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Date \_\_\_\_\_  
Algebra II



## Finding Key Points

1. Given the function  $f(x) = x^3 + 3x^2 - x - 2$ , find the zeros and relative extrema to the *nearest tenth*.

Zeros  
-3.1  
-0.7  
0.9

Maximum  
(-2.2, 4.1)

Minimum  
(0.2, -2.1)

2. Given the function  $f(x) = -x^3 - 2x^2 + 2x + 3$ , find the zeros and relative extrema to the *nearest tenth*.

Zeros  
-2.3  
-1  
1.3

Maximum  
(0.4, 3.4)

Minimum  
(-1.7, -1.3)

3. Given the function  $f(x) = x^4 - 8x^2 + x + 8$ , find the zeros and relative extrema to the *nearest tenth*.

Zeros  
-2.7  
-1  
1.2  
2.5

Maximum  
(1, 8.0)

Minimum  
(-2.0, -10.0)  
(2.0, 6.0)

4. Given the function  $f(x) = -x^4 + 3x^2 - 1$ , find the zeros and relative extrema to the *nearest tenth*.

Zeros  
-1.6  
-0.6  
0.6  
1.6

Maximum  
(-1.2, 1.25)  
(1.2, 1.25)

Minimum  
(0, -1)

\*  $4.7817E-7 = 0$   
-00000047817

5. Given the function  $f(x) = 2x^3 - 11x^2 - 14x + 26$ , find the zeros and relative extrema to the nearest tenth

<u>Zeros</u>	<u>maximum</u>	<u>minimum</u>	* $y_{\min}: -80$ $y_{\max}: 80$
-1.9 1.1 6.3	(-.6, 30.0)	(4.2, -78.7)	

6. Given the function  $f(x) = -3x^3 - 20x^2 - 10x + 8$ , find the zeros and relative extrema to the nearest tenth.

<u>Zeros</u>	<u>maximum</u>	<u>minimum</u>	* $y_{\min}: -100$ $y_{\max}: 10$
-6.0 -1.0 .4	(-.3, 9.3)	(-4.2, -80.5)	

7. Given the function  $f(x) = -x^4 + 15x^2 - 7$ , find the zeros and relative extrema to the nearest tenth.

<u>Zeros</u>	<u>maximum</u>	<u>minimum</u>	* $y_{\min}: -30$ $y_{\max}: 80$ * $-8.206E-7 \approx 0$ $-0.000008206$
-3.8 -.7 .7 3.8	(-2.7, 49.3) (2.7, 49.3)	(0, -7)	

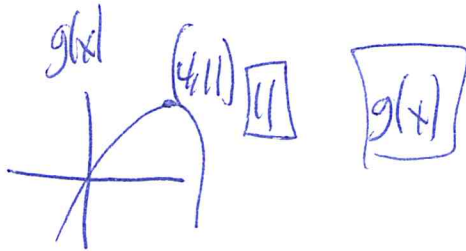
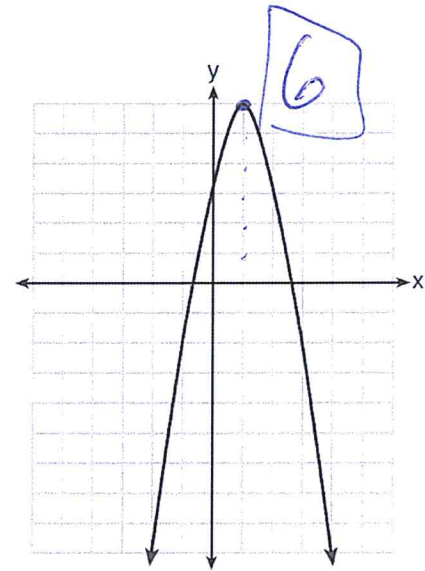
8. Given the function  $f(x) = x^3 + 8x^2 + 3x - 8$ , find the zeros and relative extrema to the nearest tenth

<u>Zeros</u>	<u>maximum</u>	<u>minimum</u>	* $y_{\max}: 80$
-7.5 -1.3 .8	(-5.1, 52.1)	(-.2, -8.3)	

9. Let  $f$  be the function represented by the graph below.

Let  $g$  be a function such that  $g(x) = -\frac{1}{2}x^2 + 4x + 3$ . *type into calc*

Determine which function has the larger maximum value.  
Justify your answer.



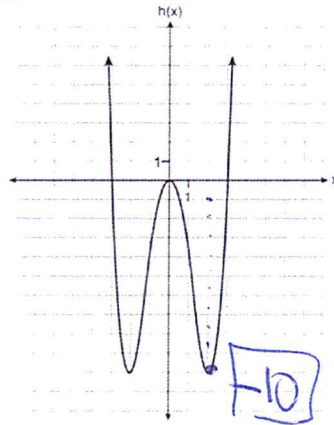
*g value*

10. Which graph has a smaller relative minimum?

$$g(x) = x^3 + 4x^2 - 2x - 10$$

*2<sup>nd</sup> Trace (minimum)  
(.23, -10.23)*

*-10.23*



*g(x) is smaller*

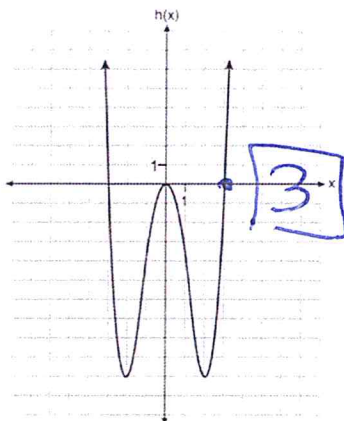
11. Which graph has the largest zero?

$$g(x) = x^3 + 4x^2 - 2x - 10$$

*2<sup>nd</sup> Trace (zero)*

*(.23, -10.23)*

*1.5*



*h(x)*

12. Which quadratic function has the largest maximum?

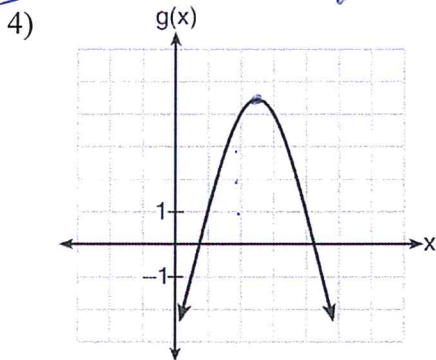
1)  $h(x) = (3-x)(2+x)$  2<sup>nd</sup> Trace: max 6.25

2)

x	f(x)
-1	-3
0	5
1	9
2	9
3	5
4	-3

≈ 9.5

3)  $k(x) = -5x^2 - 12x + 4$  2<sup>nd</sup> Trace: max 11.2



≈ 4.5

13. The graph representing a function is shown below.

Which function has a minimum that is less than the one shown in the graph?

2<sup>nd</sup> Trace  
min

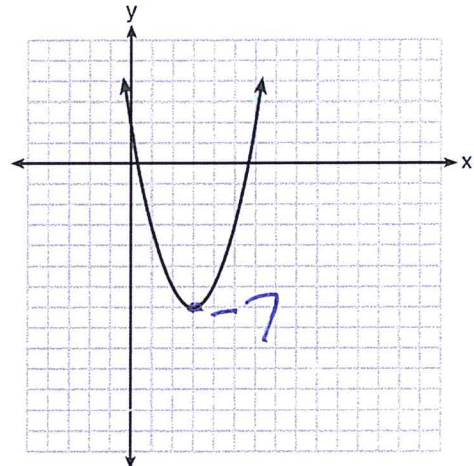
1)  $y = x^2 - 6x + 7$  -2

2)  $y = |x + 3| - 6$  -2

3)  $y = x^2 - 2x - 10$  -11

4)  $y = |x - 8| + 2$  2

-11 < -7



14. Which of the following functions has the greatest zero?

$f(x) = x^2 - 6x + 7$  4.4

$g(x) = x^2 - 2x - 10$  4.3

f(x)

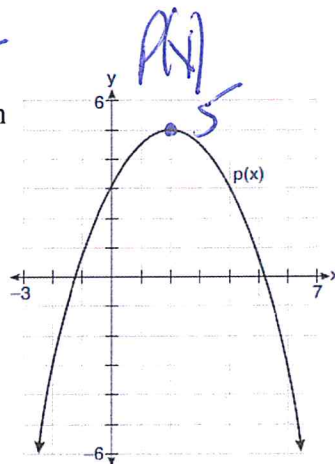
2<sup>nd</sup> Trace: zero

2<sup>nd</sup> Trace (min)  $-0.75, -5.25$

15. Consider  $f(x) = 4x^2 + 6x - 3$ , and  $p(x)$  defined by the graph below. The difference between the values of the maximum of  $p$  and minimum of  $f$  is subtraction

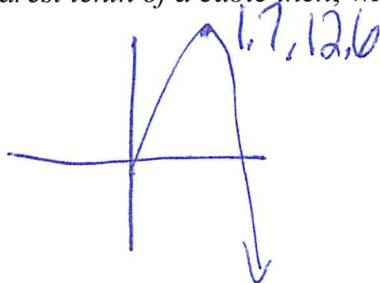
- 1) 0.25      3) 3.25  
 2) 1.25      4) 10.25

Maximum of  $p$       Minimum of  $f$   
5                      -5.25  
 $5 - (-5.25) = 10.25$



16. The function  $v(x) = x(3-x)(x+4)$  models the volume, in cubic inches, of a rectangular solid for  $0 \leq x \leq 3$ . To the nearest tenth of a cubic inch, what is the maximum volume of the rectangular solid?

$x$  min: 0  
 $x$  max: 3

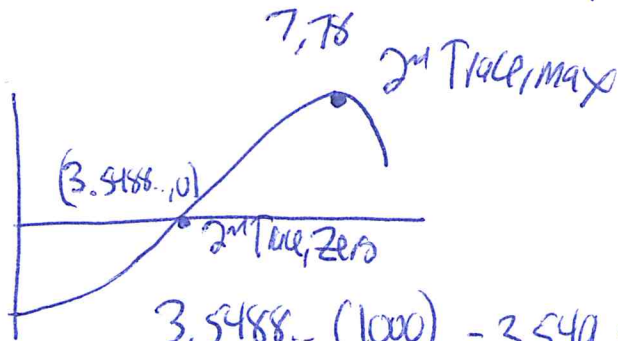


12.6

17. A manufacturer of sweatshirts finds that profits and costs fluctuate depending on the number of products created. Creating more products doesn't always increase profits because it requires additional costs, such as building a larger facility or hiring more workers. The manufacturer determines the profit,  $p(x)$ , in thousands of dollars, as a function of the number of sweatshirts sold,  $x$ , in thousands. This function,  $p$ , is given below. Over the interval  $0 \leq x \leq 9$ , state the coordinates of the maximum of  $p$  and round all values to the nearest integer. Explain what this point represents in terms of the number of sweatshirts sold and profit. Determine how many sweatshirts, to the nearest whole sweatshirt, the manufacturer would need to produce in order to first make a positive profit. Justify your answer.

$p(x) = -x^3 + 11x^2 - 7x - 69$

when 7,000 sweatshirts are sold, the maximum profit is \$78,000.



$3.5488 \cdot (1000) = 3549$  sweatshirts to first make a positive profit.