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Date _____
Pre Calculus

Testing Inverse with Composition

Determine whether the following are inverses of each other

1. $f(x) = 3x - 6$, $g(x) = \frac{1}{3}x + 2$

2. $f(x) = 2x + 8$, $g(x) = \frac{1}{2}x - 2$

$$\begin{aligned} f\left(\frac{1}{3}x + 2\right) &= 3\left(\frac{1}{3}x + 2\right) - 6 \\ &= x + 6 - 6 \\ &= x \end{aligned}$$

$$\begin{aligned} f\left(\frac{1}{2}x - 2\right) &= 2\left(\frac{1}{2}x - 2\right) + 8 \\ &= x - 4 + 8 \\ &= x + 4 \end{aligned}$$

Yes, they are inverses of each other because $f(g(x)) = x$

No, they are not inverses of each other because $f(g(x)) \neq x$

3. $f(x) = 4x - 1$, $g(x) = \frac{1}{4}x + 1$

4. $f(x) = \frac{3}{2}x - 6$, $g(x) = \frac{2}{3}x + 4$

$$\begin{aligned} f\left(\frac{1}{4}x + 1\right) &= 4\left(\frac{1}{4}x + 1\right) - 1 \\ &= x + 4 - 1 \\ &= x + 3 \end{aligned}$$

$$\begin{aligned} f\left(\frac{2}{3}x + 4\right) &= \frac{3}{2}\left(\frac{2}{3}x + 4\right) - 6 \\ &= x + 6 - 6 \\ &= x \end{aligned}$$

No, they are not inverses of each other because $f(g(x)) \neq x$

Yes, they are inverses of each other because $f(g(x)) = x$

$$5. f(x) = x^2 + 3, g(x) = \sqrt{x-3}$$

$$\begin{aligned} f(\sqrt{x-3}) &= (\sqrt{x-3})^2 + 3 \\ &= x-3+3 \\ &= x \end{aligned}$$

Yes, they are inverses of each other because $f(g(x)) = x$

$$6. f(x) = x^3 - 1, g(x) = \sqrt[3]{x+1}$$

$$\begin{aligned} f(\sqrt[3]{x+1}) &= (\sqrt[3]{x+1})^3 - 1 \\ &= x+1-1 \\ &= x \end{aligned}$$

Yes, they are inverses of each other because $f(g(x)) = x$

$$7. f(x) = x^2 - 6, g(x) = \sqrt{x-6}$$

$$\begin{aligned} f(\sqrt{x-6}) &= (\sqrt{x-6})^2 - 6 \\ &= x-6-6 \\ &= x-12 \end{aligned}$$

No, they are not inverses of each other because $f(g(x)) \neq x$

$$8. f(x) = 2x^3 + 1, g(x) = \sqrt[3]{\frac{x-1}{2}}$$

$$\begin{aligned} f\left(\sqrt[3]{\frac{x-1}{2}}\right) &= 2\left(\sqrt[3]{\frac{x-1}{2}}\right)^3 + 1 \\ &= 2\left(\frac{x-1}{2}\right) + 1 \\ &= x-1+1 \\ &= x \end{aligned}$$

Yes, they are inverses of each other because $f(g(x)) = x$