

Name Schlansky  
Mr. Schlansky

1) Stat, Edit  
2) Stat, Calc, 0: ExpReg

Date \_\_\_\_\_  
Algebra I

## Exponential Regression Equations

1. The accompanying table shows the number of bacteria present in a certain culture over a 5-hour period, where  $x$  is the time, in hours, and  $y$  is the number of bacteria.

$x$	$y$
0	1,000
1	1,049
2	1,100
3	1,157
4	1,212
5	1,271

ExpReg  
 $y = a(b)^x$   
 $y = 999.9725(1.0493)^x$   
 $y = 999.9725(1.0493)^{6.5}$   
 $y = 1367$

Write an exponential regression equation for this set of data, rounding all values to *four decimal places*. Using this equation, determine the number of whole bacteria present after 6.5 hours.

x

2. The accompanying table shows the amount of water vapor,  $y$ , that will saturate 1 cubic meter of air at different temperatures,  $x$ .

Amount of Water Vapor That Will Saturate 1 Cubic Meter of Air at Different Temperatures

Air Temperature ( $x$ ) (°C)	Water Vapor ( $y$ ) (g)
-20	1
-10	2
0	5
10	9
20	17
30	29
40	50

ExpReg  
 $y = a(b)^x$   
 $y = 4.194(1.068)^x$   
 $y = 4.194(1.068)^{50}$   
 $y = 112.5$

Write an exponential regression equation for this set of data, rounding all values to the *nearest thousandth*. Using this equation, predict the amount of water vapor that will saturate 1 cubic meter of air at a temperature of 50°C, and round your answer to the *nearest tenth of a gram*.

3. Jean invested \$380 in stocks. Over the next 5 years, the value of her investment grew, as shown in the accompanying table.

Years Since Investment ( $x$ )	Value of Stock, in Dollars ( $y$ )
0	380
1	395
2	411
3	427
4	445
5	462

Write the exponential regression equation for this set of data, rounding all values to *two decimal places*. Using this equation, find the value of her stock, to the *nearest dollar*, 10 years after her initial purchase.

x

ExpReg  
 $y = a(b)^x$   
 $y = 379.92(1.04)^x$   
 $y = 379.92(1.04)^{10}$   
 $y = 562$

4. The following table represents the amount of student loan debt Dr. Ross has  $x$  years after 2010. Write an exponential regression equation to represent the amount of debt Ross will have left after  $x$  years. Round all coefficients to the nearest thousandth.

Assuming the pattern continues, in what year will Ross have \$10,000 left in debt?

Years after 2010	Debt in Dollars
0	120,000
1	112,541
3	88,897
4	76,441
6	53,289

Exp Reg  $y$

$$y = a(b)^x$$

$$10,000 = 126565.191(0.874)^x$$

$$a = 126565.191$$

$$b = 0.874$$

$$y = 126565.191(0.874)^x$$

$\frac{10,000}{126565.191} = \frac{126565.191(0.874)^x}{126565.191}$   
 $\log 0.079... = \log 0.874^x$   
 $\log 0.079... = x \log 0.874$   
 $\frac{\log 0.079...}{\log 0.874} = \frac{x \log 0.874}{\log 0.874}$   
 $x = 18.81 \approx 19$

2010 + 19 = 2029

5. Consider the data in the table below.

State an exponential regression equation to model these data, rounding all values to the nearest thousandth. Use your equation to find  $x$  when  $y$  is 100, rounding to the nearest tenth.

x	1	2	3	4	5	6
y	3.9	6	11	18.1	28	40.3

Exp Reg  $y$

$$y = a(b)^x$$

$$100 = 2.459(1.616)^x$$

$$a = 2.459$$

$$b = 1.616$$

$$y = 2.459(1.616)^x$$

$\frac{100}{2.459} = \frac{2.459(1.616)^x}{2.459}$   
 $\log 40.256 = \log 1.616^x$   
 $\log 40.256 = x \log 1.616$   
 $\frac{\log 40.256}{\log 1.616} = \frac{x \log 1.616}{\log 1.616}$   
 $x = 7.7$

Exp Reg  $y$

$$y = a(b)^x$$

$$a = 2.458522514$$

$$b = 1.61590017$$

$$y = 2.459(1.616)^x$$

6. A runner is using a nine-week training app to prepare for a "fun run." The table below represents the amount of the program completed,  $A$ , and the distance covered in a session,  $D$ , in miles.

Based on these data, write an exponential regression equation, rounded to the nearest thousandth, to model the distance the runner is able to complete in a session as she continues through the nine-week program. After how much of the program is completed will the runner complete 2.5 miles? Round your answer to the nearest hundredth.

amount of program completed

A	$\frac{4}{9}$	$\frac{5}{9}$	$\frac{6}{9}$	$\frac{8}{9}$	1
D	2	2	2.25	3	3.25

distance covered

Exp Reg  $y$

$$y = a(b)^x$$

$$2.5 = 1.223(2.652)^A$$

$$a = 1.223$$

$$b = 2.652$$

$$y = 1.223(2.652)^A$$

$$D = 1.223(2.652)^A$$

$\frac{2.5}{1.223} = \frac{1.223(2.652)^A}{1.223}$   
 $2.04 = 2.652^A$   
 $\log 2.04 = \log 2.652^A$   
 $\log 2.04 = A \log 2.652$   
 $\frac{\log 2.04}{\log 2.652} = \frac{A \log 2.652}{\log 2.652}$   
 $A = 0.73$