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1) Stat, Edit
2) Stat, Calc, O: ExpReg

Date _____
Algebra I

Exponential Regression Equations

1. The accompanying table shows the number of bacteria present in a certain culture over a 5-hour period, where x is the time, in hours, and y is the number of bacteria.

Write an exponential regression equation for this set of data, rounding all values to *four decimal places*. Using this equation, determine the number of whole bacteria present after 6.5 hours.

x	y
0	1,000
1	1,049
2	1,100
3	1,157
4	1,212
5	1,271

ExpReg
 $y = a(b)^x$
 $y = 999.9725(1.0493)^x$
 $y = 999.9725(1.0493)^{6.5}$
 $y = 1367$

2. The accompanying table shows the amount of water vapor, y , that will saturate 1 cubic meter of air at different temperatures, x .

Write an exponential regression equation for this set of data, rounding all values to the *nearest thousandth*. Using this equation, predict the amount of water vapor that will saturate 1 cubic meter of air at a temperature of 50°C, and round your answer to the *nearest tenth of a gram*.

Amount of Water Vapor That Will Saturate
1 Cubic Meter of Air at Different Temperatures

Air Temperature (x) (°C)	Water Vapor (y) (g)
-20	1
-10	2
0	5
10	9
20	17
30	29
40	50

ExpReg
 $y = a(b)^x$
 $y = 4.194(1.068)^x$
 $y = 4.194(1.068)^{50}$
 $y = 112.5$

3. Jean invested \$380 in stocks. Over the next 5 years, the value of her investment grew, as shown in the accompanying table.

Write the exponential regression equation for this set of data, rounding all values to *two decimal places*. Using this equation, find the value of her stock, to the *nearest dollar*, 10 years after her initial purchase.

Years Since Investment (x)	Value of Stock, in Dollars (y)
0	380
1	395
2	411
3	427
4	445
5	462

ExpReg
 $y = a(b)^x$
 $y = 379.92(1.04)^x$
 $y = 379.92(1.04)^{10}$
 $y = 562$

4. The table below shows the number of new stores in a coffee shop chain that opened during the years 1986 through 1994.

Year	Number of New Stores
1986 <u>1</u>	14
1987 <u>2</u>	27
1988 <u>3</u>	48
1989 <u>4</u>	80
1990 <u>5</u>	110
1991 <u>6</u>	153
1992 <u>7</u>	261
1993 <u>8</u>	403
1994 <u>9</u>	681

ExpReg

$$y = a(b)^x$$

$$y = 10.596(1.586)^x$$

$$y = 10.596(1.586)^{16}$$

$$y = 16982$$

2001 16

Using $x = 1$ to represent the year 1986 and y to represent the number of new stores, write the exponential regression equation for these data. Round all values to the nearest thousandth.

Use your equation to determine the number of new stores in the year 2001 rounded to the nearest unit.

$$x = 16$$

5. A population of single-celled organisms was grown in a Petri dish over a period of 16 hours.

The number of organisms at a given time is recorded in the table below.

Determine the exponential regression equation model for these data, rounding all values to the nearest ten-thousandth.

Using this equation, predict the number of single-celled organisms, to the nearest whole number, at the end of the 18th hour.

Time, hrs

Number of Organisms

(x)

(y)

0

25

2

36

4

52

6

68

8

85

10

104

12

142

16

260

ExpReg

$$y = a(b)^x$$

$$y = 27.2025(1.1509)^x$$

$$y = 27.2025(1.1509)^{18}$$

$$y = 341$$

6. Using a microscope, a researcher observed and recorded the number of bacteria spores on a large sample of uniformly sized pieces of meat kept at room temperature. A summary of the data she recorded is shown in the table below.

Using these data, write an exponential regression equation, rounding all values to the nearest thousandth. The researcher knows that people are likely to suffer from food-borne illness if the number of spores exceeds 100. Using the exponential regression equation, determine the maximum amount of time, to the nearest quarter hour, that the meat can be kept at room temperature safely.

Hours (x)	Average Number of Spores (y)
0	4
0.5	10
1	15
2	60
3	260
4	1130
6	16,380

ExpReg

$$y = a(b)^x$$

$$y = 4.168(3.981)^x$$

$$100 = 4.168(3.981)^x$$

$$\frac{\log 23.99...}{\log 3.981} = \frac{\log 4.168(3.981)^x}{\log 3.981}$$

$$\log 23.99... = x \log 3.981$$

$$x = \frac{\log 23.99...}{\log 3.981}$$

$$x = 2.25 = X$$

7. A runner is using a nine-week training app to prepare for a "fun run." The table below represents the amount of the program completed, A , and the distance covered in a session, D , in miles.

Based on these data, write an exponential regression equation, rounded to the nearest thousandth, to model the distance the runner is able to complete in a session as she continues through the nine-week program. After how much of the program is completed will the runner complete 2.5 miles? Round your answer to the nearest hundredth.

A	$\frac{4}{9}$	$\frac{5}{9}$	$\frac{6}{9}$	$\frac{8}{9}$	1
D	2	2	2.25	3	3.25

ExpReg

$$y = a(b)^x$$

$$y = 1.223(2.652)^x$$

$$2.5 = 1.223(2.652)^x$$

$$\frac{\log 2.04...}{\log 2.652} = \frac{\log 1.223(2.652)^x}{\log 2.652}$$

$$\log 2.04... = x \log 2.652$$

$$x = \frac{\log 2.04...}{\log 2.652}$$

$$x = .73 = X$$

Variable Exponential Equations

1) Isolate
2) Take the log of both sides

Intersect
 y_1
 y_2

Amount completed
 L_1
miles
 L_2

8. The following table represents the amount of student loan debt Dr. Ross has x years after 2010.

Write an exponential regression equation to represent the amount of debt Ross will have left after x years. Round all coefficients to the nearest thousandth.

Assuming the pattern continues, in what year will Ross have \$10,000 left in debt?

0	120,000
1	112,541
3	88,897
4	76,441
6	53,289

ExpReg y

$$y = a(b)^x$$

$$y = 126565.191(.874)^x$$

$$10,000 = 126565.191(.874)^x$$

$$\log 126565.191 \quad \log .874^x$$

$$\log .079... = x \log .874$$

$$\frac{\log .079...}{\log .874} = \frac{x \log .874}{\log .874}$$

$$18.84 = x$$

$$\frac{2010}{+ 18}$$

$$\boxed{2028}$$

9. The table below shows the average yearly balance in a savings account where interest is compounded annually. No money is deposited or withdrawn after the initial amount is deposited.

Write an exponential regression equation to represent this situation. Round all coefficients to the nearest ten-thousandth. Use your equation to determine to the nearest tenth of a year, how long it will take for the balance to reach \$1,000,000.

Year	Balance, in Dollars
0	380.00
10	562.49
20	832.63
30	1232.49
40	1824.39
50	2700.54

ExpReg y

$$y = a(b)^x$$

$$y = 379.9996(1.0400)^x$$

$$1,000,000 = 379.9996(1.0400)^x$$

$$\log 379.9996 \quad \log 1.0400^x$$

$$\log 2631... = x \log 1.0400$$

$$\frac{\log 2631...}{\log 1.0400} = \frac{x \log 1.0400}{\log 1.0400}$$

$$200.8 = x$$