

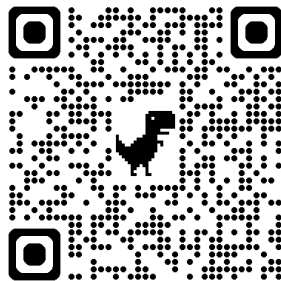
Name:

Common Core Geometry

Unit 1

Triangles and Parallel Lines Cut By a Transversal

Mr. Schlansky



Lesson 1: I can identify sides by stating their endpoints. I can identify angles by identifying the vertex (middle letter) and which directions is opens.

To name a line segment, state the two endpoints and put a line segment above them. Segments are always named with two letters.

To name an angle, the middle letter is the vertex. The vertex is where the angles come together. The two outside letters are where the angle opens up from the vertex. Angles are correctly named using 3 letters but are at times named using 1 letter.

Lesson 2: I can classify triangles by their angles and congruence using the given definitions.

Scalene triangles have 0 congruent sides/angles	Acute triangles have 3 acute angles
Isosceles triangles have 2 congruent sides/angles	Obtuse triangles have 1 obtuse angle
Equilateral triangles have 3 congruent sides/angles	Right triangles have 1 right angle

The angles of a triangle add to equal 180.

When given two angles of a triangle, add them up and subtract from 180 to find the third angle.

Lesson 3: I can classify triangles by using algebra and the given definitions.

- 1) Add up the three angles of a triangle to equal 180
- 2) Solve the equation
- 3) Substitute x into each expression to find the three angles
- 4) Classify the triangle using the definitions from Lesson 2.

Lesson 4: I can use “exterior angle theorem” by adding the sum of the two non-adjacent interior angles to equal the exterior angle.

The sum of the two non-adjacent interior angles is equal to the exterior angle.

Lesson 5: I can determine the largest side of a triangle by understanding that the largest side is opposite the largest angle.

- 1) Find the three angles of the triangle (add up and subtract from 180)
- 2) The largest side is opposite the largest angle, the middle side is opposite the middle angle, and the smallest side is opposite the smallest angle

Lesson 6: I can determine whether or not three numbers can be the sides of a triangle and find the range of possible values of the third side of the triangle using the triangle inequality theorem.

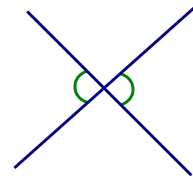
Triangle Inequality Theorem: The two smallest sides of a triangle must add up to be greater than the third side.

To determine the range of possible sides for the third side:

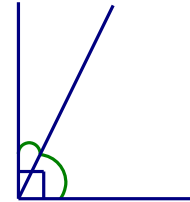
- 1) Add the two sides
- 2) Subtract the two sides
- 3) $\text{difference} < \text{third side} < \text{sum}$

Lesson 7: I can identify linear pairs and classify angle pairs as vertical, supplementary, and vertical.

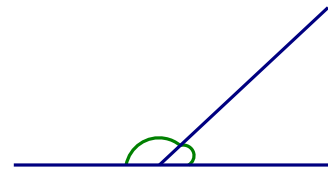
Vertical angles are congruent



Complementary angles add to 90



Supplementary angles add to 180
Linear pairs are adjacent supplementary angles

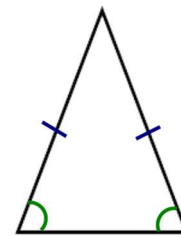


Lesson 8: I can find an angle of a triangle using the theorem “congruent angles are opposite congruent sides.”

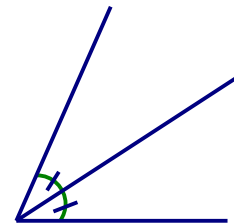
I can find an angle using the definition “an angle bisector cuts an angle into two congruent angles”

I can find an angle of a triangle using the definition “the angles of an equilateral triangle are 60, 60, 60.”

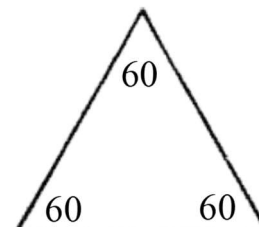
Isosceles Triangle Theorem: In a triangle, congruent angles are opposite congruent sides.



An angle bisector cuts an angle into two congruent angles.



An equilateral triangle has angles 60, 60, 60.



Lesson 9: I can find missing angles of triangles by looking for linear pairs and angles of a triangle, using isosceles triangle theorem, and applying the definitions of angle bisector and equilateral triangle.

Complex Triangle Problems:

- 1) The three angles of a triangle add to equal 180° . **Look for triangles.**
- 2) Linear pairs add to 180° . **Look for linear pairs.**
- 3) Isosceles triangle has congruent angles opposite congruent sides (given congruent sides).
- 4) Equilateral triangle has angles 60, 60, 60 (given equilateral triangle).
- 5) An angle bisector cuts an angle into two congruent halves (given bisected angles).

Lesson 10: I can find angles formed given parallel lines by extending the transversal and making all of the same angles congruent and different angles supplementary.

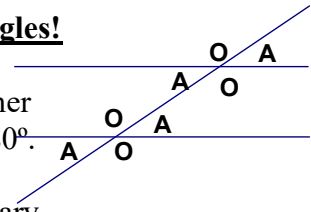
Extend parallel lines and follow the transversal!!!!!! Fill in all eight angles!

If lines are parallel:

- If the angles are the same (both acute or obtuse), set them equal to each other
- If the angles are different (one acute and one obtuse), add them to equal 180° .

If lines are *not* parallel:

- The same angles are *not* congruent and different angle are *not* supplementary



Lesson 11: I can incorporate parallel lines into complex triangle problems by following the transversal.

Complex Triangle Problems:

- 1) The three angles of a triangle add to equal 180° . Look for triangles.
- 2) Linear pairs add to 180° . Look for linear pairs.
- 3) Isosceles triangle has congruent angles opposite congruent sides (given congruent sides).
- 4) Equilateral triangle has angles 60, 60, 60 (given equilateral triangle).
- 5) An angle bisector cuts an angle into two congruent halves (given bisected angles).
- 6) Use parallel lines cut by a transversal (extend and follow the transversal, fill in 8 angles.)

Lesson 12: I can find missing angles when parallel lines are cut by a transversal by following the transversal and understanding that the same angles are congruent and the different angles are supplementary.

When given parallel lines cut by a transversal and algebraic expressions:

- If the angles are the same (both acute or both obtuse): set them equal to each other.
- If the angles are different (one acute and one obtuse): add them to equal 180.

Lesson 13: I can find the lengths of segments when medians intersect using the ratio 1:2.

When given intersecting medians (centroid), the medians are cut in a ratio of 1:2.

- If given the small piece, multiply by 2 for the large piece
- If given the large piece, divide by 2 for the small piece
- If given the whole median, divide by 3 for the small piece, multiply that by 2 for the small piece

Name _____
Mr. Schlansky

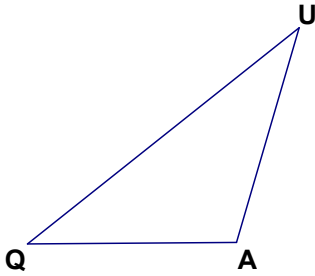
Date _____
Geometry



Naming Sides and Angles of Triangles

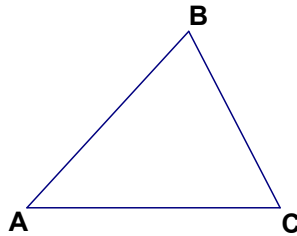
Label the appropriate sides and angles of each triangle

1.



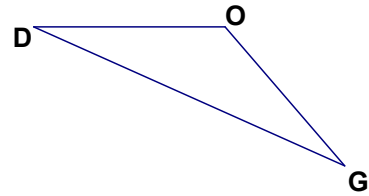
Label $\angle QAZ$ with a 1
Label $\angle AUQ$ with a 2
Label $\angle UQA$ with a 3
Label \overline{QU} with an X
Label \overline{AU} with a Y
Label \overline{AQ} with a Z

2.



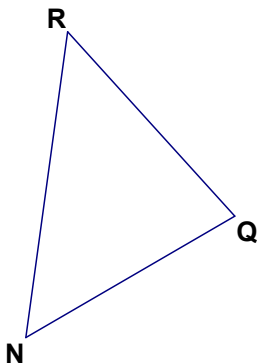
Label $\angle BAC$ with a 1
Label $\angle CBA$ with a 2
Label $\angle ACB$ with a 3
Label \overline{CB} with an X
Label \overline{AC} with a Y
Label \overline{AB} with a Z

3.



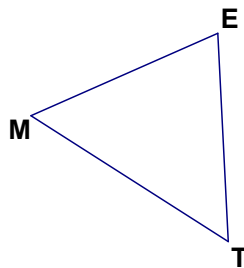
Label $\angle GDO$ with a 1
Label $\angle OGD$ with a 2
Label $\angle DOG$ with a 3
Label \overline{GD} with an X
Label \overline{OG} with a Y
Label \overline{OD} with a Z

4.



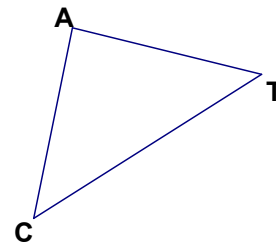
Label $\angle QRN$ with a 1
Label $\angle RNQ$ with a 2
Label $\angle RQN$ with a 3
Label \overline{NQ} with an X
Label \overline{RQ} with a Y
Label \overline{RN} with a Z

5.



Label $\angle MET$ with a 1
Label $\angle TME$ with a 2
Label $\angle ETM$ with a 3
Label \overline{MT} with an X
Label \overline{ET} with a Y
Label \overline{EM} with a Z

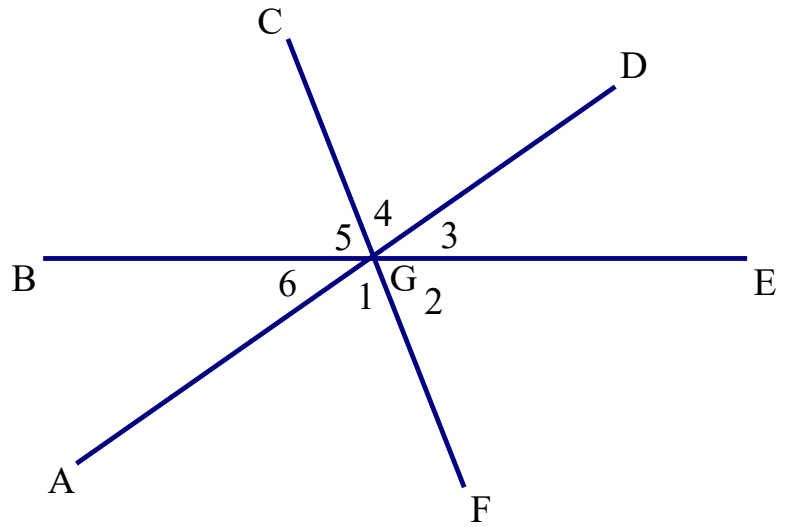
6.



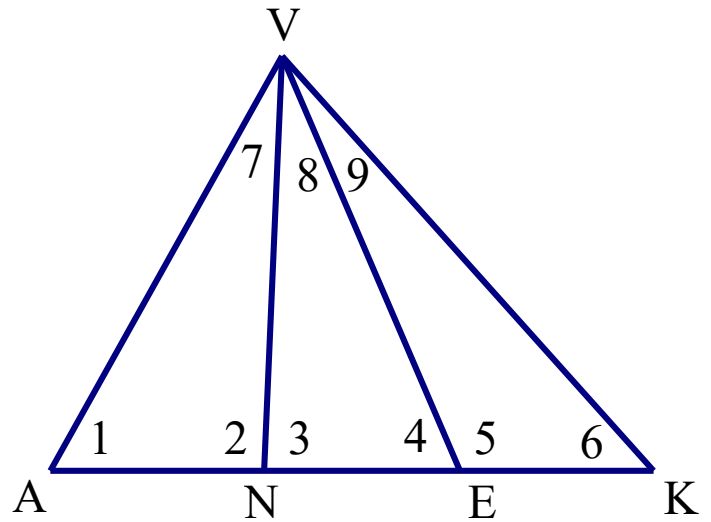
Label $\angle ACT$ with a 1
Label $\angle CTA$ with a 2
Label $\angle CAT$ with a 3
Label \overline{TA} with an X
Label \overline{CA} with a Y
Label \overline{TC} with a Z

Name the following angles using numbers:

7. $\angle CGB$
8. $\angle CGF$
9. $\angle CGE$
10. $\angle FGE$
11. $\angle AGF$
12. $\angle FGB$
13. $\angle AGE$
14. $\angle BGA$
15. $\angle DGC$
16. $\angle DGA$



17. $\angle VEN$
18. $\angle VEA$
19. $\angle AVE$
20. $\angle EVK$
21. $\angle KNV$
22. $\angle VAE$
23. $\angle KVA$
24. $\angle NVK$
25. $\angle ENV$
26. $\angle EVK$



Name _____
Mr. Schlansky

Date _____
Geometry

Classifying Triangles

Classify the following triangles as acute/obtuse/right and scalene/isosceles/equilateral

1. $90^\circ, 45^\circ$

2. $60^\circ, 60^\circ$



3. $110^\circ, 40^\circ$

4. $30^\circ, 80^\circ$

5. $20^\circ, 70^\circ$

6. $70^\circ, 40^\circ$

Name _____
Mr. Schlansky

Date _____
Geometry



Types of Triangles with Algebra

1. In $\triangle ABC$, $m\angle A = 3x$, $m\angle B = 4x - 19$, and $m\angle C = 3x - 1$. Which statement is true? $\triangle ABC$ is

- (1) Isosceles
- (2) Obtuse
- (3) Acute
- (4) Right

2. The angles of a triangle are in the ratio 2:2:5. The triangle must be:

- (1) Scalene
- (2) Right
- (3) Acute
- (4) Obtuse

3. The measures of the angles of a triangle are $7x + 6$, $9x - 20$, and $3x + 4$. The triangle is:

- (1) acute and scalene
- (2) acute and isosceles
- (3) obtuse and isosceles
- (4) obtuse and scalene

4. The measure of the angles of a triangle are $5x + 2$, $5x - 7$, and $4x + 17$. The triangle is:

- (1) acute
- (2) right
- (3) isosceles
- (4) obtuse

5. The measures of the angles of a triangle are $x - 2$, $5x + 13$, and $3x - 2$. The triangle is:
(1) isosceles (3) obtuse
(2) right (4) acute

6. The measure of the angles of a triangle are $7x + 9$, $2x + 3$, and $4x - 27$. The triangle is:
(1) acute and scalene (3) isosceles and acute
(2) right and acute (4) obtuse and isosceles

7. In $\triangle ABC$, $m\angle A = 3x + 1$, $m\angle B = 4x - 17$, and $m\angle C = 5x - 20$. Which type of triangle is $\triangle ABC$?
1) right
2) scalene
3) isosceles
4) equilateral

8. Triangle PQR has angles that are in the ratio 2:3:5. Which type of triangle is $\triangle PQR$?
1) acute
2) isosceles
3) obtuse
4) right

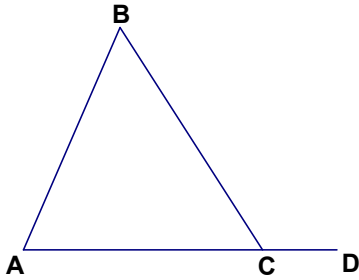
Name _____
Mr. Schlansky

Date _____
Geometry

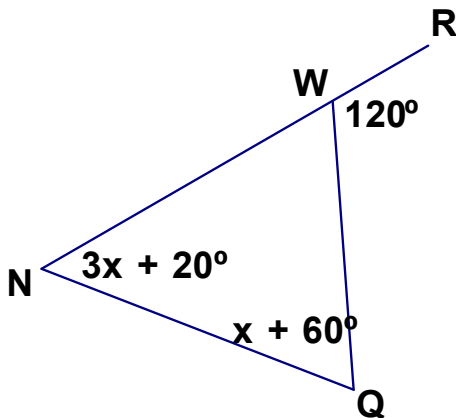
Exterior Angle Theorem



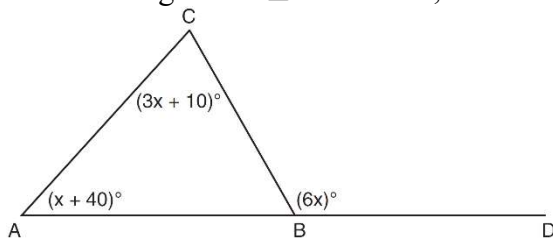
1. If $m\angle BCD = 110^\circ$ and $m\angle ABC = 40^\circ$, find $m\angle BAC$



2. Find the measure of $\angle QNW$ below



3. In the diagram of $\triangle ABC$ below, \overline{AB} is extended to point D .

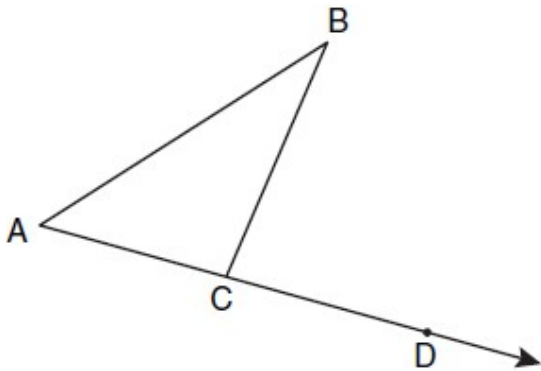


If $m\angle CAB = x + 40$, $m\angle ACB = 3x + 10$, $m\angle CBD = 6x$, what is $m\angle CAB$?

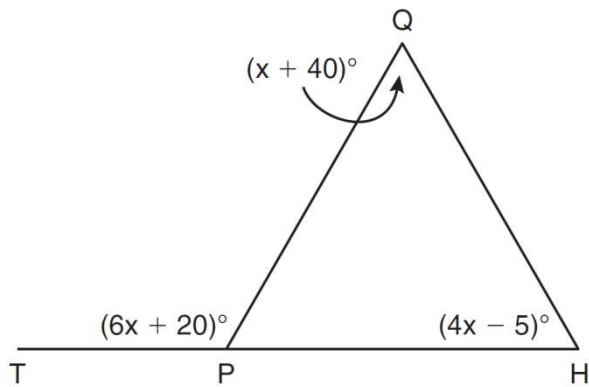
- 1) 13
- 2) 25
- 3) 53
- 4) 65

4. In the diagram below, $\triangle ABC$ is shown with \overline{AC} extended through point D .

If $m\angle BCD = 6x + 2$, $m\angle BAC = 3x + 15$, and $m\angle ABC = 2x - 1$, what is the value of x ?



5. In the diagram below of $\triangle HQP$, side \overline{HP} is extended through P to T , $m\angle QPT = 6x + 20$, $m\angle HQP = x + 40$, and $m\angle PHQ = 4x - 5$. Find $m\angle QPT$.

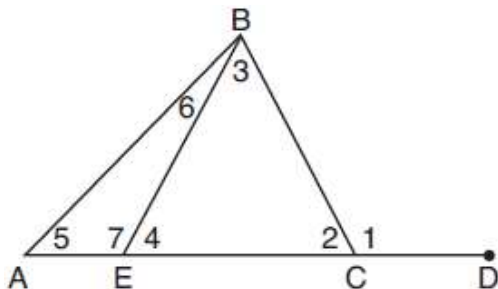


(Not drawn to scale)

6. In the diagram below of triangle ABC , \overline{AC} is extended through point C to point D , and \overline{BE} is drawn to AC .

Which equation is always true?

- | | |
|--|--|
| 1) $m\angle 1 = m\angle 3 + m\angle 2$ | 3) $m\angle 6 = m\angle 3 - m\angle 2$ |
| 2) $m\angle 5 = m\angle 3 - m\angle 2$ | 4) $m\angle 7 = m\angle 3 + m\angle 2$ |



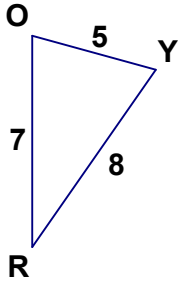
Name _____
Mr. Schlansky

Date _____
Geometry

Corresponding Sides and Angles



1. What is the largest angle of $\triangle ROY$? What is the smallest angle of $\triangle ROY$?



2. In triangle SPY, $m\angle S = 35^\circ$ and $m\angle Y = 70^\circ$. What is the largest side of the triangle? What is the shortest side of the triangle?

3. In $\triangle ABC$, $m\angle A = 45^\circ$ and $m\angle B = 60^\circ$. What is the largest side of $\triangle ABC$? What is the smallest side of $\triangle ABC$?

4. In $\triangle CAT$, $m\angle C = 65$, and $m\angle A = 40$. Which side is the shortest? Which side is the longest?

5. In triangle TYL, $m\angle T = 71^\circ$ and $m\angle Y = 42^\circ$. What is the smallest side of the triangle? What is the largest side of the triangle?

6. In triangle LYS, $m\angle L = 48^\circ$ and $m\angle Y = 101^\circ$. What is the smallest side of the triangle? What is the largest side of the triangle?

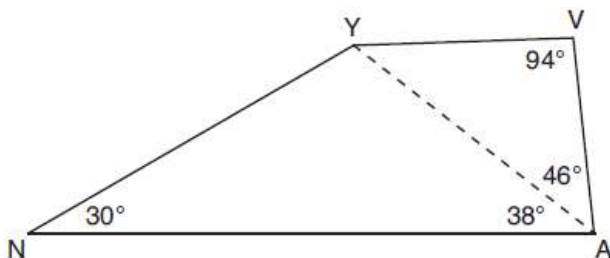
7. In $\triangle ABC$, $m\angle A = 60$, $m\angle B = 80$, and $m\angle C = 40$. Which inequality is true?

- 1) $AB > BC$
- 2) $AC > BC$
- 3) $AC < BA$
- 4) $BC < BA$

8. In the diagram of quadrilateral NAVY below, $m\angle YVA = 30^\circ$, $m\angle YAV = 38^\circ$, $m\angle AVY = 94^\circ$, and $m\angle VAY = 46^\circ$.

Which segment has the shortest length?

- | | |
|--------------------|--------------------|
| 1) \overline{AY} | 3) \overline{VA} |
| 2) \overline{NY} | 4) \overline{VY} |



Name _____
Mr. Schlansky

Date _____
Geometry

Triangle Inequality Theorem



1. Which of the following cannot make up the three sides of a triangle?

- | | |
|------------|------------|
| 1) {3,5,4} | 3) {9,7,5} |
| 2) {2,2,3} | 4) {6,1,4} |

2. Which of the following can make up the three sides of a triangle?

- | | |
|------------|------------|
| 1) {2,4,2} | 3) {8,1,6} |
| 2) {1,7,4} | 4) {5,5,7} |

3. Which numbers could represent the lengths of the sides of a triangle?

- 1) 5,9,14
- 2) 7,7,15
- 3) 1,2,4
- 4) 3,6,8

4. Which of the following cannot make up the three sides of a triangle?

- | | |
|-------------|-------------|
| 1) {5,1,6} | 3) {3,5,6} |
| 2) {9,14,8} | 4) {7,10,4} |

5. Which set of numbers represents the lengths of the sides of a triangle?

- | | |
|----------------|----------------|
| 1) {5, 18, 13} | 3) {16, 24, 7} |
| 2) {6, 17, 22} | 4) {26, 8, 15} |

6. Which of the following cannot make up the three sides of a triangle?

- | | |
|------------|--------------|
| 1) {3,9,7} | 3) {8,12,15} |
| 2) {2,7,5} | 4) {9,3,7} |

7. In $\triangle BLA$, $\overline{BL} = 12$ and $\overline{AL} = 8$. What is the range of possible values of \overline{BA} ?

8. In $\triangle CAM$, $\overline{CM} = 10$ and $\overline{CA} = 4$. What is the range of possible values of \overline{MA} ?

9. In $\triangle ABC$, $AB = 5$ feet and $BC = 3$ feet. Which inequality represents all possible values for the length of \overline{AC} , in feet?

- 1) $2 \leq AC \leq 8$
- 2) $2 < AC < 8$
- 3) $3 \leq AC \leq 7$
- 4) $3 < AC < 7$

10. Two sides of a triangle are 7 and 11. The third side of the triangle can measure:

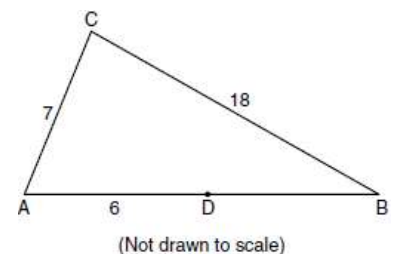
- 1) 4
- 2) 18
- 3) 8
- 4) 21

11. Jacquie is building a triangular fence for her tomato garden. She has an eight foot piece of fence and a four foot piece of fence. Which can be the length of the third piece of fence?

- 1) 2 feet
- 2) 5 feet
- 3) 4 feet
- 4) 12 feet

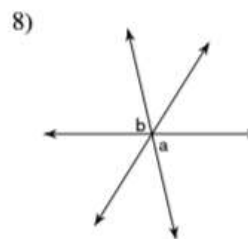
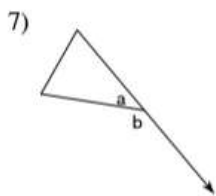
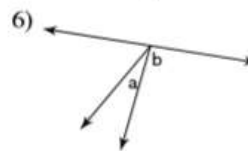
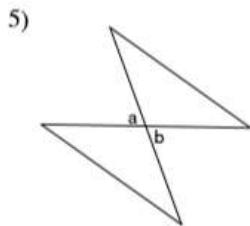
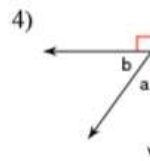
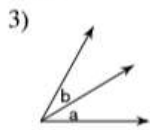
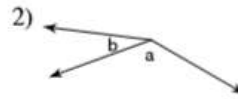
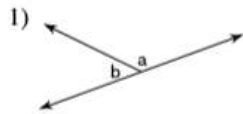
12. In the diagram below of $\triangle ABC$, D is a point on \overline{AB} , $AC = 7$, $AD = 6$, and $BC = 18$. The length of \overline{DB} could be

- 1) 5
- 2) 12
- 3) 19
- 4) 25

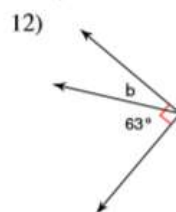
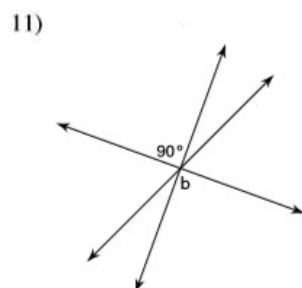
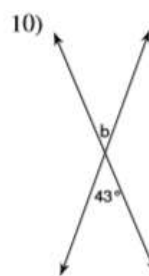
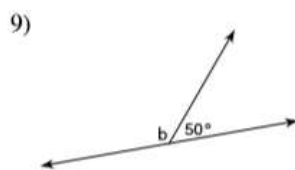


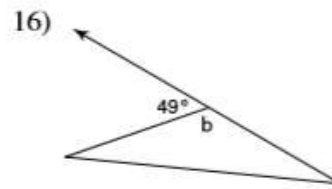
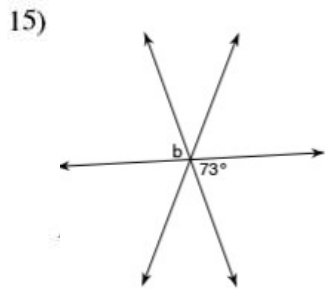
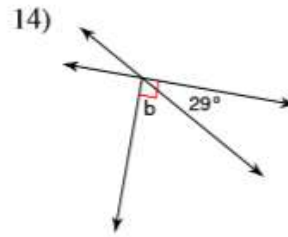
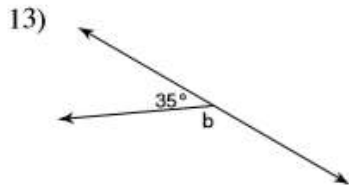
Angle Pairs: Linear Pairs, Complementary, Vertical

Determine whether the following pairs of angles are linear pairs, complementary, vertical, or neither.

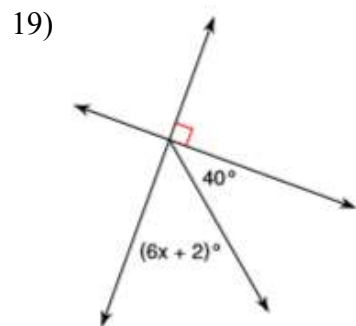
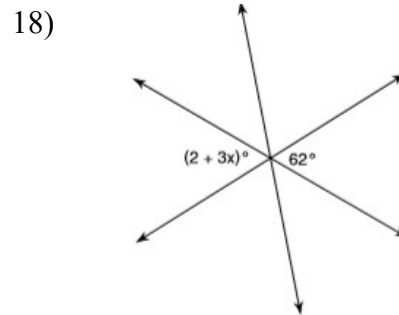
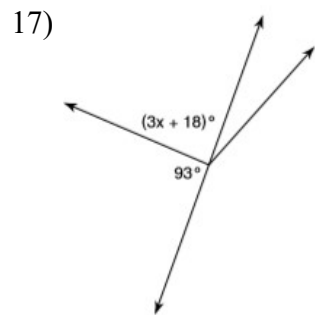


Find angle b in the following examples.





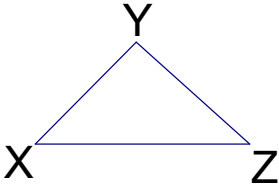
Find the value of x.



Isosceles Triangles, Angle Bisectors, and Equilateral Triangles

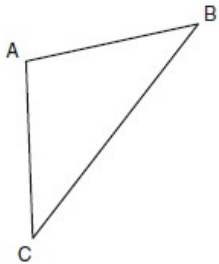


1. In $\triangle XYZ$, $\overline{XY} \cong \overline{YZ}$. If $m\angle Z = 41^\circ$, find the measure of $\angle Y$.



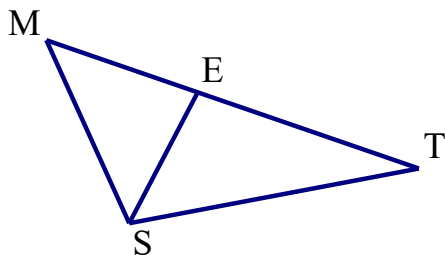
2. In $\triangle PQR$, $\overline{PQ} \cong \overline{QR}$. If $m\angle PQR = 94^\circ$, find the measure of $\angle QPR$.

3. In the diagram of $\triangle ABC$ below, $\overline{AB} \cong \overline{AC}$. The measure of $\angle B$ is 40° . What is the measure of $\angle A$?

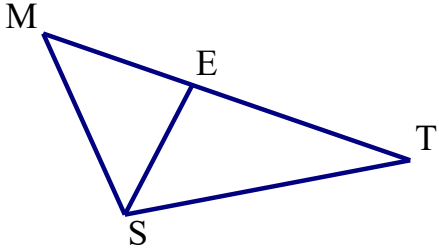


4. In $\triangle RST$, $m\angle RST = 46$ and $\overline{RS} \cong \overline{ST}$. Find $m\angle STR$.

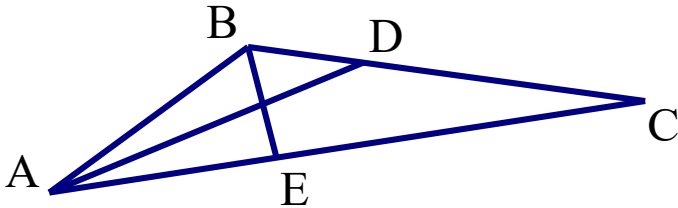
5. In the diagram below of $\triangle MST$, \overline{ES} bisects $\angle MST$. If $m\angle MST = 70$, find $\angle MSE$ and $\angle TSE$.



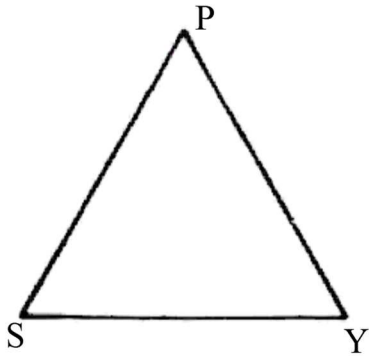
6. In the diagram below of $\triangle MST$, \overline{ES} bisects $\angle MST$. If $m\angle MSE = 40$, find $\angle TSE$ and $\angle TSM$.



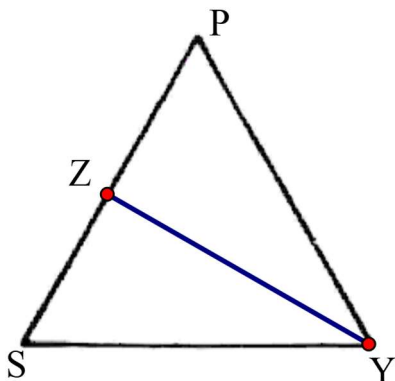
7. In the diagram below of $\triangle ABC$, \overline{DA} bisects $\angle BAC$ and \overline{BE} bisects $\angle ABC$. If $\angle BAD = 20$ and $\angle ABC = 100$, find $\angle CAD$, $\angle CAB$, $\angle ABE$, $\angle CBE$.



8. In the diagram below, $\triangle SPY$ is equilateral. Find the measure of $\angle S$, $\angle P$, $\angle Y$.



9. In the diagram below, $\triangle SPY$ is equilateral and \overline{ZY} bisects $\angle PYS$. Find the measure of $\angle PYZ$.

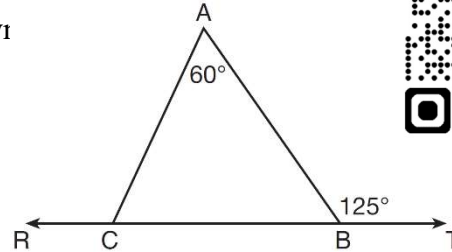


Complex Triangle Problems



1. In the diagram below, $\overleftrightarrow{RCBT}$ and $\triangle ABC$ are shown. What is $m\angle ACR$?

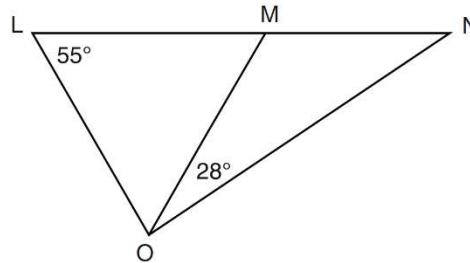
- 1) 125
- 2) 115
- 3) 65
- 4) 55



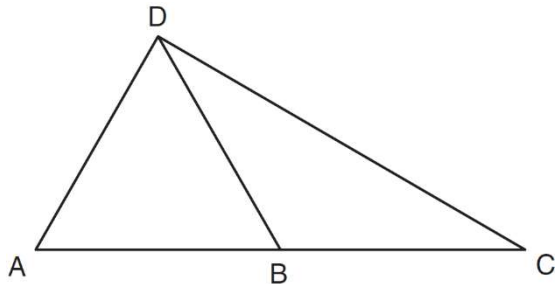
2. In the diagram below, $\triangle LMO$ is isosceles with $LO = MO$.

If $m\angle L = 55$ and $m\angle NOM = 28$, what is $m\angle N$?

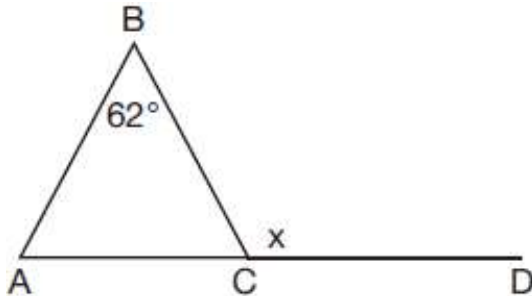
- 1) 27
- 2) 28
- 3) 42
- 4) 70



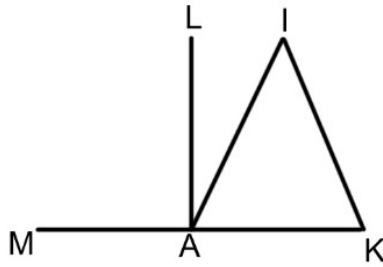
3. In the diagram below of $\triangle ACD$, B is a point on \overline{AC} such that $\triangle ADB$ is an equilateral triangle, and $\triangle DBC$ is an isosceles triangle with $\overline{DB} \cong \overline{BC}$. Find $m\angle C$.



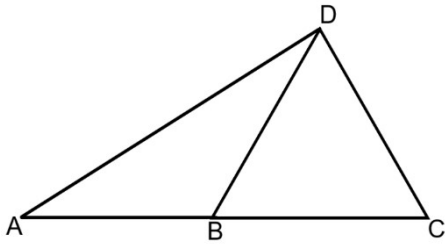
4. Given $\triangle ABC$ with $m\angle B = 62^\circ$ and side \overline{AC} extended to D , as shown below. Which value of x makes $\overline{AB} \cong \overline{CB}$?



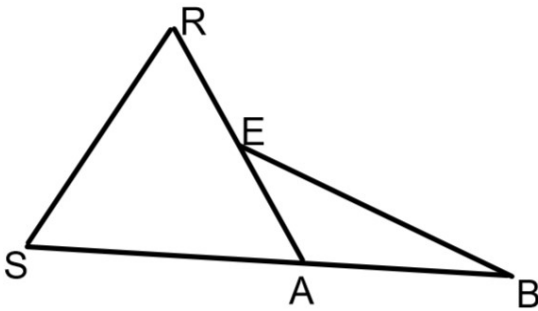
5. In the diagram below, $m\angle MAL = 90$, $m\angle IAL = 20$, and $\overline{IA} \cong \overline{AK}$. Find $m\angle I$.



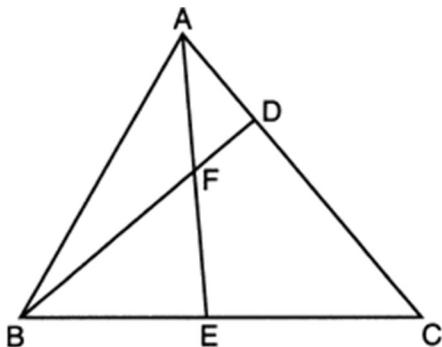
6. In the diagram below, $\triangle DBC$ is an equilateral triangle and $m\angle ADB = 25$. Find $m\angle DAB$.



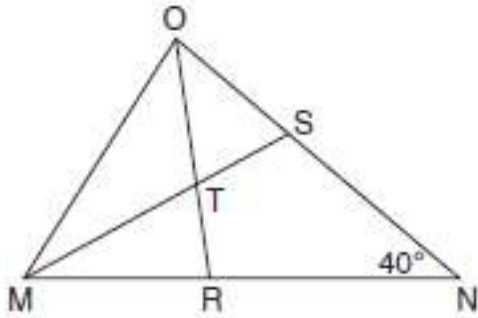
7. In the diagram below, $\overline{SR} \cong \overline{RA}$, $m\angle SRA = 40$, and $m\angle ABE = 30$. Find $m\angle BEA$.



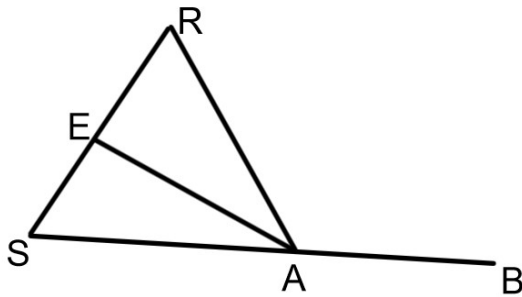
8. In the diagram of $\triangle ABC$ below, \overline{AE} bisects angle BAC , and altitude \overline{BD} is drawn. If $m\angle C = 50^\circ$ and $m\angle ABC = 60^\circ$, what is $m\angle FEB$?



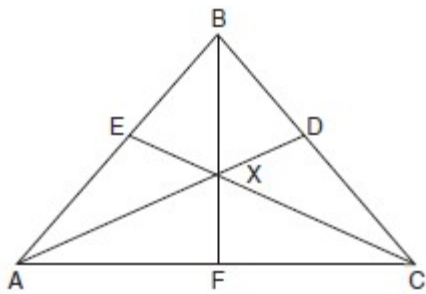
9. In the diagram below of triangle MNO , $\angle M$ and $\angle O$ are bisected by \overline{MS} and \overline{OR} , respectively. Segments MS and OR intersect at T , and $m\angle N = 40^\circ$. If $m\angle TMR = 28^\circ$, what is the measure of angle OTS ?



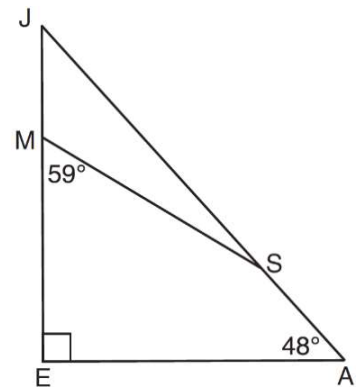
10. In the diagram below, \overline{EA} bisects $\angle SAR$, $\overline{RA} \cong \overline{AS}$ and $m\angle SRA = 55$. Find $m\angle RAB$ and $m\angle REA$.



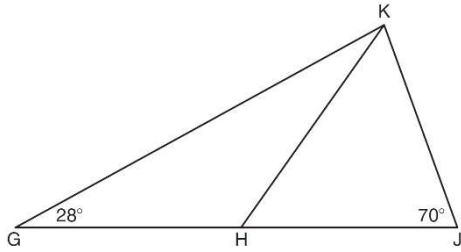
11. In the diagram below of isosceles triangle ABC , $\overline{AB} \cong \overline{CB}$ and angle bisectors \overline{AD} , \overline{BF} , and \overline{CE} are drawn and intersect at X . If $m\angle BAC = 50^\circ$, find $m\angle AXC$.



12. In the diagram of $\triangle JEA$ below, $m\angle JEA = 90$ and $m\angle EAJ = 48$. Line segment MS connects points M and S on the triangle, such that $m\angle EMS = 59$. What is $m\angle JSM$?



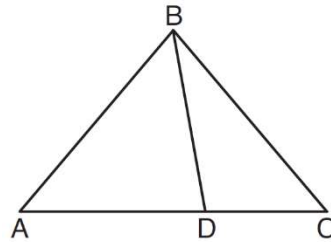
13. In the diagram below of $\triangle GJK$, H is a point on \overline{GJ} , $\overline{HJ} \cong \overline{JK}$, $m\angle G = 28$, and $m\angle GJK = 70$. Determine whether $\triangle GHK$ is an isosceles triangle and justify your answer.



14. In the diagram below, $m\angle BDC = 100^\circ$, $m\angle A = 50^\circ$, and $m\angle DBC = 30^\circ$.

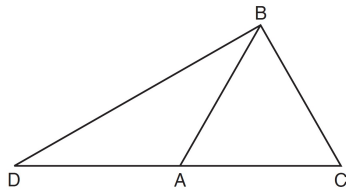
Which statement is true?

- 1) $\triangle ABD$ is obtuse.
- 2) $\triangle ABC$ is isosceles.
- 3) $m\angle ABD = 80^\circ$
- 4) $\triangle ABD$ is scalene.



15. In the diagram of $\triangle BCD$ shown below, \overline{BA} is drawn from vertex B to point A on \overline{DC} , such that $\overline{BC} \cong \overline{BA}$.

In $\triangle DAB$, $m\angle D = x$, $m\angle DAB = 5x - 30$, and $m\angle DBA = 3x - 60$. In $\triangle ABC$, $AB = 6y - 8$ and $BC = 4y - 2$. [Only algebraic solutions can receive full credit.] Find $m\angle D$. Find $m\angle BAC$. Find the length of \overline{BC} . Find the length of \overline{DC} .



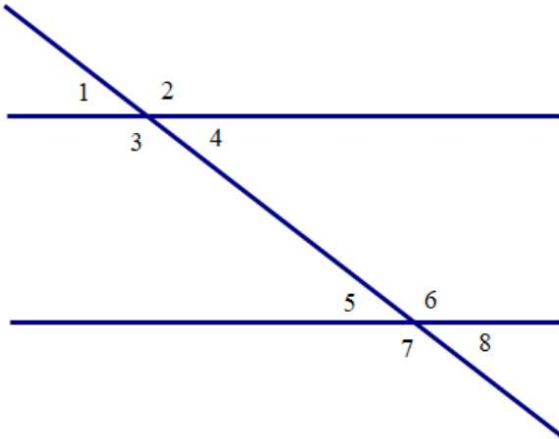
Name _____
Mr. Schlansky

Date _____
Geometry

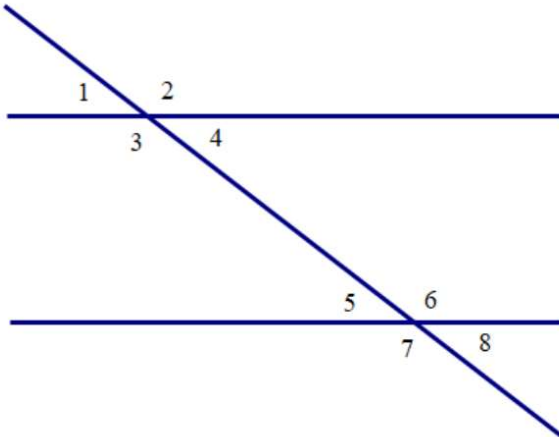


Parallel Lines Cut By a Transversal

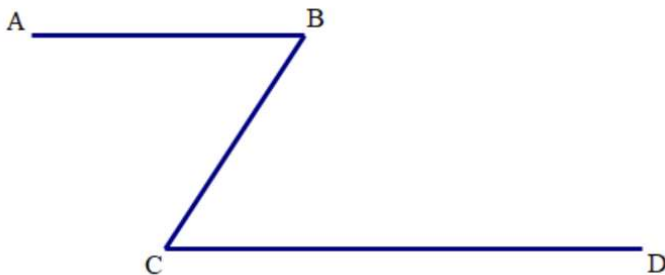
1. In the diagram below, two parallel lines are cut by a transversal. If $m\angle 1 = 60$, fill in the rest of the angles.



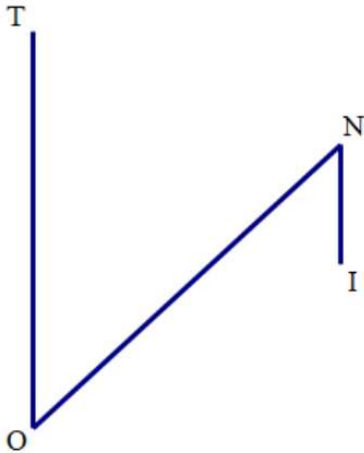
2. In the diagram below, two parallel lines are cut by a transversal. If $m\angle 2 = 100$, fill in the rest of the angles.



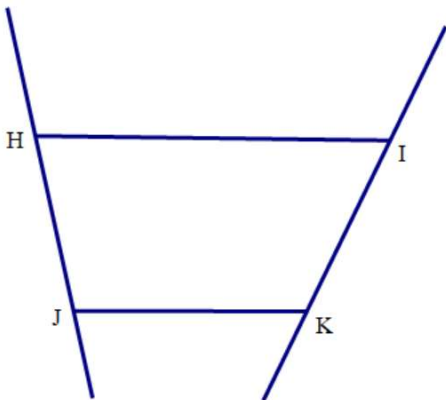
3. In the diagram below, $\overline{AB} \parallel \overline{CD}$. If $m\angle ABC = 40$, create and find 8 angles.



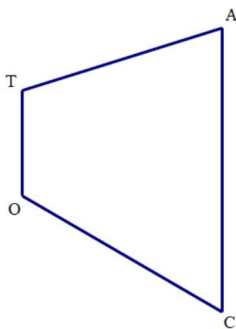
4. In the diagram below, $\overline{TO} \parallel \overline{NI}$. If $m\angle TON = 30$, create and find 8 angles.



5. In the diagram below, $\overline{HI} \parallel \overline{JK}$. If $m\angle HIK = 70$ and $m\angle HJK = 130$, create and find 16 angles.

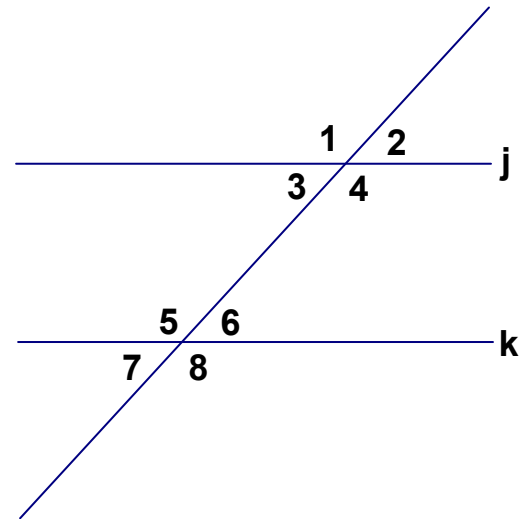


6. Trapezoid TACO has $\overline{TO} \parallel \overline{AC}$. If $m\angle TOC = 120$ and $m\angle TAC = 40$, create and find 16 angles.



7. In figure 1, if $j \parallel k$, which of the following must be true?
 (1) $\angle 1 \cong \angle 2$ (3) $\angle 2 \cong \angle 4$
 (2) $\angle 1$ is supplementary to $\angle 5$ (4) $\angle 3 \cong \angle 6$

Figure 1

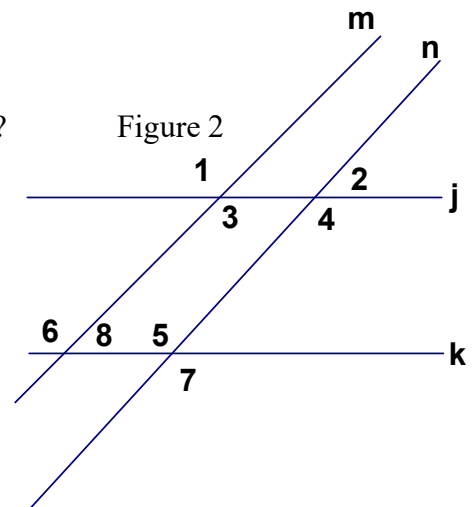


8. In figure 1, if $j \parallel k$, which of the following must be true?
 (1) $\angle 1$ is supplementary to $\angle 7$ (3) $\angle 6 \cong \angle 8$
 (2) $\angle 1$ is supplementary to $\angle 4$ (4) $\angle 5 \cong \angle 2$

9. In figure 1, if $j \parallel k$, which of the following must be true?
 (1) $\angle 5$ is supplementary to $\angle 4$ (3) $\angle 6 \cong \angle 4$
 (2) $\angle 2$ is supplementary to $\angle 3$ (4) $\angle 5 \cong \angle 4$

10. In figure 2, if $\angle 1 \cong \angle 4$, which of the following must be true?
 (1) $j \parallel k$ (3) $m \parallel n$
 (2) $\angle 5 \cong \angle 8$ (4) m not \parallel to n

Figure 2

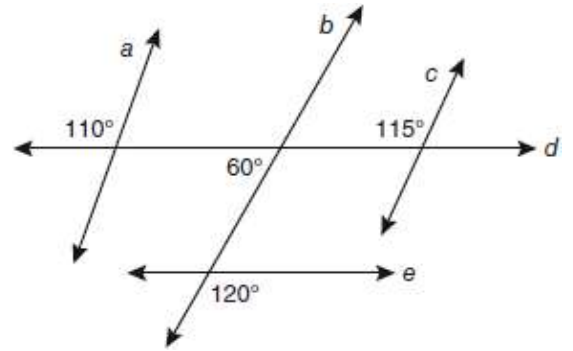


11. In figure 2, if $\angle 7$ is not supplementary to $\angle 2$, which of the following *must* be true?
 (1) $j \parallel k$ (3) $m \parallel n$
 (2) j not \parallel to k (4) m not \parallel to n

12. In figure 2, if $\angle 4$ *not* $\cong \angle 1$, which of the following must be true?
 (1) $j \parallel k$ (3) $m \parallel n$
 (2) j not \parallel to k (4) m not \parallel to n

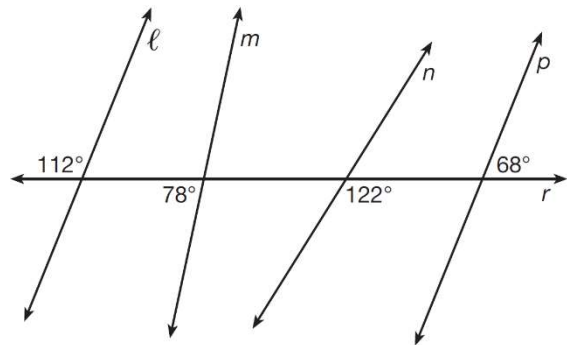
13. Based on the diagram below, which statement is true?

- 1) $a \parallel b$
- 2) $a \parallel c$
- 3) $b \parallel c$
- 4) $d \parallel e$



14. In the diagram below, lines ℓ , m , n , and p intersect line r . Which statement is true?

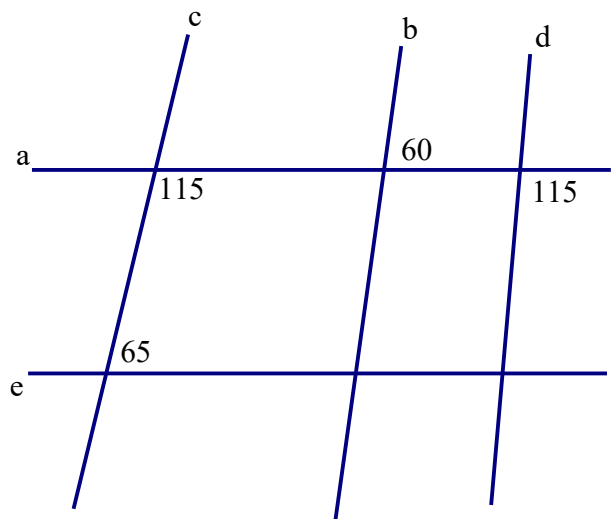
- 1) $\ell \parallel n$
- 2) $\ell \parallel p$
- 3) $m \parallel p$
- 4) $m \parallel n$



15. Which of the following statements are true?

- I: $a \parallel e$
- II: $c \parallel b$
- III: $c \parallel d$
- IV: $b \parallel d$

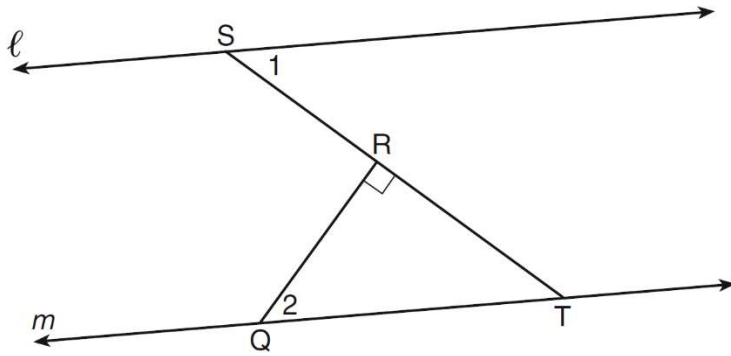
- 1) I only
- 2) II only
- 3) I and III only
- 4) II and IV only



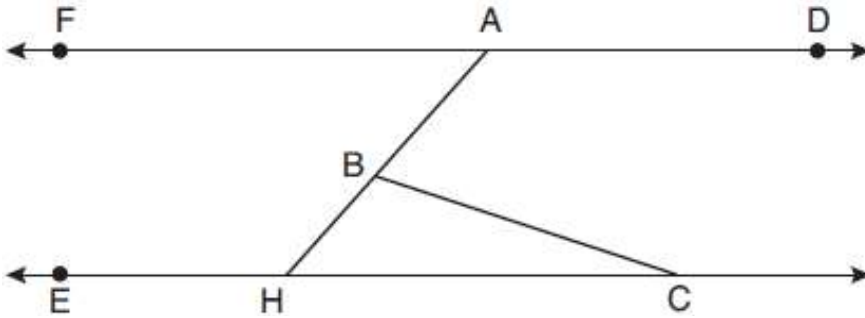
Parallel Lines With Triangles



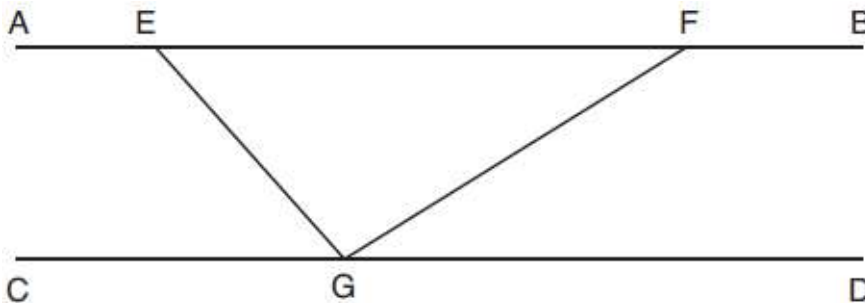
1. In the diagram below, $\ell \parallel m$ and $\overline{QR} \perp \overline{ST}$.
If $m\angle 1 = 63$, find $m\angle 2$.



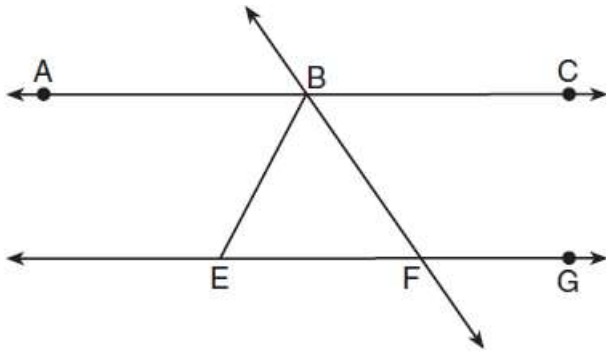
2. In the diagram below, $\overline{FAD} \parallel \overline{EHC}$, and \overline{ABH} and \overline{BC} are drawn. If $m\angle FAB = 48^\circ$ and $m\angle ECB = 18^\circ$, what is $m\angle ABC$?



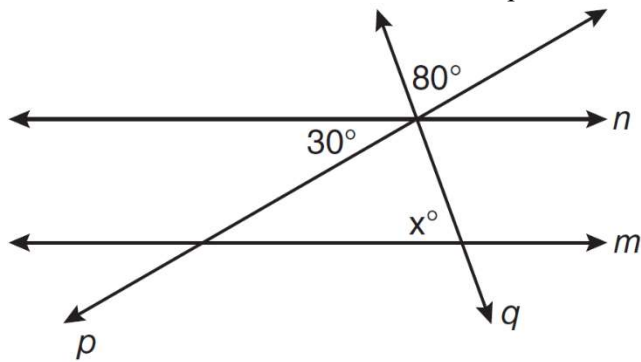
3. In the diagram below, $\overline{AEFB} \parallel \overline{CGD}$, and \overline{GE} and \overline{GF} are drawn.
If $m\angle EFG = 32^\circ$ and $m\angle CGE = 43$, what is $m\angle EGF$?



4. As shown in the diagram below, $\overleftrightarrow{ABC} \parallel \overleftrightarrow{EFG}$ and $\overline{BF} \cong \overline{EF}$.
 If $m\angle CBF = 42.5^\circ$, find $m\angle EBF$.

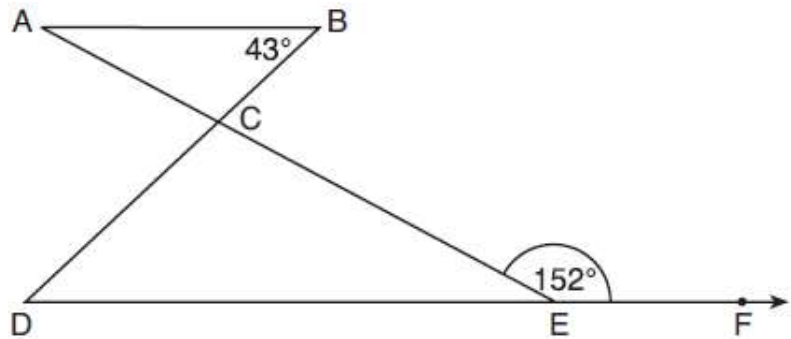


5. In the diagram below, lines n and m are cut by transversals p and q .
 What value of x would make lines n and m parallel?

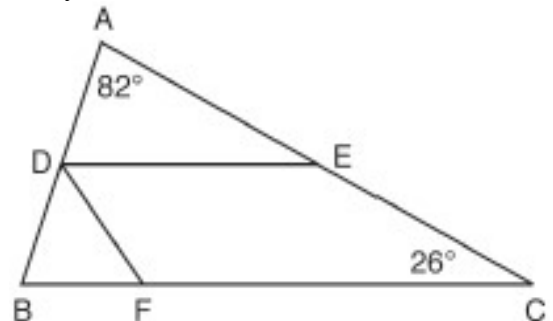


6. In the diagram below, $\overline{AB} \parallel \overline{DEF}$, \overline{AE} and \overline{BD} intersect at C , $m\angle B = 43^\circ$, and $m\angle CEF = 152^\circ$.
 Which statement is true?

- 1) $m\angle D = 28^\circ$
- 2) $m\angle A = 43^\circ$
- 3) $m\angle ACD = 71^\circ$
- 4) $m\angle BCE = 109^\circ$



7. In the diagram below, \overline{DE} divides \overline{AB} and \overline{AC} proportionally, $m\angle C = 26^\circ$, $m\angle A = 82^\circ$, and \overline{DF} bisects $\angle BDE$. What is the measure of angle DFB ?



Name _____
Mr. Schlansky

Date _____
Geometry

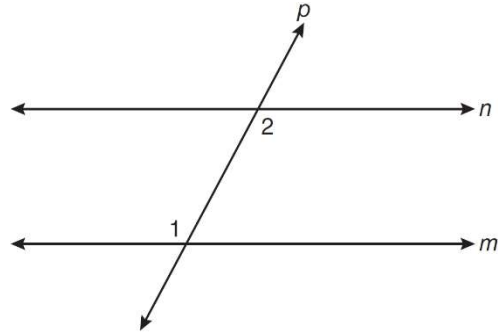


Parallel Lines Cut By a Transversal with Algebra

1. In the diagram below, line p intersects line m and line n .

If $m\angle 1 = 7x$ and $m\angle 2 = 5x + 30$, lines m and n are parallel when x equals

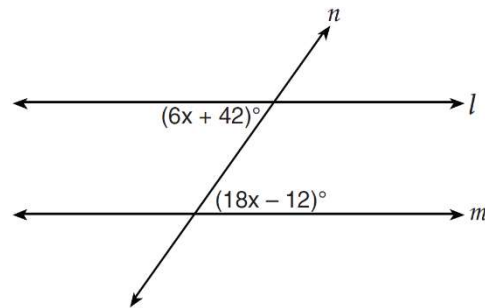
- 1) 12.5
- 2) 15
- 3) 87.5
- 4) 105



2. Line n intersects lines l and m , forming the angles shown in the diagram below.

Which value of x would prove $l \parallel m$?

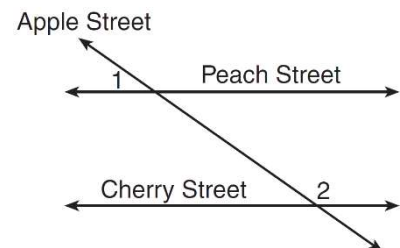
- 1) 2.5
- 2) 4.5
- 3) 6.25
- 4) 8.75



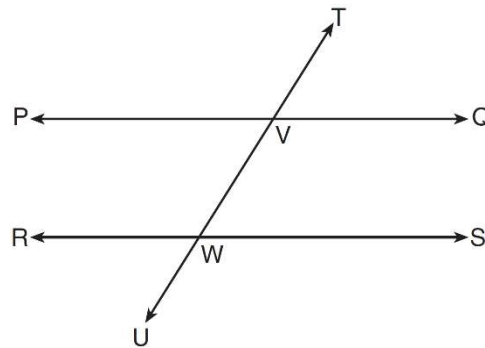
3. Peach Street and Cherry Street are parallel. Apple Street intersects them, as shown in the diagram below.

If $m\angle 1 = 2x + 36$ and $m\angle 2 = 7x - 9$, what is $m\angle 1$?

- 1) 9
- 2) 17
- 3) 54
- 4) 70



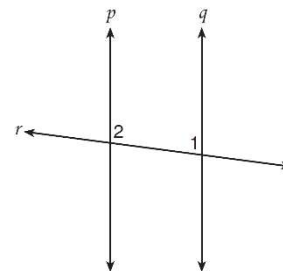
4. In the diagram below, transversal \overleftrightarrow{TU} intersects \overleftrightarrow{PQ} and \overleftrightarrow{RS} at V and W , respectively.



If $m\angle TVQ = 5x - 22$ and $m\angle VWS = 3x + 10$, for which value of x is $\overleftrightarrow{PQ} \parallel \overleftrightarrow{RS}$?

- 1) 6
- 2) 16
- 3) 24
- 4) 28

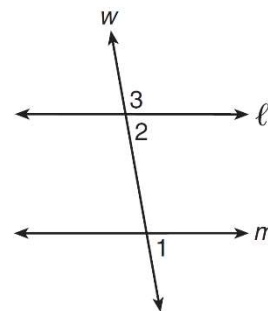
5. Lines p and q are intersected by line r , as shown below.



If $m\angle 1 = 7x - 36$ and $m\angle 2 = 5x + 12$, for which value of x would $p \parallel q$?

- 1) 17
- 2) 24
- 3) 83
- 4) 97

6. In the diagram below, line ℓ is parallel to line m , and line w is a transversal.



If $m\angle 2 = 3x + 17$ and $m\angle 3 = 5x - 21$, what is $m\angle 1$?

- 1) 19
- 2) 23
- 3) 74
- 4) 86

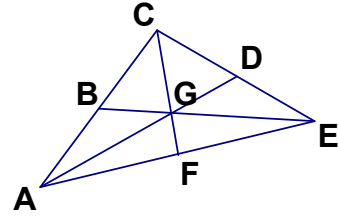
(Not drawn to scale)



Intersecting Medians (Centroid Problems)

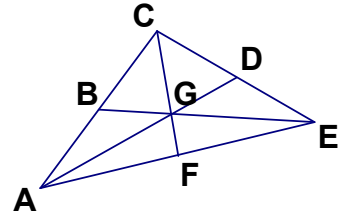
1. In the given triangle, all three medians are drawn in. If $\overline{AG} = 10$, find

- a) \overline{GD}
- b) \overline{AD}



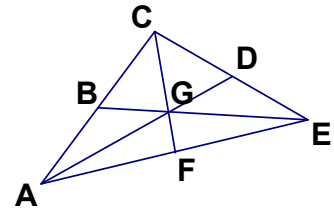
2. In the given triangle, all three medians are drawn in. If $\overline{FG} = 4$, find

- a) \overline{CG}
- b) \overline{CF}



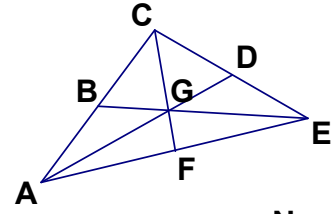
3. In the given triangle, all three medians are drawn in. If $\overline{AD} = 24$, find

- a) \overline{AG}
- b) \overline{DG}



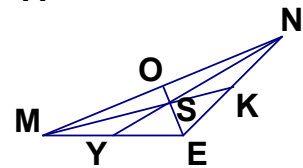
4. In the given triangle, all three medians are drawn in. If $\overline{AC} = 30$, find

- a) \overline{AB}
- b) \overline{BC}



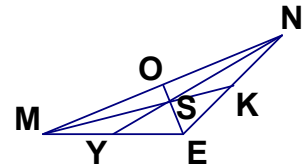
5. In the given triangle, all three medians are drawn in. If $\overline{MS} = 12$, find

- a) \overline{SK}
- b) \overline{MK}



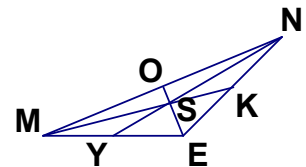
6. In the given triangle, all three medians are drawn in. If $\overline{OE} = 9$, find

- a) \overline{OS}
- b) \overline{SE}

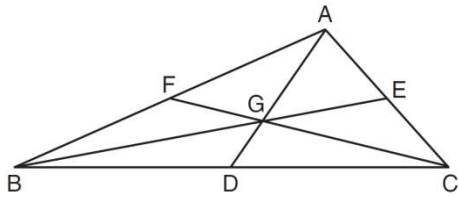


7. In the given triangle, all three medians are drawn in. If $\overline{YN} = 30$, find

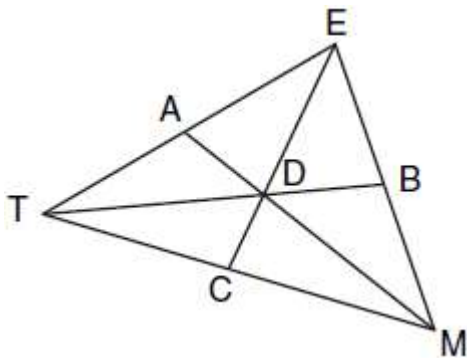
- a) \overline{YS}
- b) \overline{SN}



8. In the diagram below of $\triangle ABC$, medians \overline{AD} , \overline{BE} , and \overline{CF} intersect at G . If $CF = 24$, what is the length of \overline{FG} ?



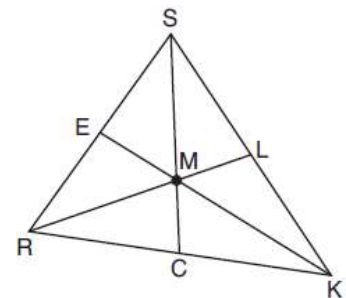
9. In the diagram below of $\triangle TEM$, medians \overline{TB} , \overline{EC} , and \overline{MA} intersect at D , and $TB = 9$. Find the length of \overline{TD} .



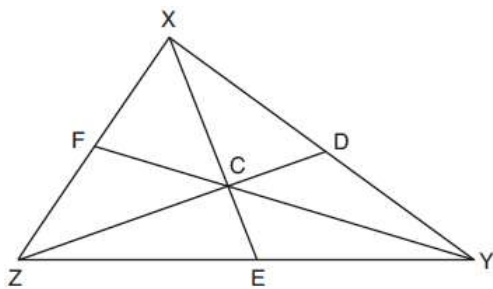
10. In triangle SRK below, medians \overline{SC} , \overline{KE} , and \overline{RL} intersect at M .

Which statement must always be true?

- 1) $3(MC) = SC$
- 2) $MC = \frac{1}{3}(SM)$
- 3) $RM = 2MC$
- 4) $SM = KM$



11. In $\triangle XYZ$, shown below, medians \overline{XE} , \overline{YF} , and \overline{ZD} intersect at C . If $CE = 5$, $YF = 21$, and $XZ = 15$, determine and state the perimeter of triangle CFX .



Name _____
Mr. Schlansky

Date _____
Geometry



Triangles/Parallel Lines Review Sheet

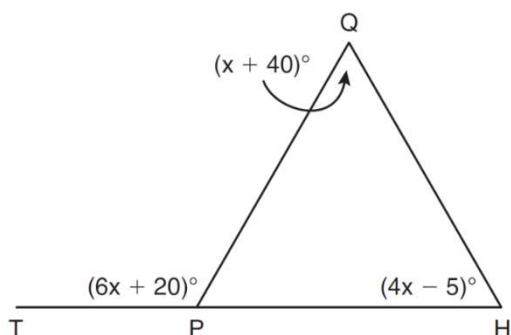
1. In $\triangle ABC$, $m\angle A = 3x + 1$, $m\angle B = 4x - 17$, and $m\angle C = 5x - 20$. Which type of triangle is $\triangle ABC$?

- 1) right
- 2) scalene
- 3) isosceles
- 4) equilateral

2. Triangle PQR has angles that are in the ratio 2:3:5. Which type of triangle is $\triangle PQR$?

- 1) acute
- 2) isosceles
- 3) obtuse
- 4) right

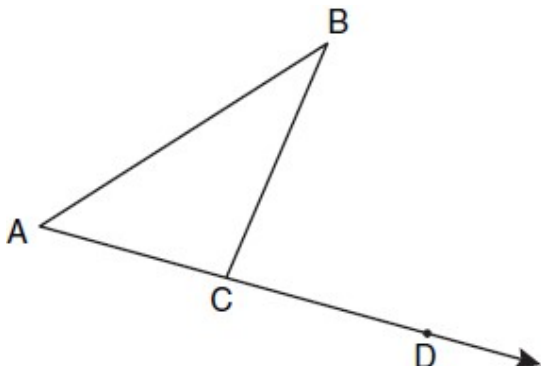
3. In the diagram below of $\triangle HQP$, side \overline{HP} is extended through P to T , $m\angle QPT = 6x + 20$, $m\angle HQP = x + 40$, and $m\angle PHQ = 4x - 5$. Find $m\angle QPT$.



(Not drawn to scale)

4. In the diagram below, $\triangle ABC$ is shown with \overline{AC} extended through point D .

If $m\angle BCD = 6x + 2$, $m\angle BAC = 3x + 15$, and $m\angle ABC = 2x - 1$, what is the value of x ?



5. In triangle SPY, $m\angle S = 35^\circ$ and $m\angle Y = 70^\circ$. What is the largest side of the triangle? What is the shortest side of the triangle?

6. In $\triangle ABC$, $m\angle A = 45^\circ$ and $m\angle B = 60^\circ$. What is the largest side of $\triangle ABC$? What is the smallest side of $\triangle ABC$?

7. Which set of numbers represents the lengths of the sides of a triangle?

- 1) {5, 18, 13}
- 2) {6, 17, 22}
- 3) {16, 24, 7}
- 4) {26, 8, 15}

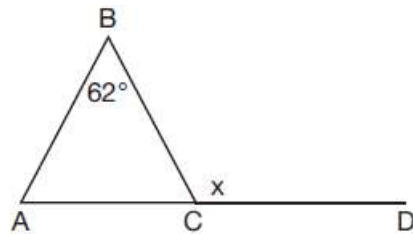
8. Which of the following cannot make up the three sides of a triangle?

- 1) {3, 9, 7}
- 2) {2, 7, 5}
- 3) {8, 12, 15}
- 4) {9, 3, 7}

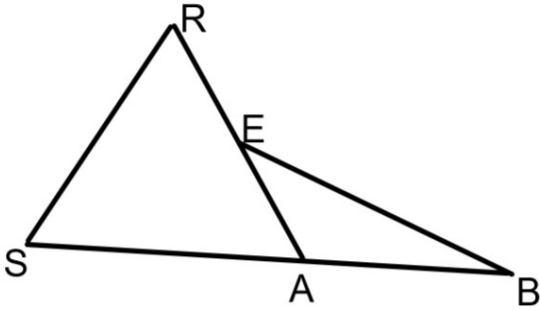
9. Given $\triangle ABC$ with $m\angle B = 62^\circ$ and side \overline{AC} extended to D , as shown below.

Which value of x makes $\overline{AB} \cong \overline{CB}$?

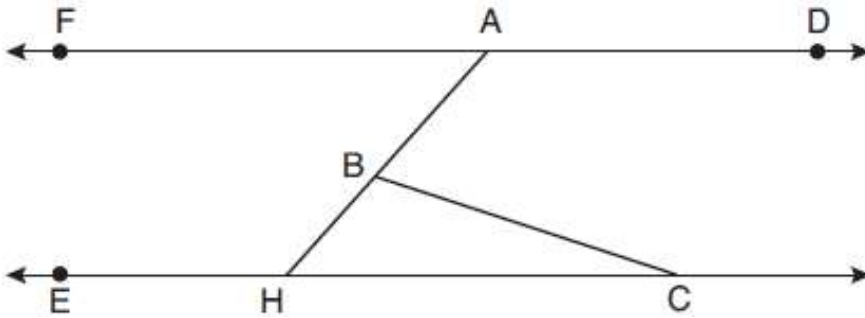
- 1) 59°
- 2) 62°
- 3) 118°
- 4) 121°



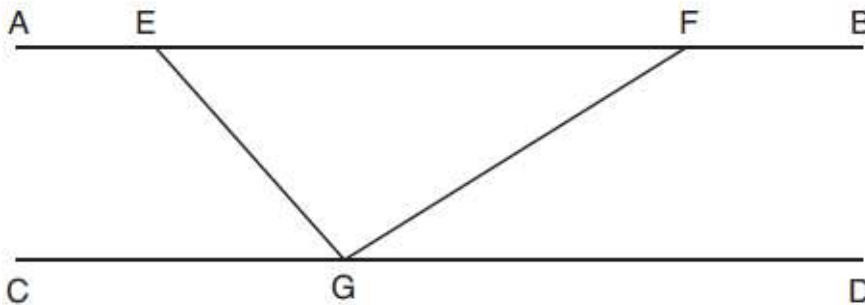
10. In the diagram below, $\overline{SR} \cong \overline{RA}$, $m\angle SRA = 40$, and $m\angle ABE = 30$. Find $m\angle BEA$.



11. In the diagram below, $\overline{FAD} \parallel \overline{EHC}$, and \overline{ABH} and \overline{BC} are drawn. If $m\angle FAB = 48^\circ$ and $m\angle ECB = 18^\circ$, what is $m\angle ABC$?



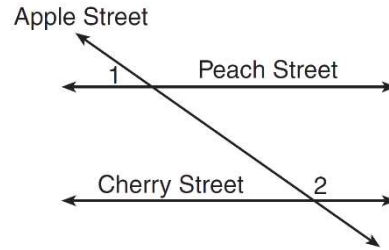
12. In the diagram below, $\overline{AEFB} \parallel \overline{CGD}$, and \overline{GE} and \overline{GF} are drawn. If $m\angle EFG = 32^\circ$ and $m\angle CGE = 43$, what is $m\angle EGF$?



13. Peach Street and Cherry Street are parallel. Apple Street intersects them, as shown in the diagram below.

If $m\angle 1 = 2x + 36$ and $m\angle 2 = 7x - 9$, what is $m\angle 1$?

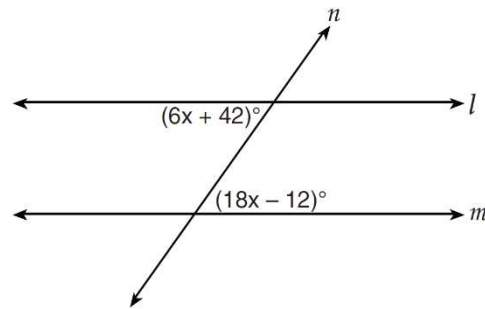
- 1) 9
- 2) 17
- 3) 54
- 4) 70



14. Line n intersects lines l and m , forming the angles shown in the diagram below.

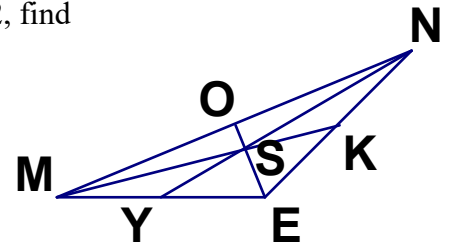
Which value of x would prove $l \parallel m$?

- 1) 2.5
- 2) 4.5
- 3) 6.25
- 4) 8.75



15. In the given triangle, all three medians are drawn in. If $\overline{MS} = 12$, find

- c) \overline{SK}
- d) \overline{MK}



16. In the given triangle, all three medians are drawn in. If $\overline{OS} = 9$, find

- c) \overline{ES}
- d) \overline{OE}

