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Algebra II



Finding k in a Polynomial Equation

1. Consider the polynomial $p(x) = x^3 + kx^2 + x + 6$. Find a value of k so that $x+1$ is a factor of P .

$$0 = (-1)^3 + k(-1)^2 + (-1) + 6$$

$$0 = -1 + k(1) - 1 + 6$$

$$0 = -1 + k - 1 + 6$$

$$0 = k + 4$$

$$\underline{-4 = k}$$

-1 is a zero

$(-1, 0)$

2. Consider the polynomial $p(x) = x^3 + kx - 30$. Find a value of k so that $x+3$ is a factor of P .

$$0 = (-3)^3 + k(-3) - 30$$

$$0 = -27 - 3k - 30$$

$$0 = -3k - 57$$

$$+57 \quad +57$$

$$57 = -3k$$

$$\frac{57}{-3} = \frac{-3k}{-3}$$

$$\underline{-19 = k}$$

-3 is a zero

$(-3, 0)$

3. Given $p(x) = 6x^3 + 31x^2 + kx - 12$, and $x+4$ is a factor, find the value of k .

$$0 = 6(-4)^3 + 31(-4)^2 + k(-4) - 12$$

$$0 = -384 + 496 - 4k - 12$$

$$0 = -4k + 100$$

$$-100 \quad -100$$

$$\frac{-100}{-4} = \frac{-4k}{-4}$$

-4 is a zero

$(-4, 0)$

$$\underline{25 = k}$$

4. Given $z(x) = 6x^3 + bx^2 - 52x + 15$, and $x+5$ is a factor, find the value of b .

$$0 = 6(-5)^3 + b(-5)^2 - 52(-5) + 15$$

$$0 = -750 + 25b + 260 + 15$$

$$0 = 25b - 475$$

$$+475 \quad +475$$

$$475 = 25b$$

$$\frac{475}{25} = \frac{25b}{25}$$

$$\underline{19 = b}$$

-5 is a zero

$(-5, 0)$

5. Given $p(x) = x^3 + 5x^2 + kx - 24$, and $x+3$ is a factor, find the value of k .

$$\begin{aligned}
 0 &= (-3)^3 + 5(-3)^2 + k(-3) - 24 && -3 \text{ is a zero} \\
 0 &= -27 + 45 - 3k - 24 && (-3, 0) \\
 0 &= -3k - 6 \\
 +6 & && +6 \\
 \frac{6}{-3} &= \frac{-3k}{-3} && \Rightarrow k = 2
 \end{aligned}$$

6. If $x-1$ is a factor of $x^3 - kx^2 + 2x$, what is the value of k ?

$$\begin{aligned}
 1 & \text{ is a zero} && (1, 0) \\
 (1)^3 - k(1)^2 + 2(1) &= 0 \\
 1 - k + 2 &= 0 \\
 -k + 3 &= 0 \\
 +k & && +k \\
 \underline{3} &= k
 \end{aligned}$$

7. The polynomial function $g(x) = x^3 + ax^2 - 5x + 6$ has a factor of $(x-3)$. Determine the value of a .

$$\begin{aligned}
 3 & \text{ is a zero} && (3, 0) \\
 0 &= (3)^3 + a(3)^2 - 5(3) + 6 \\
 0 &= 27 + 9a - 15 + 6 && \Rightarrow -2 = 9a \\
 0 &= 9a + 18 \\
 -18 & && -18 \\
 \frac{-18}{9} &= \frac{9a}{9}
 \end{aligned}$$

8. Consider the polynomial $p(x) = x^3 + kx + 2$. Find a value of k so that $x-2$ is a factor of P .

$$\begin{aligned}
 2 & \text{ is a zero} && (2, 0) \\
 0 &= (2)^3 + k(2) + 2 \\
 0 &= 8 + 2k + 2 \\
 0 &= 2k + 10 \\
 -10 & && -10 \\
 \frac{-10}{2} &= \frac{2k}{2} \\
 \underline{-5} &= k
 \end{aligned}$$