

$$A = P(1 \pm r)^t$$

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Algebra II

## Finding Exponential Rate

1. A bank account opened up 3 years ago with an initial balance of \$12000 now has a balance of \$12824. Find the annual growth rate, to the nearest tenth of a percent.

$$\begin{aligned} A &= 12824 \\ P &= 12,000 \\ r &= r \\ t &= 3 \end{aligned}$$

$$\begin{aligned} 12824 &= 12,000(1+r)^3 \\ \frac{12824}{12,000} &= \frac{12,000}{12,000}(1+r)^3 \\ 3\sqrt{1.068} &= \sqrt[3]{(1+r)^3} \end{aligned}$$

$$\begin{aligned} 1.068 &= 1+r \\ -1 &= -1 \\ .068 &= r \\ 6.8\% &= r \end{aligned}$$

2. Jack bought a new car in 2010 for \$16100. In 2018, the car is now worth \$6125. What is the annual rate of decrease to the nearest percent?

$$\begin{aligned} A &= 6125 \\ P &= 16100 \\ r &= r \\ t &= 8 \end{aligned}$$

$$\begin{aligned} 6125 &= 16100(1-r)^8 \\ \frac{6125}{16100} &= \frac{16100}{16100}(1-r)^8 \\ \sqrt[8]{.38} &= \sqrt[8]{(1-r)^8} \\ .8862 &= 1-r \\ -1 &= -1 \end{aligned}$$

$$\begin{aligned} -.11379 &= -r \\ \frac{.11379}{1} &= \frac{r}{1} \\ .11379 &= r \\ 11\% &= r \end{aligned}$$

3. A collectible toy was bought 15 years ago for \$5 and is now worth \$42. Find the annual growth rate to the nearest tenth of a percent.

$$\begin{aligned} A &= 42 \\ P &= 5 \\ r &= r \\ t &= 15 \end{aligned}$$

$$\begin{aligned} 42 &= 5(1+r)^{15} \\ \frac{42}{5} &= \frac{5}{5}(1+r)^{15} \\ \sqrt[15]{8.4} &= \sqrt[15]{(1+r)^{15}} \\ 1.152 &= 1+r \\ -1 &= -1 \end{aligned}$$

$$\begin{aligned} 1.152 &= r \\ 15.2\% &= r \end{aligned}$$

4. A colony of 120 timberwolves increased to 245 over a 6 year span. Assuming exponential growth, what was the annual growth rate to the nearest percent?

$$\begin{aligned} A &= 245 \\ P &= 120 \\ r &= r \\ t &= 6 \end{aligned}$$

$$\begin{aligned} 245 &= 120(1+r)^6 \\ \frac{245}{120} &= \frac{120}{120}(1+r)^6 \\ \sqrt[6]{2.0416} &= \sqrt[6]{(1+r)^6} \\ 1.126 &= 1+r \\ -1 &= -1 \end{aligned}$$

$$\begin{aligned} 1.126 &= r \\ 12.6\% &= r \\ 13\% &= r \end{aligned}$$

5. The principal value of a loan is \$424,100. If there is \$110,000 remaining on the loan after 19 years, what was the annual rate of decrease to the nearest tenth of a percent?

$$\begin{array}{l}
 A = 110,000 \\
 P = 424,100 \\
 r = r \\
 t = 19
 \end{array}
 \qquad
 \begin{array}{l}
 110,000 = 424,100(1-r)^{19} \\
 \frac{110,000}{424,100} = \frac{424,100}{424,100}(1-r)^{19} \\
 \sqrt[19]{.259} = \sqrt[19]{(1-r)} \\
 .9314 = 1-r \\
 -1 \qquad -1
 \end{array}
 \qquad
 \begin{array}{l}
 -.06856 = -r \\
 \frac{-.06856}{-1} = \frac{-r}{-1} \\
 .06856 = r \\
 6.9\% = r
 \end{array}$$

6. An endangered species has dropped from 937 animals to 375 animals over the past 8 years. What is the annual rate of decrease rounded to the nearest percent?

$$\begin{array}{l}
 A = 375 \\
 P = 937 \\
 r = r \\
 t = 8
 \end{array}
 \qquad
 \begin{array}{l}
 375 = 937(1-r)^8 \\
 \frac{375}{937} = \frac{937}{937}(1-r)^8 \\
 \sqrt[8]{.4002} = \sqrt[8]{(1-r)} \\
 .8918 = 1-r \\
 -1 \qquad -1
 \end{array}
 \qquad
 \begin{array}{l}
 -.10816 = -r \\
 \frac{-.10816}{-1} = \frac{-r}{-1} \\
 .10816 = r \\
 11\% = r
 \end{array}$$

7. A house purchased 5 years ago for \$100,000 was just sold for \$135,000. Assuming exponential growth, approximate the annual growth rate, to the nearest percent.

$$\begin{array}{l}
 A = 135,000 \\
 P = 100,000 \\
 r = r \\
 t = 5
 \end{array}
 \qquad
 \begin{array}{l}
 135,000 = 100,000(1+r)^5 \\
 \frac{135,000}{100,000} = \frac{100,000}{100,000}(1+r)^5 \\
 \sqrt[5]{1.35} = \sqrt[5]{(1+r)} \\
 1.0618 = 1+r \\
 -1 \qquad -1
 \end{array}
 \qquad
 \begin{array}{l}
 .0618 = r \\
 \text{6\%} = r
 \end{array}$$

8. Over the past 4 years, the value of a stock increased from \$1200 to \$2300. What is the <sup>annual</sup> monthly growth rate, rounded to the nearest tenth of a percent?

$$\begin{array}{l}
 A = 2300 \\
 P = 1200 \\
 r = r \\
 t = 4
 \end{array}
 \qquad
 \begin{array}{l}
 2300 = 1200(1+r)^4 \\
 \frac{2300}{1200} = \frac{1200}{1200}(1+r)^4 \\
 \sqrt[4]{1.916} = \sqrt[4]{(1+r)} \\
 1.176 = 1+r \\
 -1 \qquad -1
 \end{array}
 \qquad
 \begin{array}{l}
 .176 = r \\
 17.7\%
 \end{array}$$