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Date _____
Pre Calculus

Radicals/Complex Numbers Review Sheet

For #1-8, express in simplest radical form

1. $-2\sqrt{8xy^3} \cdot 4\sqrt{6x^4y^2}$ *multiply/divide first*

$$-8\sqrt{48x^5y^5}$$

$$-8\sqrt{16x^4y^4} \sqrt{3xy}$$

$$-8(4x^2y^2)\sqrt{3xy}$$

$$-32x^2y^2\sqrt{3xy}$$

2. $2y^2\sqrt[3]{25y^6} \cdot xy^3\sqrt[3]{10x^5y^3}$

$$2xy^3 \sqrt[3]{250x^5y^9}$$

$$2xy^3 \sqrt[3]{125x^3y^9} \sqrt[3]{2x^2}$$

$$2xy^3(5xy^3) \sqrt[3]{2x^2}$$

$$10x^2y^6 \sqrt[3]{2x^2}$$

3. $\frac{10\sqrt{250x^4y^5z^2}}{2\sqrt{5xyz}}$

$$5\sqrt{50x^3y^4z}$$

$$5\sqrt{25x^2y^4} \sqrt{2xz}$$

$$5(5xy^2)\sqrt{2xz}$$

$$25xy^2\sqrt{2xz}$$

4. $\frac{20xy^4\sqrt[3]{48x^8y^{12}}}{4x^3\sqrt[3]{3x^2y^3}}$

$$5y^4\sqrt[3]{16x^6y^9}$$

$$5y^4 \sqrt[3]{8x^6y^9} \sqrt[3]{2}$$

$$5y^4(2x^2y^3) \sqrt[3]{2}$$

$$10x^2y^7 \sqrt[3]{2}$$

5. $\sqrt{200k} - 2\sqrt{18k}$

$$\sqrt{100} \sqrt{2k} - 2(3)\sqrt{2k}$$

$$10\sqrt{2k} - 6\sqrt{2k}$$

$$4\sqrt{2k}$$

6. $5\sqrt[3]{16x} + 2\sqrt[3]{250x}$

$$5\sqrt[3]{8} \sqrt[3]{2x} + 2\sqrt[3]{125} \sqrt[3]{2x}$$

$$5(2)\sqrt[3]{2x} + 2(5)\sqrt[3]{2x}$$

$$10\sqrt[3]{2x} + 10\sqrt[3]{2x}$$

$$20\sqrt[3]{2x}$$

$$7. \frac{10(6+\sqrt{3})}{6-\sqrt{3}(6+\sqrt{3})}$$

$$\frac{10(6+\sqrt{3})}{36-3}$$

$$\frac{60+10\sqrt{3}}{33}$$

$$8. \frac{-4(2-\sqrt{10})}{2+\sqrt{10}(2-\sqrt{10})}$$

$$\frac{-8+4\sqrt{10}}{2-10}$$

$$\frac{-4+4\sqrt{10}}{-8+4\sqrt{10}}$$

$$\frac{2-\sqrt{10}}{2}$$

For #9-10, solve for x

9. $x = 1 + \sqrt{x+5}$

$$\overset{-1}{(x-1)}^2 = \overset{-1}{(x+5)}^2$$

$$(x-1)(x-1) = x+5$$

$$x^2 - 1x - 1x + 1 = x + 5$$

$$x^2 - 2x + 1 = x + 5$$

$$-x - 5 \quad -x - 5$$

$$x^2 - 3x - 4 = 0$$

$$(x-4)(x+1) = 0$$

$$(x=4) \quad x=+1$$

reject

10. $3 = -x + \sqrt{x+5}$

$$\overset{+x}{(x+3)}^2 = \overset{+x}{(x+5)}^2$$

$$(x+3)(x+3) = x+5$$

$$x^2 + 3x + 3x + 9 = x + 5$$

$$x^2 + 6x + 9 = x + 5$$

$$-x - 5 \quad -x - 5$$

$$x^2 + 5x + 4 = 0$$

$$(x+4)(x+1) = 0$$

$$x=-4 \quad x=-1$$

reject

$$\begin{array}{r} 1 \\ i \\ -1 \\ -i \end{array} \begin{array}{r} .0 \\ .25 \\ .50 \\ .75 \end{array}$$

For #11-14, express in simplest $a + bi$ form

11. $5i^3(6i^7 - 3i^{17})$

$$30i^{10} - 15i^{20}$$

$$\frac{20}{4} = 5.0$$

(11)

$$30(-1) - 15(1)$$

$$-30 - 15$$

$$-45 + 0i$$

$$\frac{10}{4}$$

$$2.5$$

(-1)

12. $-2i^9(3i^3 + 4i^{12})$

$$-6i^{12} - 8i^{21}$$

$$-6(1) - 8(i)$$

$$-6 - 8i$$

$$\frac{12}{4} = 3.0 \quad (1)$$

$$\frac{21}{4} = 5.25 \quad (i)$$

13. $\frac{(7-2i)(5+i)}{(5-i)(5+i)}$

$$\frac{35+7i-10i-2i^2}{25-i^2}$$

$$\frac{35-3i-2(-1)}{25-(-1)}$$

$$\frac{35-3i+2}{25+1}$$

$$\frac{37-3i}{26}$$

$$\frac{37}{26} - \frac{3}{26}i$$

14. $\frac{(6+2i)(-2+7i)}{(-2-7i)(-2+7i)}$

$$\frac{-12+42i-4i+14i^2}{4-49i^2}$$

$$\frac{-12+38i+14(-1)}{4-49(-1)}$$

$$\frac{-12+38i-14}{4+49}$$

$$\frac{-26+38i}{53}$$

$$-\frac{26}{53} + \frac{38}{53}i$$

For #15-16, graph each complex number, find an magnitude of the resultant.

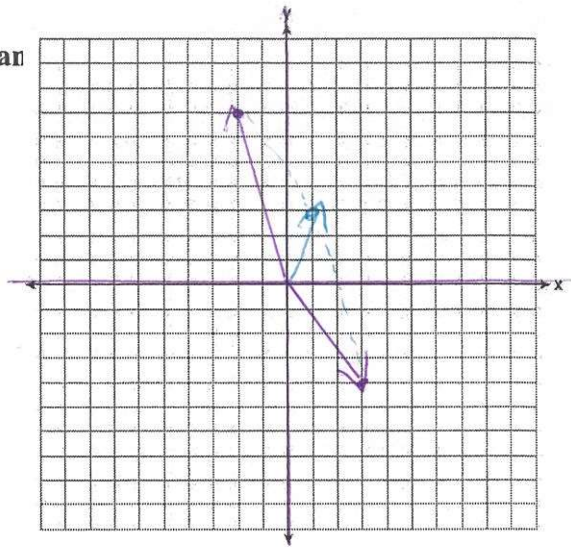
15. $(-2 + \sqrt{-49})$ and $(3 - \sqrt{-16})$

$-2+7i$ $3-4i$

$(-2, 7)$ $(3, -4)$

$-2+7i + 3-4i$ resultant
 $1+3i$

$\sqrt{1^2+3^2}$
 $\sqrt{1+9} = \sqrt{10}$ magnitude of resultant



16. $(7 - 4i)$ and $(-5 + 7i)$

$(7, -4)$ $(-5, 7)$

$7-4i + -5+7i$ resultant
 $2+3i$

$\sqrt{2^2+3^2}$
 $\sqrt{4+9} = \sqrt{13}$ magnitude of resultant

