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Date \_\_\_\_\_  
Pre Calculus

## Unit 3 Quadratics Review Sheet

Solve the following quadratic equations for all values of  $x$  in simplest radical form or simplest  $a+bi$  form if necessary.

1.  $5x^2 + 60 = 0$

no  $x$  term  
isolate / square  
root

$$\begin{aligned} -60 & -60 \\ 5x^2 & = -60 \\ \frac{5x^2}{5} & = \frac{-60}{5} \\ x^2 & = -12 \\ \sqrt{x^2} & = \sqrt{-12} \\ x & = \pm 2i\sqrt{3} \end{aligned}$$

2.  $-3x^2 - 50 = 130$

$$\begin{aligned} +50 & +50 \\ -3x^2 & = 180 \\ \frac{-3x^2}{-3} & = \frac{180}{-3} \\ x^2 & = -60 \\ \sqrt{x^2} & = \sqrt{-60} \\ x & = \pm i\sqrt{60} \\ & = \pm 2i\sqrt{15} \end{aligned}$$

3.  $a^2 - 8a = 20$

$$\begin{aligned} -20 & -20 \\ a^2 - 8a - 20 & = 0 \\ (a-10)(a+2) & = 0 \\ a=10 & \quad a=-2 \end{aligned}$$

4.  $2x^2 + 3x = 5$

$$\begin{aligned} -5 & -5 \\ 2x^2 + 3x - 5 & = 0 \\ (2x^2 + 5x) - (2x - 5) & \\ \frac{2x^2 + 5x}{x} - \frac{2x - 5}{-1} & \\ x(2x+5) - 1(2x-5) & \\ (x-1)(2x+5) & = 0 \\ x-1 & = 0 \quad 2x+5=0 \\ x=1 & \quad -5-5 \\ & \quad \frac{2x}{2} = \frac{-5}{2} \\ & \quad x = \frac{-5}{2} \end{aligned}$$

Solve the following using *both* the quadratic formula and completing the square methods

8.  $x^2 - 6x + 4 = 0$

Completing the square

$$\begin{aligned} x^2 - 6x + 4 & = 0 & \left(\frac{-6}{2}\right)^2 = 9 \\ x^2 - 6x & = -4 \\ x^2 - 6x + 9 & = -4 + 9 \\ \sqrt{x-3}^2 & = \sqrt{5} \\ x-3 & = \pm\sqrt{5} \\ +3 & +3 \\ x & = 3 \pm \sqrt{5} \end{aligned}$$

quadratic formula

$$\begin{aligned} x^2 - 6x + 4 & = 0 & a=1 \\ & & b=-6 \\ & & c=4 \\ x & = \frac{6 \pm \sqrt{(-6)^2 - 4(1)(4)}}{2(1)} \\ & & \sqrt{20} \\ & & \sqrt{4} \sqrt{5} \\ & & 2\sqrt{5} \\ x & = \frac{6 \pm 2\sqrt{5}}{2} \\ x & = 3 \pm \sqrt{5} \end{aligned}$$

8.  $4x^2 + 12x = 7$

Completing the square

$$\begin{aligned} 4x^2 + 12x & = 7 \\ \frac{4x^2 + 12x}{4} & = \frac{7}{4} \\ x^2 + 3x + \frac{9}{4} & = \frac{7}{4} + \frac{9}{4} \\ \sqrt{x + \frac{3}{2}}^2 & = \sqrt{4} \\ x + \frac{3}{2} & = \pm 2 \\ -\frac{3}{2} & -\frac{3}{2} \\ x & = -\frac{3}{2} \pm 2 \\ x & = -\frac{3}{2} + 2 = \frac{1}{2} \\ x & = -\frac{3}{2} - 2 = -\frac{7}{2} \end{aligned}$$

quadratic formula

$$\begin{aligned} 4x^2 + 12x & = 7 \\ -7 & -7 \\ 4x^2 + 12x - 7 & = 0 \\ a=4 & \quad b=12 & \quad c=-7 \\ x & = \frac{-12 \pm \sqrt{(12)^2 - 4(4)(-7)}}{2(4)} \\ & & \sqrt{256} \\ x & = \frac{-12 \pm 16}{8} \\ x & = \frac{-12+16}{8} = \frac{1}{2} \\ x & = \frac{-12-16}{8} = -\frac{7}{2} \end{aligned}$$

Solve the following polynomial equations for all values of  $x$  in simplest radical form or  $a+bi$  form if necessary

9.  $x^4 - 4x^2 - 32 = 0$

$$(x^2 - 8)(x^2 + 4) = 0$$

$$\begin{array}{l|l} x^2 - 8 = 0 & x^2 + 4 = 0 \\ +8 & +4 \\ +8 & -4 \\ \hline \sqrt{x^2} = \sqrt{8} & \sqrt{x^2} = \sqrt{-4} \\ x = \pm\sqrt{8} & x = \pm 2i \end{array}$$

10.  $\frac{x^3 - 3x^2}{x^2} - \frac{-5x + 15}{-5} = 0$

$$x^2(x-3) - 5(x-3) = 0$$

$$(x^2 - 5)(x-3) = 0$$

$$\begin{array}{l|l} x^2 - 5 = 0 & x - 3 = 0 \\ +5 & +3 \\ +5 & +3 \\ \hline \sqrt{x^2} = \sqrt{5} & x = 3 \\ x = \pm\sqrt{5} & \end{array}$$

Solve the following inequalities and graph on a number line

11.  $x^2 \leq 4x + 12$

*convergent*

$$-4x - 12 \leq -4x - 12$$

$$x^2 - 4x - 12 = 0$$

$$(x-6)(x+2) = 0$$

$$x=6 \quad x=-2$$

12.  $3x^2 + 2x \leq 8$

*convergent*

$$-8 \leq -8$$

$$3x^2 + 2x - 8 = 0$$

$$(3x^2 + 6x - 4x - 8) = 0$$

$$3x(x+2) - 4(x+2) = 0$$

$$(3x-4)(x+2) = 0$$

$$3x-4=0 \quad x+2 \neq 0$$

$$\frac{3x}{3} = \frac{4}{3} \quad -2 \neq -2$$

$$x = \frac{4}{3} \quad x = -2$$

13.  $x^4 - 20x^2 + 64 < 64$

*not not*

$$-4 < x < 2 \text{ or } 2 < x < 4$$

$$(-4, 2) \cup (2, 4)$$

$$x^4 - 20x^2 + 64 = 0$$

$$(x^2 - 16)(x^2 - 4) = 0$$

$$(x+4)(x-4)(x+2)(x-2) = 0$$

$$x = -4 \quad x = 4 \quad x = -2 \quad x = 2$$

-5: (-)(-)(-)(-) < 0 ✓  
 -3: (+)(-)(-)(-) < 0 ✓  
 3: (+)(-)(+)(+) < 0 ✓

14.  $x^3 + 6x^2 - 25x + 150 \leq 150$

*not not*

$$-150 \leq -150$$

$$(x^3 + 6x^2 - 25x + 150) = 0$$

$$x^2(x+6) - 25(x+6) = 0$$

$$(x^2 - 25)(x+6) = 0$$

$$(x+5)(x-5)(x+6) = 0$$

$$x = -5 \quad x = 5 \quad x = -6$$

-7: (-)(-)(-) <= 0 ✓  
 0: (+)(-)(+) <= 0 ✓

15. The nature of the roots of  $-2x^2 + x = 6$  are:

- 1) real, rational, and equal
- 2) real, rational, and unequal
- 3) real, irrational, and unequal
- 4) imaginary

$$-2x^2 + x - 6 = 0$$

$$b-b$$

$$\pm \sqrt{b^2 - 4ac}$$

$$\pm \sqrt{(1)^2 - 4(-2)(-6)}$$

$$\pm \sqrt{-47}$$

16. The nature of the roots of  $2x^2 = 3x + 1$  are:

- 1) real, rational, and equal
- 2) real, rational, and unequal
- 3) real, irrational, and unequal
- 4) imaginary

$$2x^2 - 3x - 1 = 0$$

$$3x-1 \quad -3x-1$$

$$\pm \sqrt{b^2 - 4ac}$$

$$\pm \sqrt{(-3)^2 - 4(2)(-1)}$$

$$\pm \sqrt{17}$$

17. For what value of k are the roots of  $-2x^2 + kx - 6 = 0$  imaginary?

- 1) 7
- 2) -7
- 3) 3.5
- 4) 9

$$b^2 - 4ac < 0$$

$$k^2 - 4(-2)(-6) < 0$$

convergent

$$\sqrt{28} \pm \sqrt{8}$$

$$k^2 - 48 < 0$$

$$+48 \quad +48$$

$$k = \pm 6.9$$



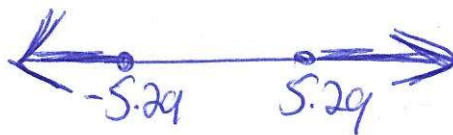
18. The roots of  $x^2 + kx + 7 = 0$  are real when k is equal to:

- 1) 1
- 2) -4
- 3) 10
- 4) -5

$$b^2 - 4ac \geq 0$$

$$k^2 - 4(1)(7) \geq 0$$

divergent



$$k^2 - 28 \geq 0$$

$$+28 \quad +28$$

$$\sqrt{k^2} \geq \sqrt{28}$$

$$k = \pm 5.29$$

$$x^2 - \text{sum}x + \text{product} = 0$$

$$\text{sum} = -\frac{b}{a}$$

$$\text{product} = \frac{c}{a}$$

Find the sum and product of the roots of the following equations:

19.  $x^2 - 7x = 5$

$$\begin{array}{l} \cancel{x^2 - 7x} \\ -5 - 5 \\ x^2 - 7x - 5 = 0 \end{array} \quad \begin{array}{l} \text{sum} = \frac{7}{1} = 7 \\ \text{product} = \frac{-5}{1} = -5 \end{array}$$

20.  $5x^2 + 3x = 4$

$$\begin{array}{l} -4 - 4 \\ 5x^2 + 3x - 4 = 0 \end{array} \quad \begin{array}{l} \text{sum} = -\frac{3}{5} \\ \text{product} = -\frac{4}{5} \end{array}$$

write the equation with the following roots:

21.  $x = -4 \pm \sqrt{2}$

$$\begin{array}{l} \text{sum} = -4 + \sqrt{2} + -4 - \sqrt{2} = -8 \\ \text{product} = (-4 + \sqrt{2})(-4 - \sqrt{2}) = 16 - 2 = 14 \end{array}$$

$$x^2 + 8x + 14 = 0$$

22.  $x = 2 \pm 4i$

$$\begin{array}{l} \text{sum} = 2 + 4i + 2 - 4i = 4 \\ \text{product} = (2 + 4i)(2 - 4i) = 4 - 16i^2 \\ 4 + 16 = 20 \end{array}$$

$$x^2 - 4x + 20 = 0$$

23. One root of  $x^2 + kx + 30 = 0$  is -6. Find the other root.

$$\text{product} = \frac{c}{a}$$

$$\text{product} = \frac{30}{1} = 30$$

$$r_1 \cdot r_2 = 30$$

$$\frac{-b}{-b} \cdot r_2 = 30$$

$$r_2 = -5$$

$$-5$$

$$\text{sum} = -b + -5 = -11 = -\frac{b}{a}$$

$$b = 11$$

$$k = 11$$

24. One root of  $x^2 - 7x + k = 0$  is 9. Find the other root.

$$\text{sum} = -\frac{b}{a}$$

$$\text{sum} = \frac{7}{1} = 7$$

$$\text{product} = 2 \cdot 9 = \frac{18}{1} = \frac{c}{a}$$

$$r_1 + r_2 = 9$$

$$\begin{array}{l} 7 + r_2 = 9 \\ -7 \quad -7 \end{array}$$

$$r_2 = 2$$

$$c = 18$$

$$k = 18$$