 1
 \nearrow down 4

$$17. f(x) = -\left(\frac{1}{4}(x-2)\right)^2 + 1$$

\nwarrow reflection over x-axis
 \swarrow horizontal stretch by a scale factor of 4
 \searrow right 2
 \nearrow up 1

$$18. g(x) = \frac{2}{3} \log_4\left(\frac{1}{2}(x+1)\right) - 2$$

\nwarrow vertical shrink by a scale factor of $\frac{2}{3}$
 \swarrow horizontal compression by a scale factor of $\frac{1}{2}$
 \searrow left 1
 \nearrow down 2

$$19. f(x) = -2(x-1)| + 4$$

\nwarrow reflection over y-axis
 \swarrow horizontal compression by a scale factor of $\frac{1}{2}$
 \searrow right 1
 \nearrow up 4

$$20. f(x) = -\sqrt{3(x-1)} + 6$$

\nwarrow reflection over x-axis
 \swarrow horizontal compression by a scale factor of $\frac{1}{3}$
 \searrow right 1
 \nearrow up 6

$$21. f(x) = -2(x-1)^3$$

\nwarrow reflection over x-axis
 \swarrow vertical stretch by a scale factor of 2
 \searrow right 1