

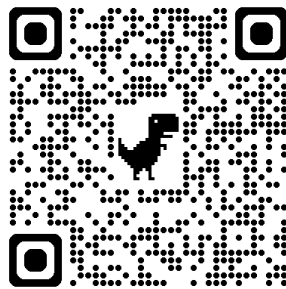
**Name:**

# **Common Core Algebra II**

## **Unit 8**

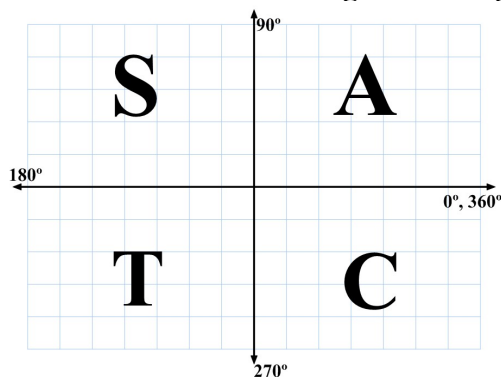
### **Trigonometry and Graphing Trigonometric Functions**

**Mr. Schlansky**



**2026**

**Lesson 1: I can sketch angles on the grid using 0, 90, 180, and 270.**



The reference angle is the acute angle made with the x-axis.

**Lesson 2: I can find co-terminal angles by adding or subtracting 360.**

We always want an angle between 0 and 360. If it is not, add or subtract 360 until it is.

**Lesson 3: I can convert between degrees and radians by multiplying by multiplying by  $\frac{\pi}{180}$  or  $\frac{180}{\pi}$ .**

Degrees to radians: Multiply by  $\frac{\pi}{180}$

Radians to degrees: Multiply by  $\frac{180}{\pi}$

\*If you are converting to degrees 180 is on top. If you are converting to radians  $\pi$  is on top.

**Lesson 4: I can sketch radian angles on the grid by converting to degrees by multiplying by  $\frac{180}{\pi}$  and using 0, 90, 180, and 270.**

1) Convert radians to degrees by multiplying by  $\frac{180}{\pi}$ .

2) Graph that angle on the grid.

\*If multiple choice, convert the radians to degrees first, whether the radians are in the problem or the answers.

**Lesson 5: I can find six trig ratios using SOHCAHTOA and the reciprocal trig functions.**

To find trig ratios:

**SOHCAHTOA**

$$\begin{array}{lll} \sin \theta = \frac{opp}{hyp} & \cos \theta = \frac{adj}{hyp} & \tan \theta = \frac{opp}{adj} \\ \csc \theta = \frac{hyp}{opp} & \sec \theta = \frac{hyp}{adj} & \cot \theta = \frac{adj}{opp} \end{array}$$

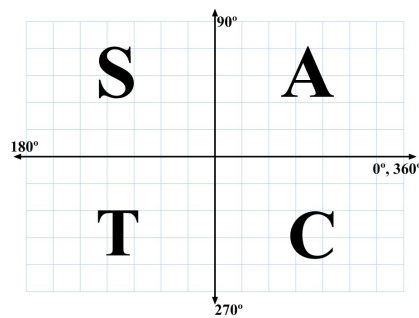
Reciprocal trig function pairs:

$$\begin{array}{lll} \csc \theta & \sec \theta & \tan \theta \\ \sin \theta & \cos \theta & \cot \theta \end{array}$$

**Lesson 6: I can determine the signs of each function in each quadrant using ASTC.**

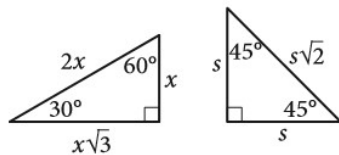
Unit Circle: A circle with a center at the origin and a radius of 1.

Any point on the unit circle is  $(\cos \theta, \sin \theta)$



<b>Quadrant I: All positive:</b>	<b>sin +</b>	<b>cos +</b>	<b>tan +</b>
<b>Quadrant II: Sine positive:</b>	<b>sin +</b>	<b>cos -</b>	<b>tan -</b>
<b>Quadrant III: Tangent positive:</b>	<b>sin -</b>	<b>cos -</b>	<b>tan +</b>
<b>Quadrant IV: Cosine positive:</b>	<b>sin -</b>	<b>cos +</b>	<b>tan -</b>

**Lesson 7: I can find the sides of special right angles using their given ratios**



Special Right Triangles

45, 45, 90: The legs are the same, the hypotenuse is the same with a  $\sqrt{2}$  after it.

30, 60, 90: The hypotenuse is double the small leg, the large leg is the same as the small leg with a  $\sqrt{3}$  after it.

	30	45	60
Sin	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$
Cos	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$
tan	$\frac{\sqrt{3}}{3}$	1	$\sqrt{3}$

**Lesson 8: I can evaluate special angles using QSFR**

To evaluate special angles (multiples of 30, 45, 60):

- 1) Sketch the angle on the grid and find the reference angle
- 2) List quadrant, sign, trig function, reference angle horizontally
- 3) Evaluate the given expression

\*Convert to degrees first if necessary

**Lesson 9: I can evaluate special angles multiple choice using QSFR**

- 1) Type in the original problem and write down the decimal
- 2) Type in each choice and see which decimal matches

\*DON'T CONVERT TO DEGREES!

\*For the reciprocal functions, type in 1 over the regular trig function.

Ex)  $\csc\left(\frac{2\pi}{3}\right) = \frac{1}{\sin\left(\frac{2\pi}{3}\right)}$

**Lesson 10: I can find a missing side of a right triangle using Pythagorean Theorem of Pythagorean Triples.**

Know your Pythagorean Triples!

$$a^2 + b^2 = c^2$$

$a$  and  $b$  are the legs

$c$  is the hypotenuse

3,4,5

5,12,13

7,24,25

8,15,17

9,40,41

If it is a Pythagorean Triple, use the triple to find the missing side.

If it is not a Pythagorean Triple, use  $a^2 + b^2 = c^2$  to find the third side.

\*If using Pythagorean Theorem, leave your answer as a radical if it is not a perfect square.

**Lesson 11: I can rationalize a denominator by multiplying the numerator and denominator by the radical.**

To rationalize the denominator, multiply top and bottom by the radical

When multiplying a radical by itself, the radical cancels out

**Lesson 12: I can find trig ratios using SOHCAHTOA, the reciprocal functions, and ASTC.**

To find a trig ratio,

1) Sketch a triangle on the grid connecting to the origin and x axis and then:

a) If given  $\sin/\cos/\tan = \frac{\text{something}}{\text{something}}$ , use SOHCAHTOA to fill in 2 sides of a triangle

b) If given a point, plot point and create triangle to origin and x axis. The x coordinate is the horizontal leg and the y coordinate is the vertical leg.

c) If given a circle, the radius is the hypotenuse and the x or y coordinate will be given.

d) If given a point on the unit circle,  $x = \cos \theta$  and  $y = \sin \theta$ . Follow procedure *a* from there.

2) Use Pythagorean Triples/Pythagorean Theorem to find the third side.

3) Find the trig ratios using SOHCAHTOA and the reciprocal functions.

4) Determine the signs using ASTC

\*Know your Pythagorean triples:  $\{3,4,5\}$ ,  $\{5, 12, 13\}$ ,  $\{8, 15, 17\}$ ,  $\{7, 24, 25\}$

**Lesson 13: I can practice finding trig ratios using SOHCAHTOA, the reciprocal functions, and ASTC.**

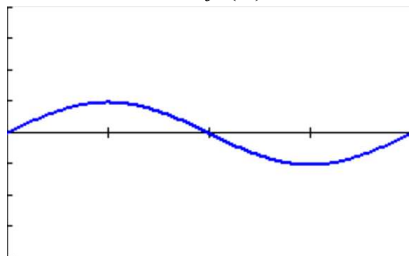
Same notes as lesson 11.

**Lesson 14: I can graph sinusoidal functions with different amplitudes, midlines, and frequencies using AMPSINFREQXSHIFT, knowing the four different waves, and using**

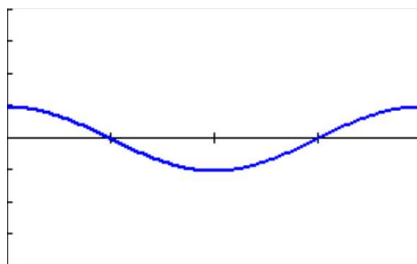
$$period = \frac{2\pi}{frequency}$$

**Know what your waves look like!**

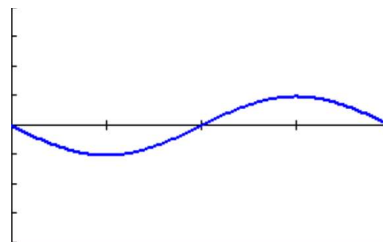
$$f(x) = \sin x$$



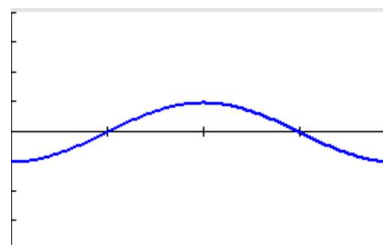
$$f(x) = \cos x$$



$$f(x) = -\sin x$$



$$f(x) = -\cos x$$



**AMPSINFREQXSHIFT**

Amplitude: Distance from the midline to minimum or maximum

Frequency: How many waves from 0 to  $2\pi$

Period: (Wavelength): How long it takes to make one full cycle

Shift: y value of the midline. The average value of the function.

$$Period = \frac{2\pi}{frequency}, Frequency = \frac{2\pi}{period}$$

To graph:

- 1) Use AMPSINFREQXSHIFT to determine the amplitude, sin or cos (+ or -), frequency, and shift/midline.
- 2) Use  $Period = \frac{2\pi}{frequency}$  to find the period.
- 3) Draw in midline and make dashes for max and min on the y axis.
- 4) Make 4 dashes and put the period at the end of the 4<sup>th</sup> dash on the x axis.
- 5) Draw in the appropriate curve.

**Lesson 15: I can practice graphing sinusoidal functions**

Same notes as Lesson 13.

**Lesson 16: I can graph sinusoidal functions with given domains by stretching or shrinking the waves.**

Same notes as lesson 11. If the domain is bigger than the period, you may need to make multiple waves and/or compress them.

**Lesson 17: I can write the equation of sinusoidal functions using AMPSINFREQXSHIFT,**

$$\text{midline} = \frac{\text{min} + \text{max}}{2}, \text{ and } \text{frequency} = \frac{2\pi}{\text{period}}.$$

To write the equation:

- 1) Find midline ( $\frac{\text{min} + \text{max}}{2}$ )
- 2) Determine the period (the x value where the first full wave ends)
- 3) Use  $\text{Frequency} = \frac{2\pi}{\text{period}}$  to determine the frequency
- 4) Substitute all values into AMPSINFREQXSHIFT

\*If multiple choice, cross out incorrect choices using obvious components such as type of wave and midline/shift.

**Lesson 18: I can apply the components of sinusoidal functions in different ways by drawing a little picture.**

Draw a little picture that contains the midline, min, max, and period to give you structure. Same notes as Lessons 11 - 14.

**Lesson 19: I can graph sinusoidal models using AMPSINFREQXSHIFT and drawing a little picture.**

Same notes as Lessons 11-15.

- 1) Graph the wave using AMPSINFREQXSHIFT
- 2) The first follow up question is usually period ( $\frac{2\pi}{\text{frequency}}$ ) and context of the period (the amount of time it takes to complete one full \_\_\_\_\_)
- 3) The second follow up question can be anything. Don't be afraid to use your calculator.

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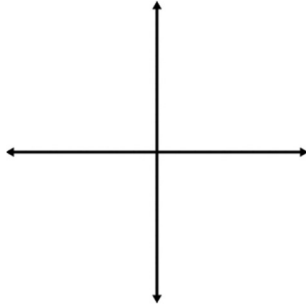
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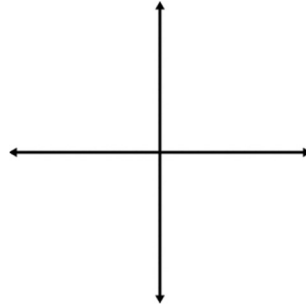
## *Sketching Angles on the Grid*

Sketch each angle on the grid and sketch the reference angle

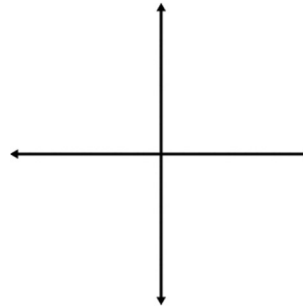
1.  $\theta = 150^\circ$



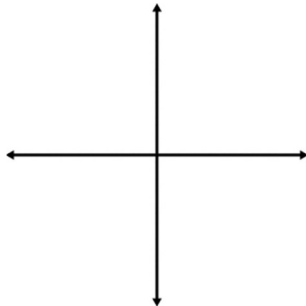
2.  $\theta = 225^\circ$



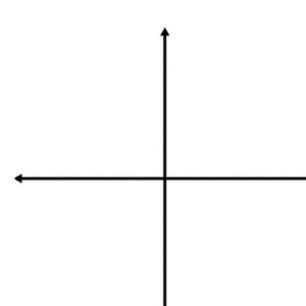
3.  $\theta = 300^\circ$



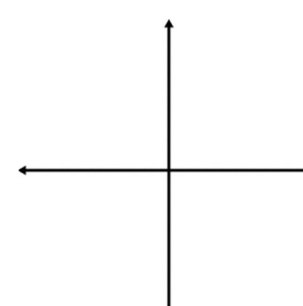
4.  $\theta = 190^\circ$



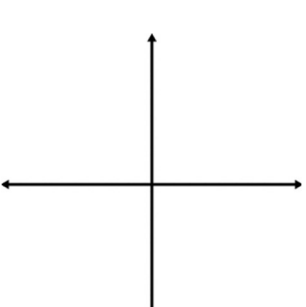
5.  $\theta = 220^\circ$



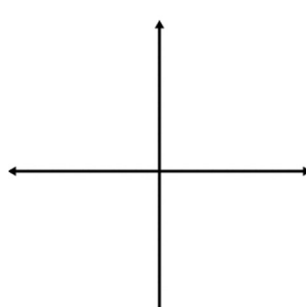
6.  $\theta = 260^\circ$



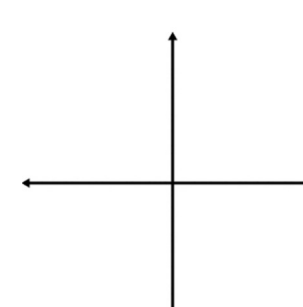
7.  $\theta = 100^\circ$



8.  $\theta = 330^\circ$

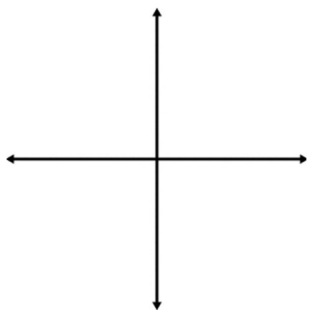


9.  $\theta = 200^\circ$

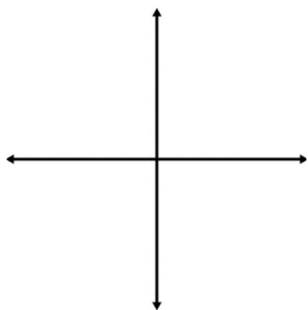




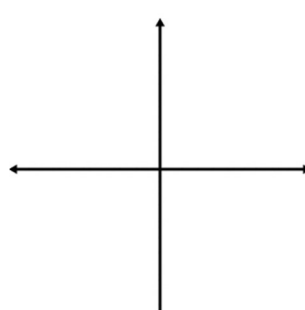
10.  $\theta = 127^\circ$



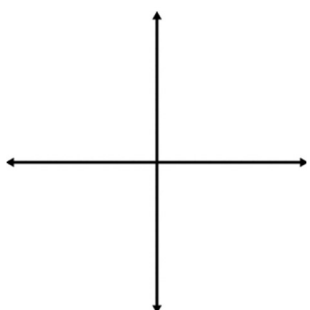
11.  $\theta = 83^\circ$



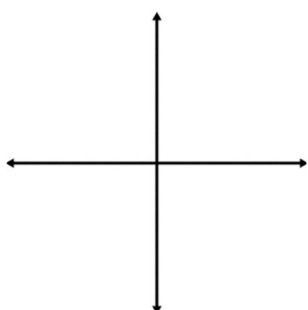
12.  $\theta = 301^\circ$



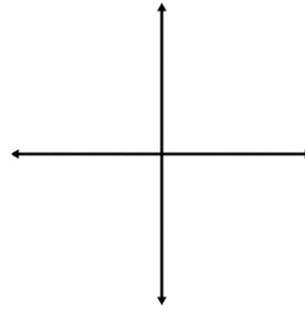
13.  $\theta = 230^\circ$



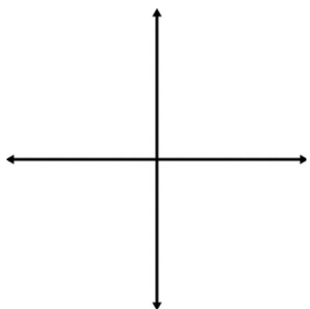
14.  $\theta = 190^\circ$



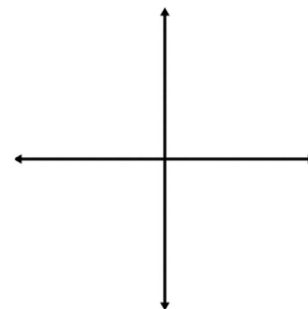
15.  $\theta = 71.6^\circ$



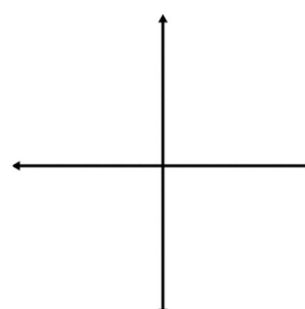
16.  $\theta = 202^\circ$



17.  $\theta = 120^\circ$



18.  $\theta = 312.5^\circ$



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## *Co-terminal Angles*

**For each angle, state two angles that terminate at the same point.**

1.  $120^\circ$

2.  $250^\circ$

3.  $48^\circ$

4.  $311^\circ$

5.  $212^\circ$

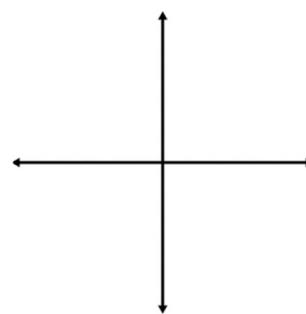
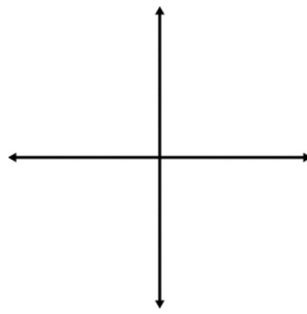
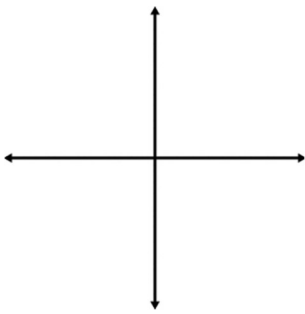
6.  $142^\circ$

**Sketch the following angles and find the reference angle**

7.  $-200^\circ$

8.  $375^\circ$

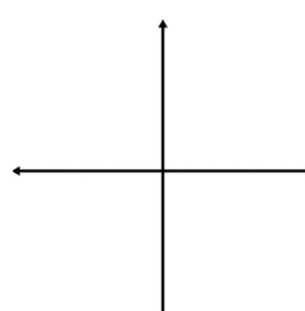
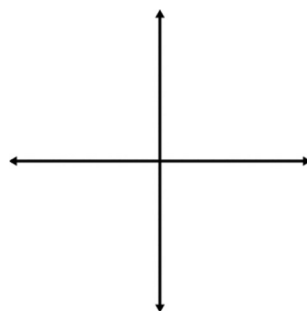
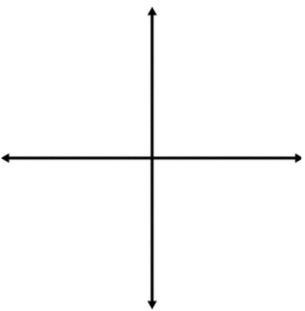
9.  $475^\circ$



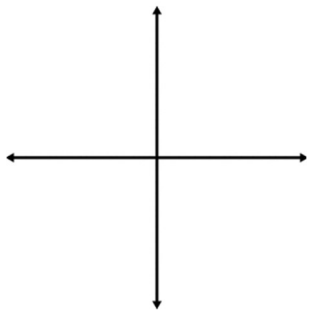
10.  $-120^\circ$

11.  $665^\circ$

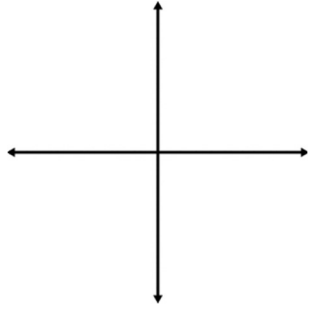
12.  $-302^\circ$



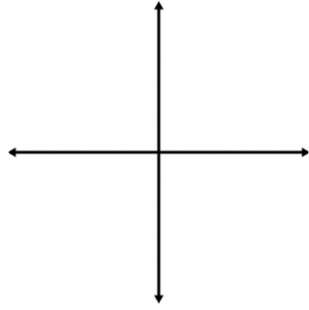
13.  $421^\circ$



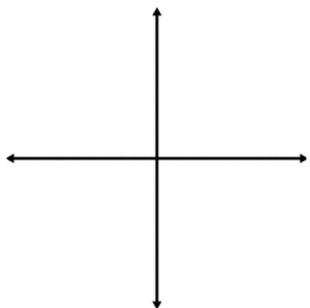
14.  $-279^\circ$



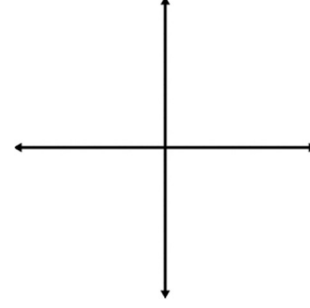
15.  $701^\circ$



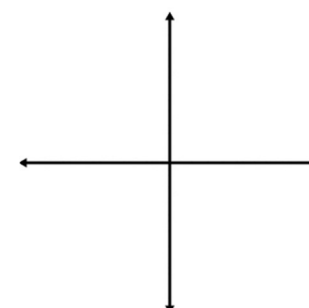
16.  $620^\circ$



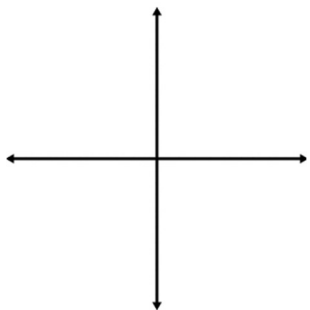
17.  $-305^\circ$



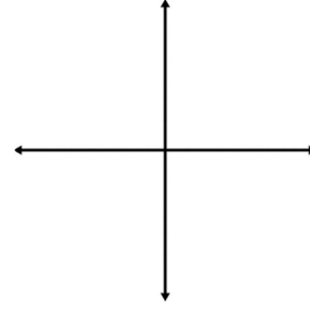
18.  $580^\circ$



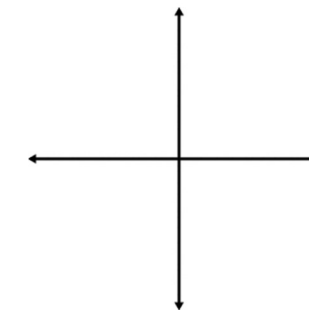
16.  $790^\circ$



17.  $1111^\circ$



18.  $-1060^\circ$



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## *Degrees/ Radians Conversions*

Convert the following from degrees to radians. Leave your answers in terms of  $\pi$ .

1.  $90^\circ$

2.  $30^\circ$

3.  $60^\circ$

4.  $135^\circ$

5.  $150^\circ$

6.  $330^\circ$

7.  $225^\circ$

8.  $330^\circ$

9.  $450^\circ$

10.  $-120^\circ$

11.  $45^\circ$

12.  $-300^\circ$

13.  $67.5^\circ$

14.  $337.5^\circ$

15.  $-420^\circ$

**Convert the following from radians to degrees. Round to the nearest thousandth if necessary**

16.  $\frac{\pi}{4}$  radians

17.  $\frac{3\pi}{2}$  radians

18.  $\frac{12\pi}{4}$  radians

19.  $\frac{6\pi}{5}$  radians

20.  $\frac{2\pi}{5}$  radians

21.  $\frac{4\pi}{3}$  radians

22.  $\frac{3\pi}{8}$  radians

23.  $\frac{\pi}{10}$  radians

24.  $\frac{5\pi}{8}$  radians

25. 4 radians

26. 3 radians

27. 1.5 radians

28. 2.75 radians

29. 3.6 radians

30. 5 radians

31. 5.25 radians

32. 4.8 radians

33. 2.1 radians

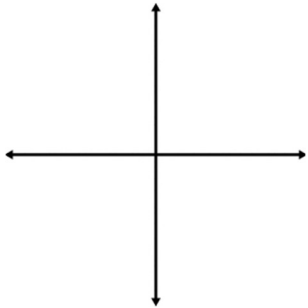
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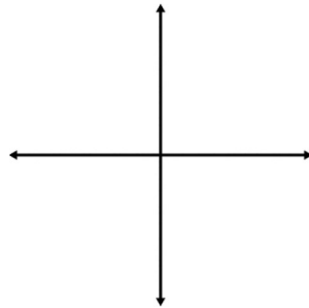


## *Sketching Radian Angles on the Grid*

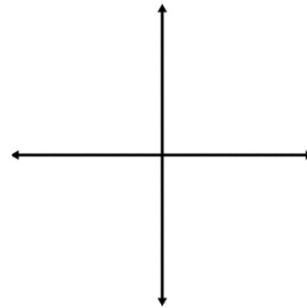
1.  $\theta = \frac{5\pi}{3}$



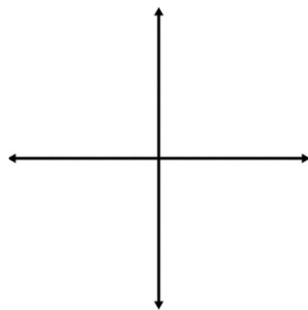
2.  $\theta = \frac{7\pi}{4}$



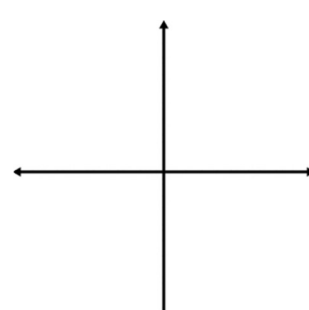
3.  $\theta = \frac{6\pi}{5}$



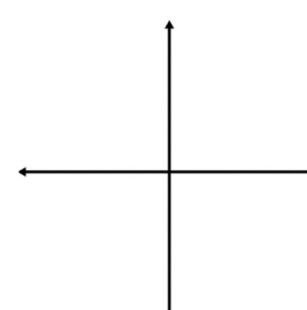
4.  $\theta = 2$



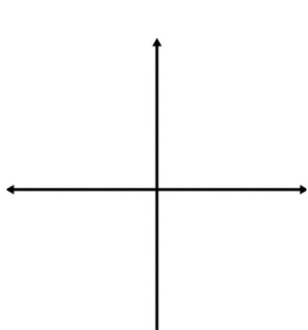
5.  $\theta = 3$



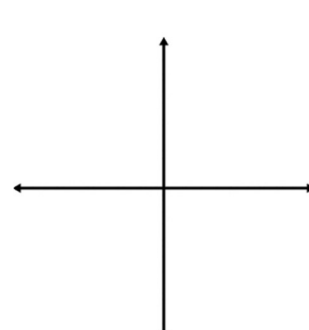
6.  $\theta = 5$



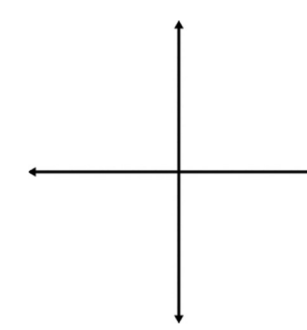
7.  $\theta = 4.1$



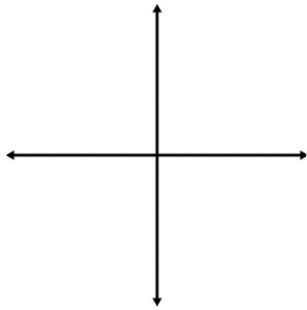
8.  $\theta = 2.7$



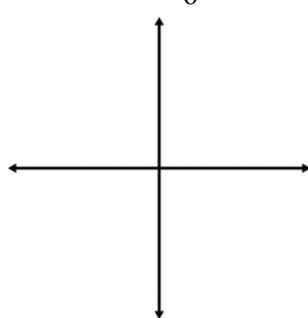
9.  $\theta = 6.1$



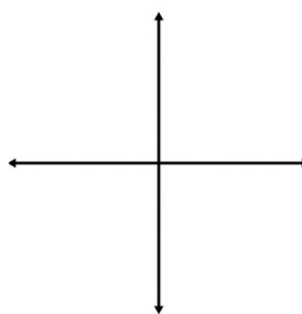
10.  $\theta = 7.2$



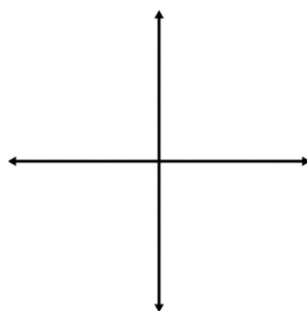
11.  $\theta = -\frac{\pi}{6}$



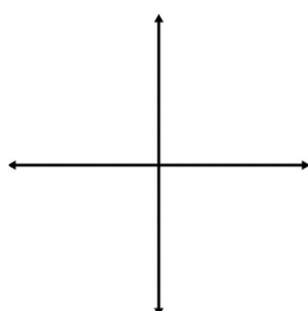
12.  $\theta = 9.2$



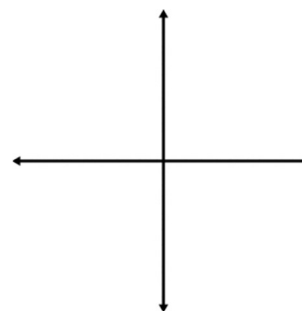
13.  $\theta = -2$



14.  $\theta = 10.4$

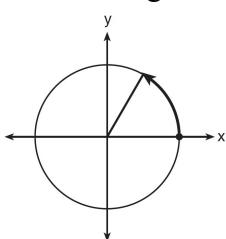


15.  $\theta = -4.3$

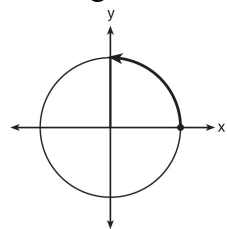


16. Which diagram shows an angle rotation of 1 radian on the unit circle?

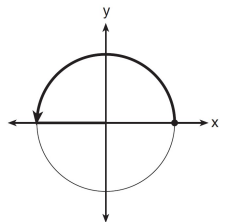
1)



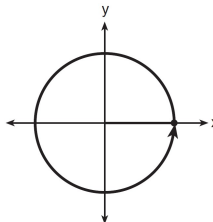
2)



3)

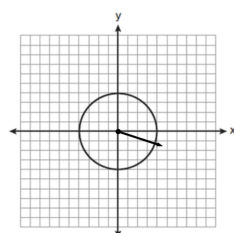


4)

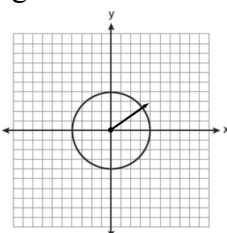


17. Which of the following sketches would represent 6 radians?

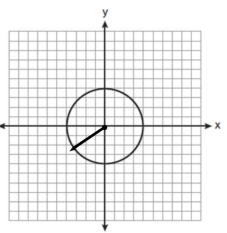
1)



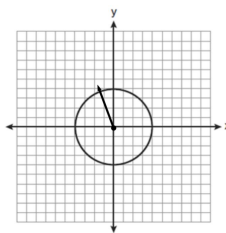
2)



3)

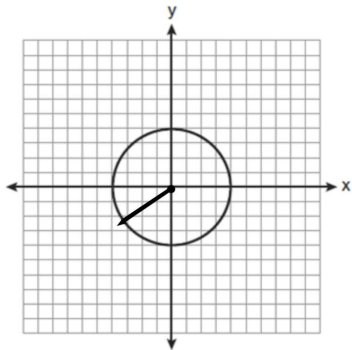


4)



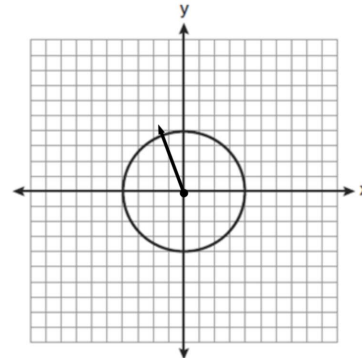
18. Which angle is sketched below?

- 1) 2.4 radians
- 2) 4.5 radians
- 3) 3.8 radians
- 4) 5.2 radians



19. Which angle is sketched below?

- 1) 1 radian
- 2) 1.7 radians
- 3) 3 radians
- 4) 4.1 radians

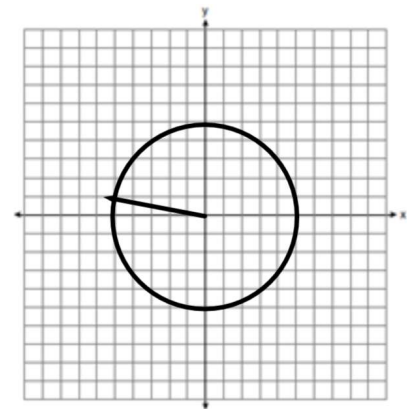


20. Which of the following sketches would represent 3.9 radians?

- 1)
- 2)
- 3)
- 4)

21. Which of the following can be the radian measure of the angle sketched below?

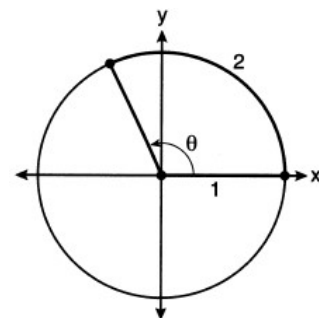
- 1) 1.5
- 2) 3
- 3) 3.8
- 4) 5



22. An angle,  $\theta$ , is rotated counterclockwise on the unit circle, with its terminal side in the second quadrant, as shown in the diagram below.

Which value represents the radian measure of angle  $\theta$ ?

- 1) 1
- 2) 2
- 3) 65.4
- 4) 114.6





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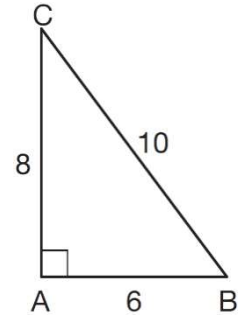
Date \_\_\_\_\_  
Geometry



## Basic Trigonometric Ratios

1. Find the following trigonometric ratios for the given triangle:

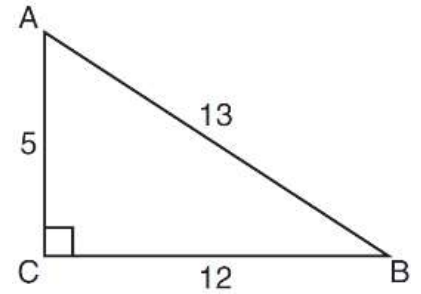
- a)  $\sin B$                       b)  $\cos B$                       c)  $\tan B$



- d)  $\csc B$                       e)  $\sec B$                       f)  $\cot B$

2. Find the following trigonometric ratios for the given triangle:

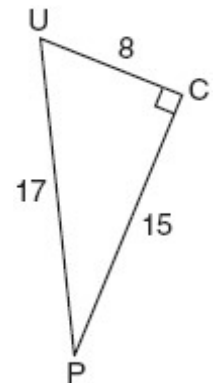
- a)  $\sin A$                       b)  $\cos A$                       c)  $\tan A$



- d)  $\csc A$                       e)  $\sec A$                       f)  $\cot A$

3. Find the following trigonometric ratios for the given triangle:

- a)  $\sin U$                       b)  $\cos U$                       c)  $\tan U$



- d)  $\csc U$                       e)  $\sec U$                       f)  $\cot U$

Name \_\_\_\_\_  
Mr. Schlansky

Date \_\_\_\_\_  
Algebra II



## *Signs of Quadrants*

**In which quadrant does  $\theta$  lie if:**

1.  $\sin \theta > 0, \tan \theta < 0$

2.  $\sin \theta > 0, \tan \theta > 0$

3.  $\cos \theta > 0, \sin \theta < 0$

4.  $\cos \theta < 0, \sin \theta < 0$

5.  $\cos \theta < 0, \tan \theta < 0$

6.  $\tan \theta > 0, \csc \theta < 0$

7.  $\sin \theta < 0, \sec \theta > 0$

8.  $\tan \theta > 0, \sin \theta < 0$

9.  $\cos \theta < 0, \csc \theta > 0$

10.  $\sec \theta < 0, \tan \theta > 0$

11.  $\sin \theta > 0, \sec \theta < 0$

12.  $\tan \theta < 0, \csc \theta > 0$

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Algebra II



## *Evaluating Special Angles*

1.  $\sin(30)$

2.  $\cos\left(\frac{\pi}{4}\right)$

3.  $\tan(60)$

4.  $\cos\left(\frac{5\pi}{6}\right)$

5.  $\sin(120)$

6.  $\tan\left(\frac{3\pi}{4}\right)$

7.  $\tan(210)$

8.  $\sin\left(\frac{5\pi}{4}\right)$

9.  $\cos(240)$

10.  $\cos\left(\frac{11\pi}{6}\right)$

11.  $\sin(315)$

12.  $\tan\left(\frac{5\pi}{3}\right)$

13.  $\cos(120)$

14.  $\tan\left(\frac{3\pi}{4}\right)$

15.  $\sin(300)$

16.  $\tan\left(\frac{5\pi}{6}\right)$

17.  $\cos(315)$

18.  $\cos\left(\frac{7\pi}{6}\right)$

19.  $\sec(30)$

20.  $\csc\left(\frac{\pi}{3}\right)$

21.  $\cot(210)$

22.  $\csc\left(\frac{3\pi}{4}\right)$

23.  $\cot(300)$

24.  $\sec\left(\frac{5\pi}{6}\right)$

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Algebra II



## *Evaluating Special Angles Multiple Choice*

1. What is the exact value of  $\cos\left(\frac{5\pi}{6}\right)$ ?

1)  $\frac{\sqrt{3}}{2}$

3)  $-\frac{\sqrt{3}}{2}$

2)  $\frac{1}{2}$

4)  $-\frac{1}{2}$

2. What is the exact value of  $\tan\left(\frac{3\pi}{4}\right)$ ?

1) 1

2) -1

3)  $\sqrt{3}$

4)  $-\sqrt{3}$

3. What is the exact value of  $\cos\left(-\frac{5\pi}{6}\right)$ ?

1)  $\frac{\sqrt{3}}{2}$

3)  $-\frac{\sqrt{3}}{2}$

2)  $\frac{1}{2}$

4)  $-\frac{\sqrt{2}}{2}$

4. The exact value of  $\sin\left(\frac{8\pi}{3}\right)$  is

1)  $\frac{1}{2}$

2)  $-\frac{1}{2}$

3)  $-\frac{\sqrt{3}}{2}$

4)  $\frac{\sqrt{3}}{2}$

5. What is the exact value of  $\sec\left(\frac{2\pi}{3}\right)$ ?

1) -2

3) 2

2)  $-\frac{2\sqrt{3}}{3}$

4)  $\frac{2\sqrt{3}}{3}$

6. What is the exact value of  $\cot\left(\frac{5\pi}{3}\right)$ ?

1)  $\frac{1}{\sqrt{3}}$

3)  $\sqrt{3}$

2)  $-\frac{1}{\sqrt{3}}$

4)  $-\sqrt{3}$

7. What is the exact value of  $\csc\left(-\frac{7\pi}{4}\right)$ ?

1)  $-\frac{2\sqrt{3}}{3}$

3)  $-\frac{\sqrt{2}}{2}$

2)  $\sqrt{2}$

4)  $\frac{\sqrt{2}}{2}$

8. What is the exact value of  $\cot\left(-\frac{\pi}{3}\right)$ ?

1)  $-\frac{\sqrt{3}}{3}$

3)  $\frac{\sqrt{3}}{3}$

2)  $-\sqrt{3}$

4)  $\sqrt{3}$

9. What is the exact value of  $\cos\left(\frac{3\pi}{4}\right)$ ?

1)  $\frac{\sqrt{3}}{2}$

3)  $-\frac{\sqrt{3}}{2}$

2)  $\frac{\sqrt{2}}{2}$

4)  $-\frac{\sqrt{2}}{2}$

10. What is the exact value of  $\tan\left(-\frac{5\pi}{6}\right)$ ?

1)  $\frac{1}{\sqrt{3}}$

3)  $\sqrt{3}$

2)  $-\frac{1}{\sqrt{3}}$

4)  $-\sqrt{3}$

11. The value of  $\cos\left(-\frac{\pi}{4}\right)$  is equivalent to

1)  $\frac{\sqrt{3}}{2}$

3)  $-\frac{\sqrt{3}}{2}$

2)  $\frac{\sqrt{2}}{2}$

4)  $-\frac{\sqrt{2}}{2}$

12. The value of  $\cos\left(\frac{5\pi}{6}\right)$

1)  $\sec\left(\frac{5\pi}{6}\right)$

3)  $\tan\left(\frac{5\pi}{4}\right)$

2)  $\sin\left(\frac{4\pi}{3}\right)$

4)  $\sin\left(\frac{2\pi}{3}\right)$

13. The value of  $\sin\left(\frac{2\pi}{3}\right)$  is equivalent to

1)  $\sin\left(\frac{4\pi}{3}\right)$

3)  $\tan\left(\frac{\pi}{3}\right)$

2)  $\cos\left(\frac{\pi}{6}\right)$

4)  $\csc\left(\frac{2\pi}{3}\right)$

14. The value of  $\tan\left(\frac{\pi}{4}\right)$  is equivalent to

1)  $\cot\left(-\frac{\pi}{4}\right)$

3)  $\tan\left(\frac{3\pi}{4}\right)$

2)  $\cot\left(-\frac{3\pi}{4}\right)$

4)  $\tan\left(\frac{5\pi}{6}\right)$

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Pre Calculus



## *The Unit Circle*

**Find the exact value of the coordinate on the unit circle for each of the following**

1.  $\theta = 30^\circ$

2.  $\theta = \frac{\pi}{3}$

3.  $\theta = 45^\circ$

4.  $\theta = \frac{5\pi}{3}$

5.  $\theta = 300^\circ$

6.  $\theta = \frac{7\pi}{6}$

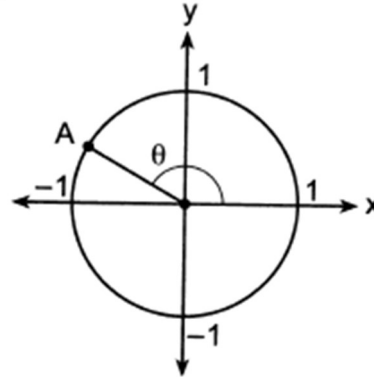
7.  $\theta = 330^\circ$

8.  $\theta = \frac{5\pi}{4}$

9.  $\theta = 120^\circ$



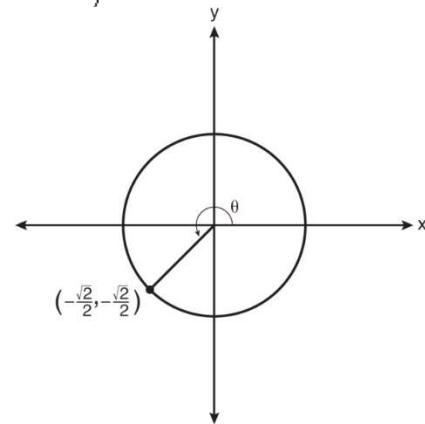
10. In the diagram of a unit circle below, point  $A$ ,  $\left(-\frac{\sqrt{3}}{2}, \frac{1}{2}\right)$ , represents the point where the terminal side of  $\theta$  intersects the unit circle.



What is  $m\angle\theta$ ?

- 1)  $30^\circ$
- 2)  $120^\circ$
- 3)  $135^\circ$
- 4)  $150^\circ$

11. In the diagram below of a unit circle, the ordered pair  $\left(-\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}\right)$  represents the point where the terminal side of  $\theta$  intersects the unit circle.



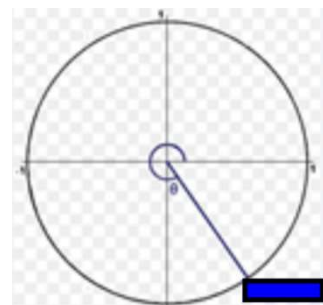
What is  $m\angle\theta$ ?

- 1)  $\frac{\pi}{4}$
- 2)  $\frac{3\pi}{4}$
- 3)  $\frac{5\pi}{4}$
- 4)  $\frac{4\pi}{3}$

12. In the diagram of a unit circle below, a point on the unit circle as coordinates  $\left(\frac{1}{2}, -\frac{\sqrt{3}}{2}\right)$ .

What is  $m\angle\theta$ ?

- 1)  $300^\circ$
- 2)  $315^\circ$
- 3)  $240^\circ$
- 4)  $330^\circ$



## Pythagorean Theorem

Look out for hidden right triangles where you may need to use  $a^2 + b^2 = c^2$

$a$  and  $b$  are the legs

$c$  is the hypotenuse

Know your Pythagorean Triples!

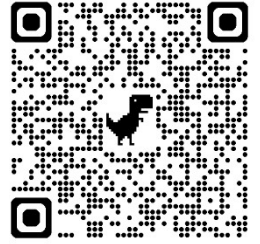
3,4,5

5,12,13

7,24,25

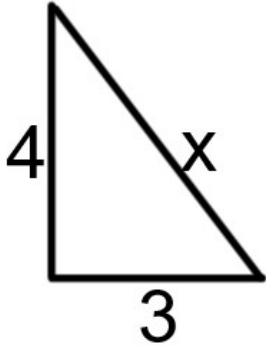
8,15,17

9,40,41

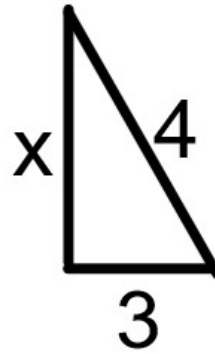


Find the missing side of each right triangle rounding to the nearest tenth

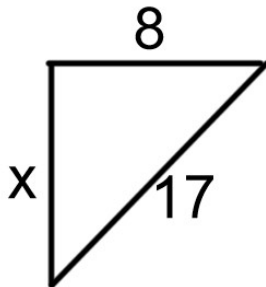
1.



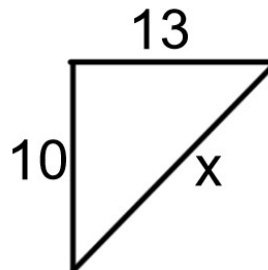
2.



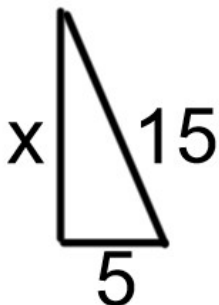
3.



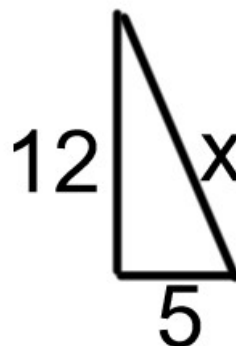
4.



5.



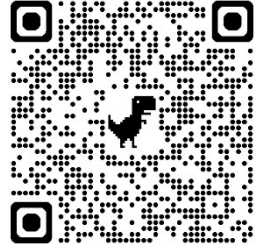
6.



## Rationalizing the Denominator

To rationalize the denominator, multiply top and bottom by the radical

When multiplying a radical by itself, the radical cancels out



### Rationalize the following denominators

1.  $\frac{2}{\sqrt{5}}$

2.  $\frac{-7}{\sqrt{11}}$

3.  $\frac{3}{\sqrt{2}}$

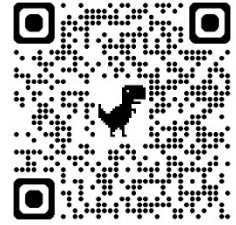
4.  $\frac{6}{\sqrt{3}}$

5.  $\frac{4}{\sqrt{6}}$

6.  $\frac{-5}{\sqrt{10}}$

Name \_\_\_\_\_  
Mr. Schlansky

Date \_\_\_\_\_  
Algebra II



## *Advanced Trig Ratios*

1. If  $\cos \theta = \frac{12}{13}$  and  $\theta$  is in Quadrant I, find:

a)  $\cos \theta$

b)  $\sin \theta$

c)  $\tan \theta$

d)  $\sec \theta$

e)  $\csc \theta$

f)  $\cot \theta$

2. If  $\sin \theta = -\frac{3}{5}$  and  $\theta$  is in Quadrant III, find:

a)  $\cos \theta$

b)  $\sin \theta$

c)  $\tan \theta$

d)  $\sec \theta$

e)  $\csc \theta$

f)  $\cot \theta$

3. If  $\tan \theta = \frac{24}{7}$  and  $\theta$  is in Quadrant III, find:

a)  $\cos \theta$

b)  $\sin \theta$

c)  $\tan \theta$

d)  $\sec \theta$

e)  $\csc \theta$

f)  $\cot \theta$

4. If  $\sin \theta = \frac{5}{8}$  and  $\theta$  is in Quadrant II, find:

a)  $\cos \theta$

b)  $\sin \theta$

c)  $\tan \theta$

d)  $\sec \theta$

e)  $\csc \theta$

f)  $\cot \theta$

5. Angle  $\theta$  is in standard position and  $(3, 4)$  is a point on the terminal side of  $\theta$ . Find:

a)  $\cos \theta$

b)  $\sin \theta$

c)  $\tan \theta$

d)  $\sec \theta$

e)  $\csc \theta$

f)  $\cot \theta$

6. Angle  $\theta$  is in standard position and  $(4, -7)$  is a point on the terminal side of  $\theta$ . Find:

a)  $\cos \theta$

b)  $\sin \theta$

c)  $\tan \theta$

d)  $\sec \theta$

e)  $\csc \theta$

f)  $\cot \theta$

7. Angle  $\theta$  is in standard position and  $(-5, -12)$  is a point on the terminal side of  $\theta$ . Find:

a)  $\cos \theta$

b)  $\sin \theta$

c)  $\tan \theta$

d)  $\sec \theta$

e)  $\csc \theta$

f)  $\cot \theta$

8. Angle  $\theta$  is in standard position and  $(-2, 3)$  is a point on the terminal side of  $\theta$ . Find:

a)  $\cos \theta$

b)  $\sin \theta$

c)  $\tan \theta$

d)  $\sec \theta$

e)  $\csc \theta$

f)  $\cot \theta$

9. A circle centered at the origin has a radius of 10 units. The terminal side of an angle,  $\theta$ , intercepts the circle in Quadrant I at point  $C$ . The  $y$ -coordinate of point  $C$  is 8. Find:

a)  $\cos \theta$

b)  $\sin \theta$

c)  $\tan \theta$

d)  $\sec \theta$

e)  $\csc \theta$

f)  $\cot \theta$

10. A circle centered at the origin has a radius of 4 units. The terminal side of an angle,  $\theta$ , intercepts the circle in Quadrant II at point  $P$ . The  $x$ -coordinate of point  $P$  is 2. Find:

a)  $\cos \theta$

b)  $\sin \theta$

c)  $\tan \theta$

d)  $\sec \theta$

e)  $\csc \theta$

f)  $\cot \theta$



11. A circle centered at the origin has a radius of 6 units. The terminal side of an angle,  $\theta$ , intercepts the circle in Quadrant VI at point  $P$ . The  $x$ -coordinate of point  $P$  is 2. Find:

a)  $\cos \theta$

b)  $\sin \theta$

c)  $\tan \theta$

d)  $\sec \theta$

e)  $\csc \theta$

f)  $\cot \theta$

12. A circle centered at the origin has a radius of 9 units. The terminal side of an angle,  $\theta$ , intercepts the circle in Quadrant II at point  $P$ . The  $x$ -coordinate of point  $P$  is 7. Find:

a)  $\cos \theta$

b)  $\sin \theta$

c)  $\tan \theta$

d)  $\sec \theta$

e)  $\csc \theta$

f)  $\cot \theta$

13. The point  $\left(\frac{3}{5}, -\frac{4}{5}\right)$  lies on the unit circle. Find:

a)  $\cos \theta$

b)  $\sin \theta$

c)  $\tan \theta$

d)  $\sec \theta$

e)  $\csc \theta$

f)  $\cot \theta$

14. The point  $\left(x, -\frac{2}{3}\right)$  lies on the unit circle where  $x > 0$ . Find:

a)  $\cos \theta$

b)  $\sin \theta$

c)  $\tan \theta$

d)  $\sec \theta$

e)  $\csc \theta$

f)  $\cot \theta$

Name \_\_\_\_\_  
Mr. Schlansky

Date \_\_\_\_\_  
Algebra II



## *Advanced Trig Ratios Regents Practice*

1. If  $\cos \theta = -\frac{3}{4}$  and  $\theta$  is in Quadrant III, then  $\sin \theta$  is equivalent to

- 1)  $-\frac{\sqrt{7}}{4}$                       3)  $-\frac{5}{4}$   
2)  $\frac{\sqrt{7}}{4}$                         4)  $\frac{5}{4}$

2. If the terminal side of angle  $\theta$ , in standard position, passes through point  $(-4, 3)$ , what is the numerical value of  $\sin \theta$ ?

- 1)  $\frac{3}{5}$                       3)  $-\frac{3}{5}$   
2)  $\frac{4}{5}$                       4)  $-\frac{4}{5}$

3. A circle centered at the origin has a radius of 10 units. The terminal side of an angle,  $\theta$ , intercepts the circle in Quadrant II at point  $C$ . The  $y$ -coordinate of point  $C$  is 8. What is the value of  $\cos \theta$ ?

- 1)  $-\frac{3}{5}$                       3)  $\frac{3}{5}$   
2)  $-\frac{3}{4}$                       4)  $\frac{4}{5}$

4. Given  $\cos \theta = \frac{7}{25}$ , where  $\theta$  is an angle in standard position terminating in quadrant IV, and  $\sin^2 \theta + \cos^2 \theta = 1$ , what is the value of  $\tan \theta$ ?

- 1)  $-\frac{24}{25}$                       3)  $\frac{24}{25}$   
2)  $-\frac{24}{7}$                         4)  $\frac{24}{7}$

5. Given that  $\sin^2 \theta + \cos^2 \theta = 1$  and  $\sin \theta = -\frac{\sqrt{2}}{5}$ , what is a possible value of  $\cos \theta$ ?

- 1)  $\frac{5 + \sqrt{2}}{5}$                       3)  $\frac{3\sqrt{3}}{5}$   
2)  $\frac{\sqrt{23}}{5}$                         4)  $\frac{\sqrt{35}}{5}$

6. Given  $\cos A = \frac{3}{\sqrt{10}}$  and  $\cot A = -3$ , determine the value of  $\sin A$  in radical form.

7. An angle,  $\theta$ , is in standard position and its terminal side passes through the point  $(2, -1)$ . Find the *exact* value of  $\sin \theta$ .

8. A circle centered at the origin has a radius of 4 units. The terminal side of an angle,  $\theta$ , intercepts the circle in Quadrant III at point  $P$ . The  $x$ -coordinate of point  $P$  is 2. What is the value of  $\cos \theta$ ?

9. The terminal side of  $\theta$ , an angle in standard position, intersects the unit circle at  $P\left(-\frac{1}{3}, -\frac{\sqrt{8}}{3}\right)$ .

What is the value of  $\sec \theta$ ?

1)  $-3$

3)  $-\frac{1}{3}$

2)  $-\frac{3\sqrt{8}}{8}$

4)  $-\frac{\sqrt{8}}{3}$

10. Point  $M\left(t, \frac{4}{7}\right)$  is located in the second quadrant on the unit circle. Determine the exact value of  $t$ .

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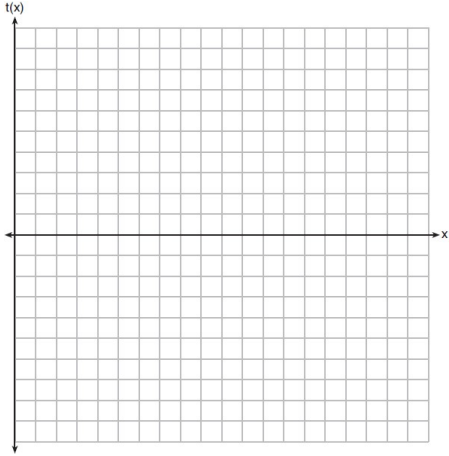
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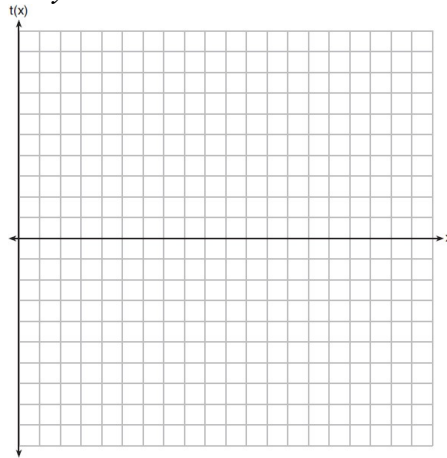
## Graphing Sinusoidal Curves

Graph one full wave of the following trigonometric functions

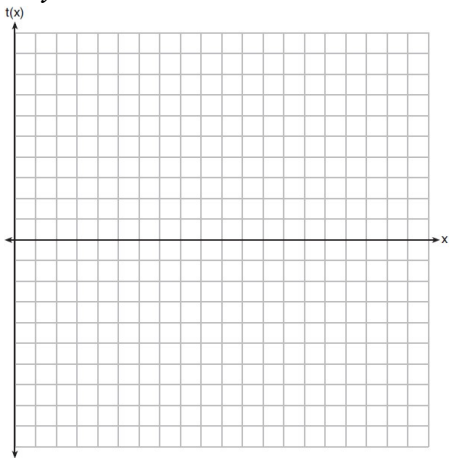
1.  $y = 3 \sin 2x - 1$



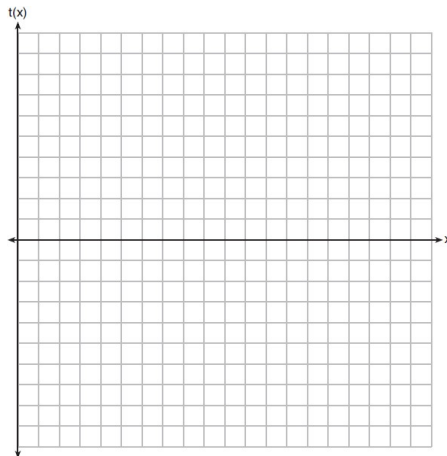
2.  $y = 2 \cos 4x + 3$



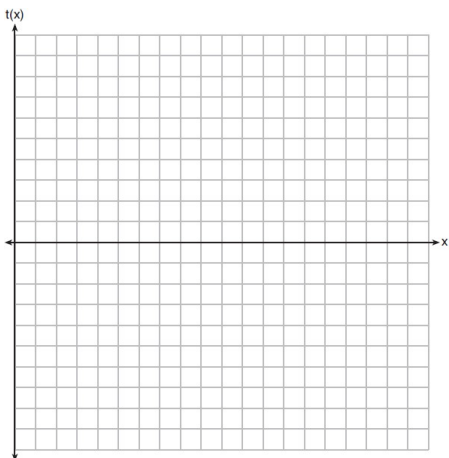
3.  $y = -3 \sin \pi x + 2$



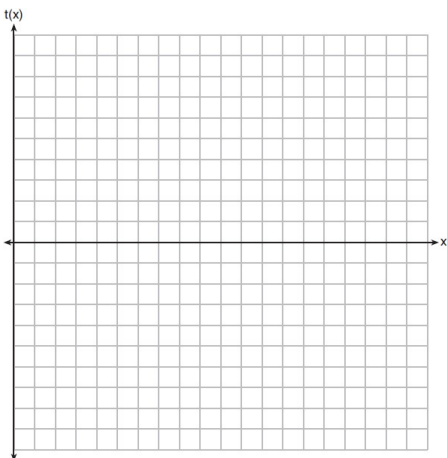
4.  $y = -4 \cos 2\pi x - 2$



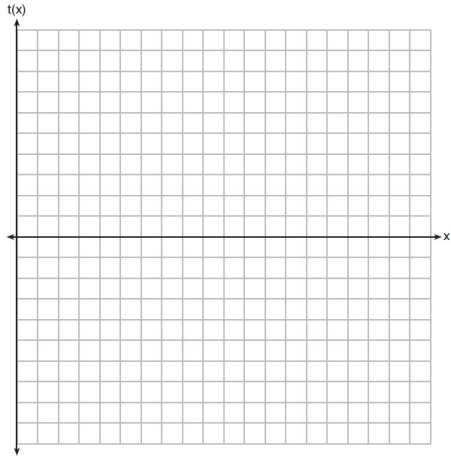
5.  $y = 6 \sin 2x - 1$



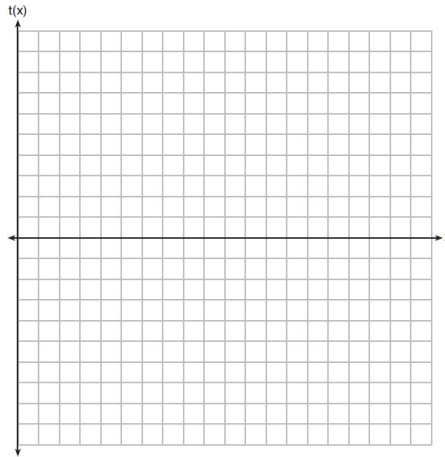
6.  $y = -2 \cos 3x + 3$



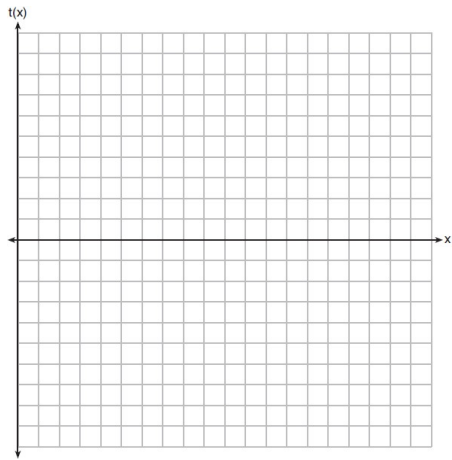
$$7. y = -4 \sin \frac{1}{2} x + 2$$



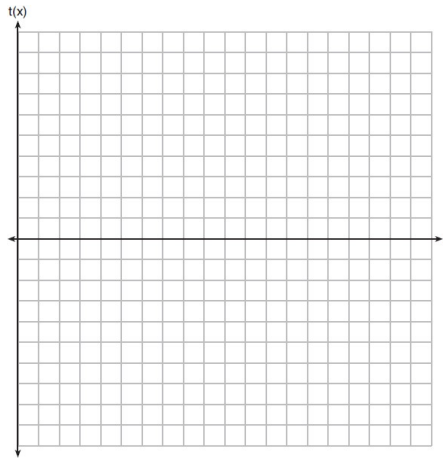
$$8. y = -5 \cos \frac{1}{3} x + 3$$



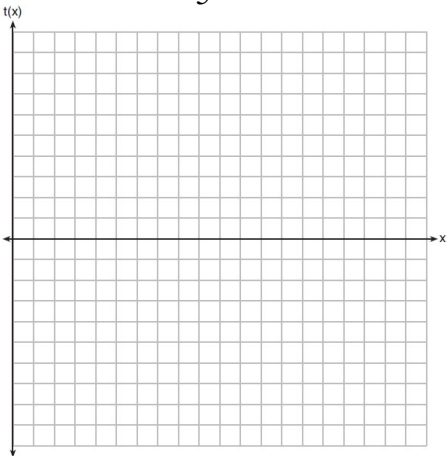
$$9. y = 3 \sin \frac{2}{3} x - 2$$



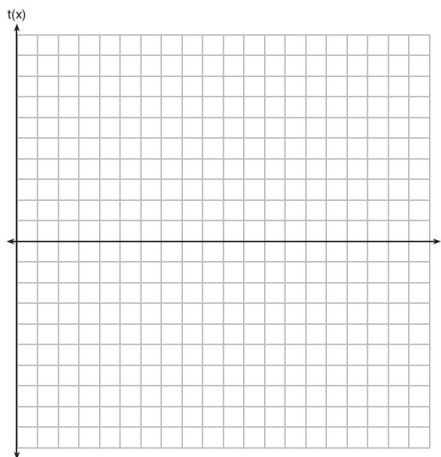
$$10. y = -3 \cos \frac{\pi}{3} x + 1$$



$$11. y = -6 \sin \frac{1}{5} x + 2$$



$$12. y = -5 \sin \frac{\pi}{6} x + 2$$





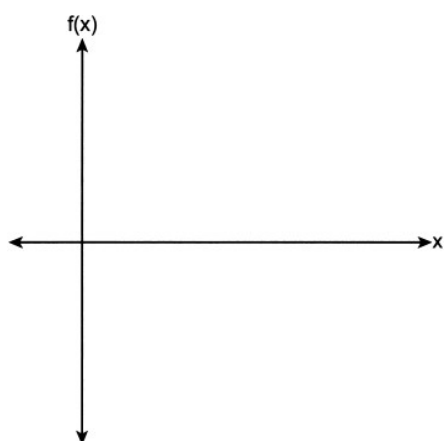
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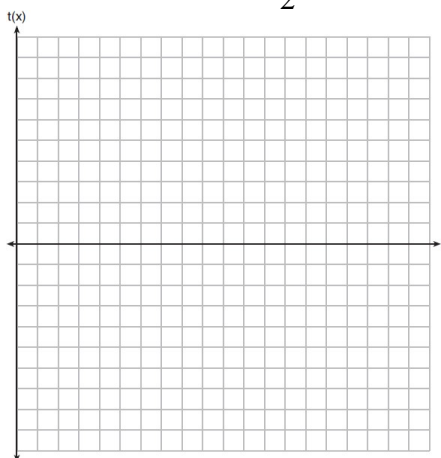
## Graphing Sinusoidal Curves Practice

Graph one full wave of the following trigonometric functions and state the domain and range.

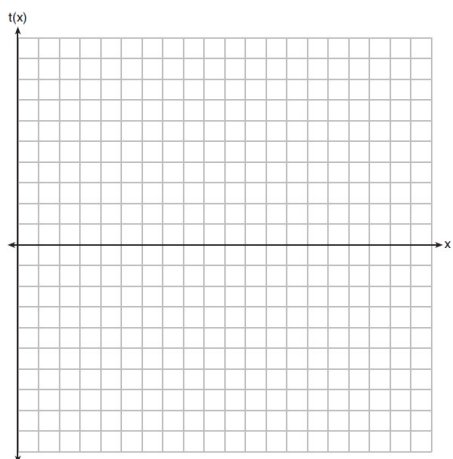
1.  $f(x) = 3 \sin 2x + 1$



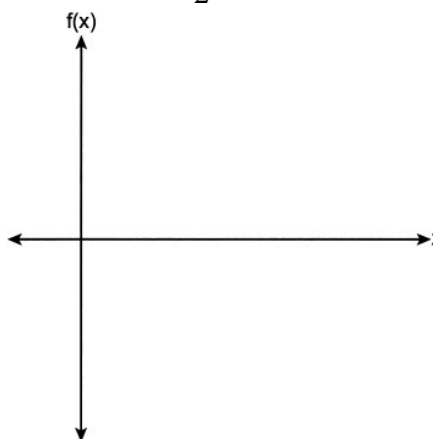
2.  $y = -2 \cos \frac{1}{2}x$



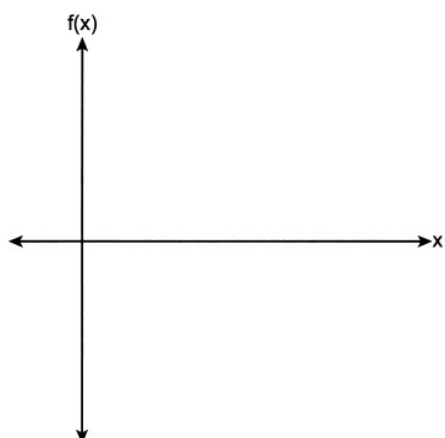
3.  $y = 3 \cos 4x + 2$



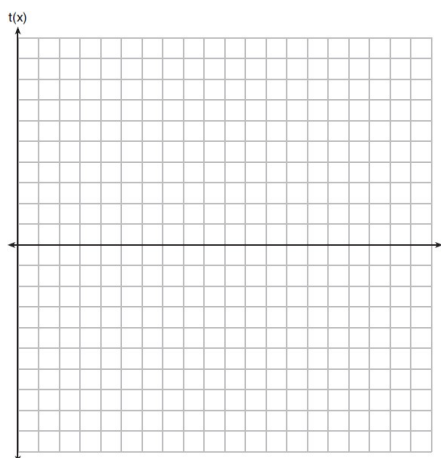
4.  $y = -2 \sin \frac{1}{2}x - 1$



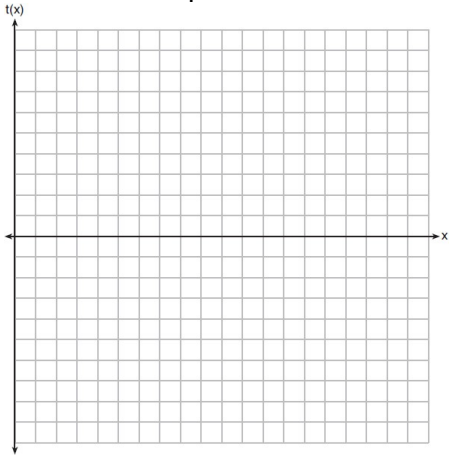
5.  $y = 2 \cos 4x - 3$



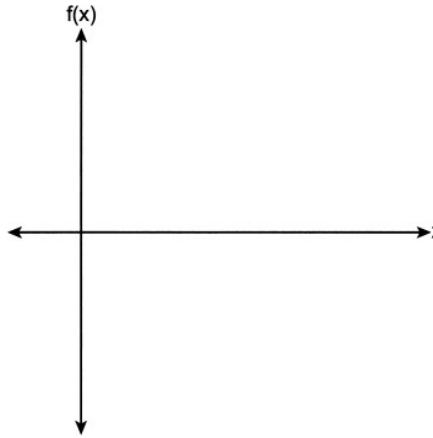
6.  $y = \frac{1}{2} \sin 2x - 4$



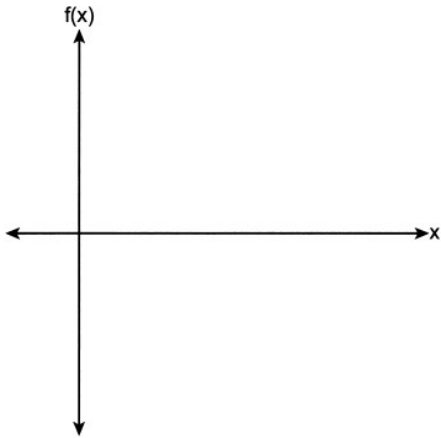
7.  $y = -4 \cos \frac{\pi}{4} x + 1$



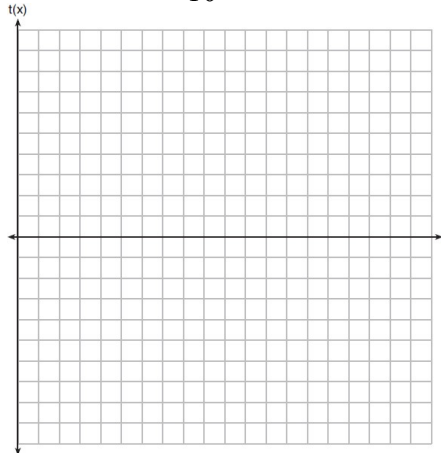
8.  $y = 3 \sin \frac{\pi}{2} x + 2$



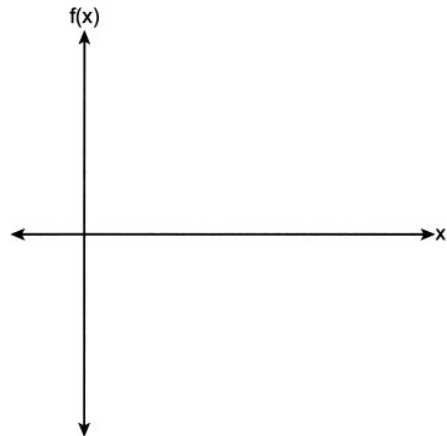
9.  $y = -4 \sin \frac{2\pi}{5} x + 2$



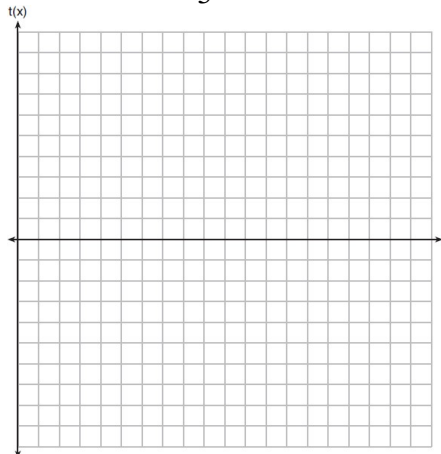
10.  $y = 3 \cos \frac{\pi}{10} x - 4$



11.  $y = -3 \cos \frac{\pi}{6} x + 1$



12.  $y = 2 \sin \frac{2\pi}{3} x - 1$







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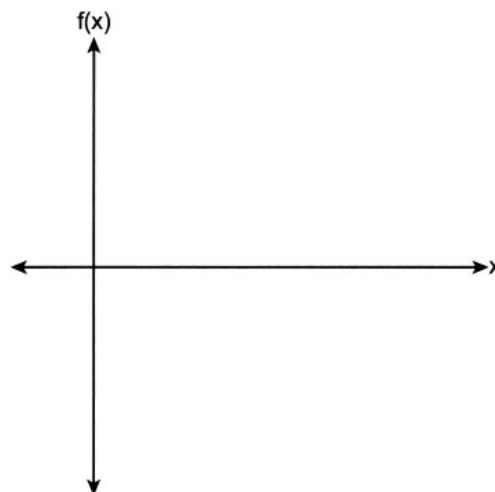
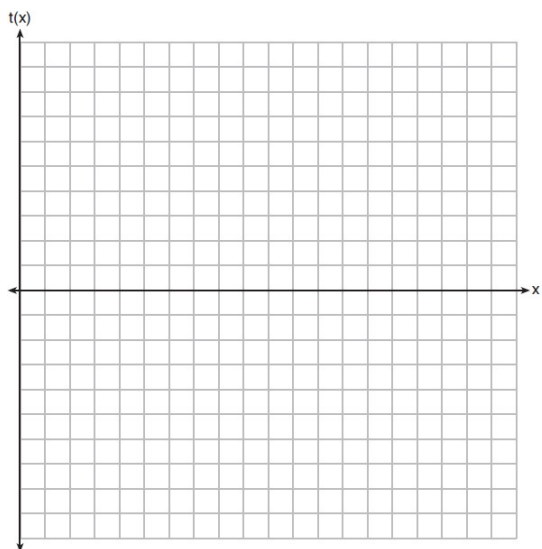
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## *Graphing Sinusoidal Curves Over Given Domains*

Graph the following two functions over the domain  $[0, 2\pi]$  on the set of axes below.

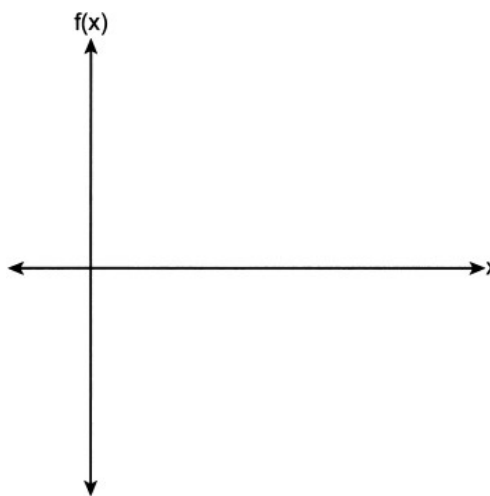
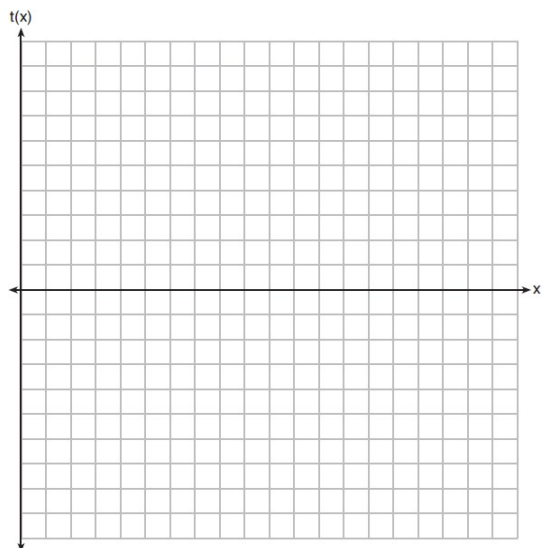
1.  $t(x) = 3 \sin(2x) + 2$

2.  $y = -2 \cos \frac{1}{2}x + 1$



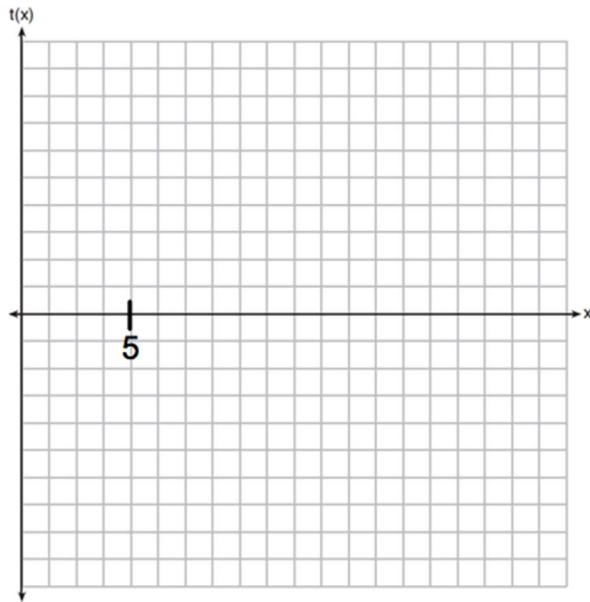
3.  $y = -2 \sin 4x + 3$

4.  $y = 3 \cos \frac{1}{2}x - 5$



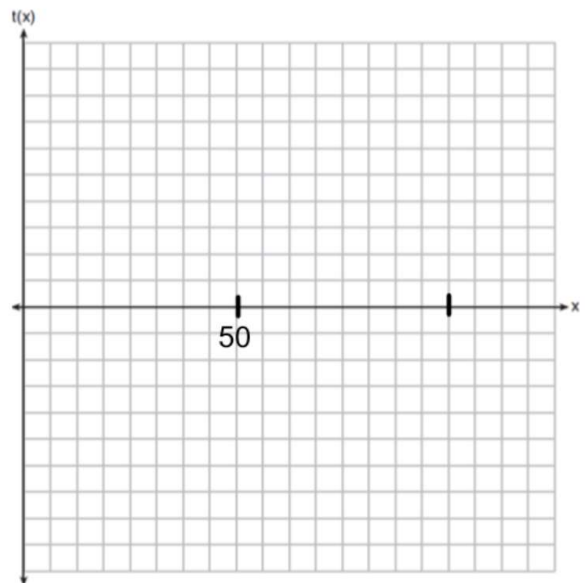
5. On the set of axes below, graph

$$y = 3 \cos \frac{2\pi}{5} x - 2 \text{ over the domain } [0, 10]$$



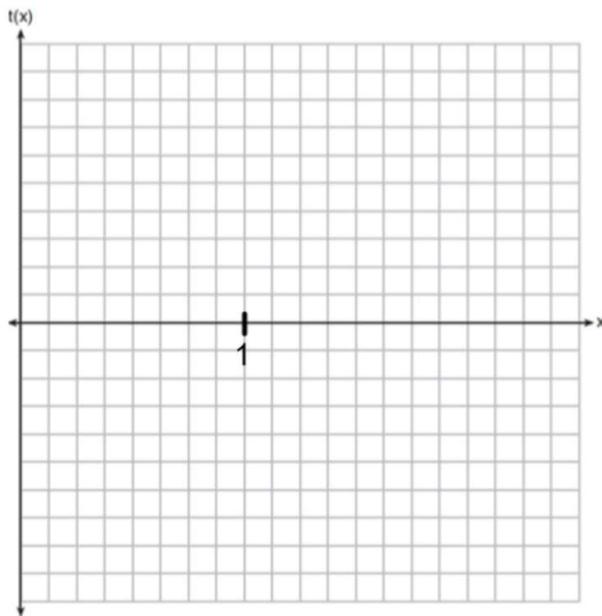
6. On the set of axes below, graph

$$y = -2 \sin \frac{\pi}{50} x + 1 \text{ over the domain } [0, 100]$$



7. On the set of axes below, graph

$$y = 3 \sin 4\pi x - 2 \text{ over the domain } [0, 2]$$

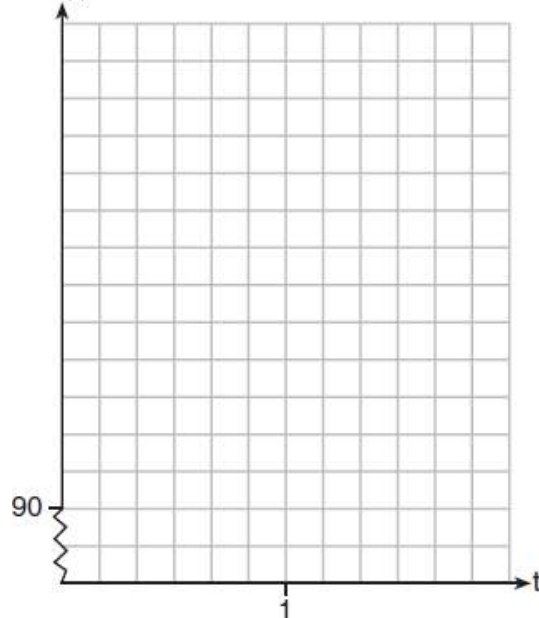


8. On the set of axes below, graph

$$P(t) = 24 \cos(3\pi t) + 120 \text{ over the domain}$$

$$0 \leq t \leq 2.$$

$P(t)$



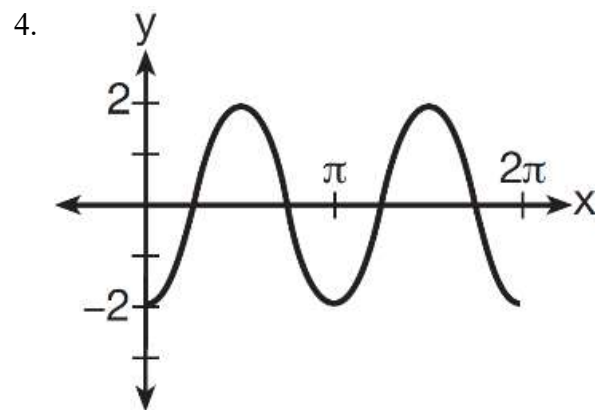
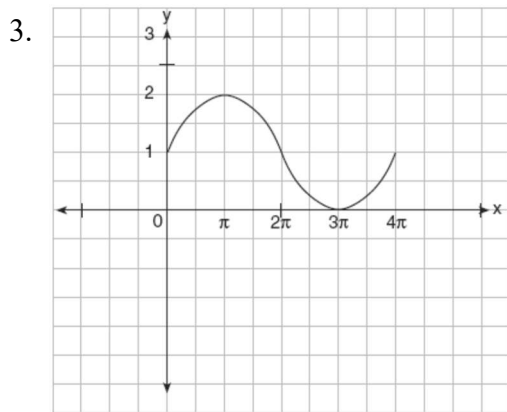
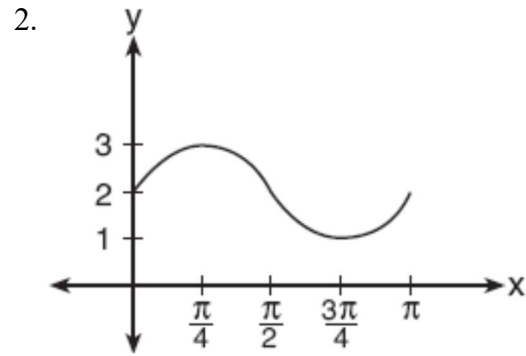
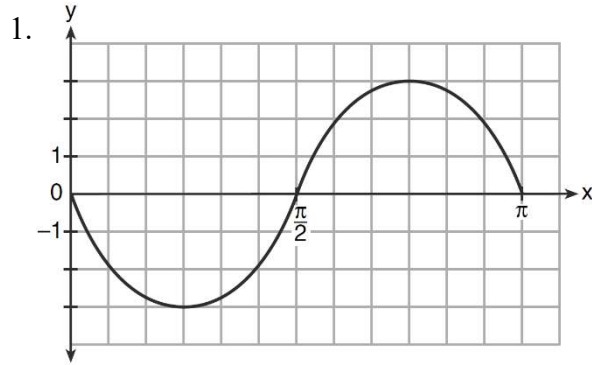
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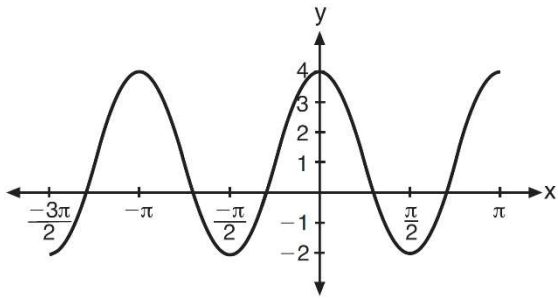


## Writing Equations of Sinusoidal Graphs

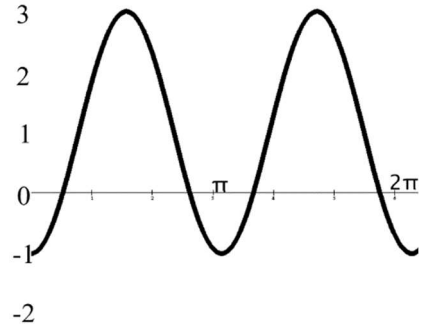
Write an equation for the graph of the trigonometric functions shown below.



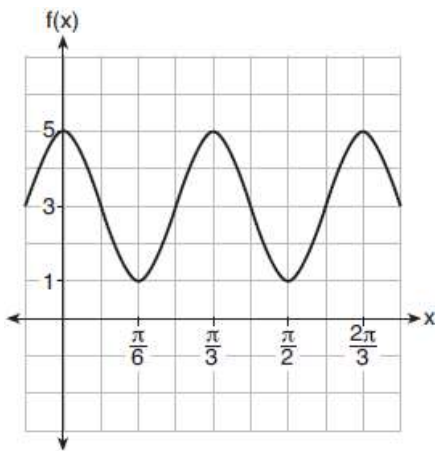
5.



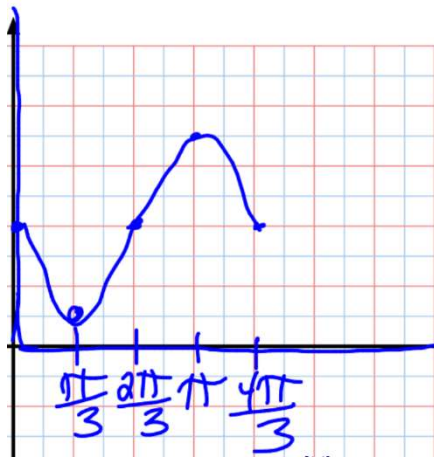
6.



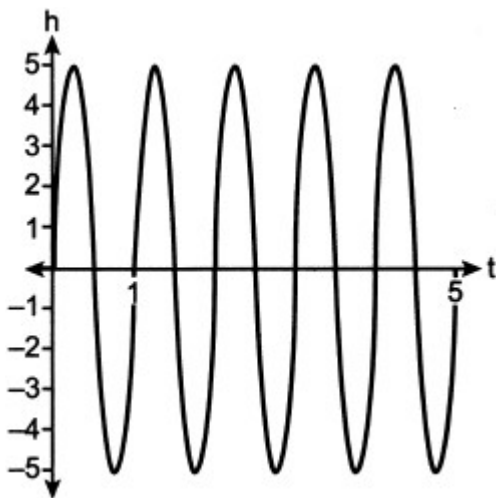
7.



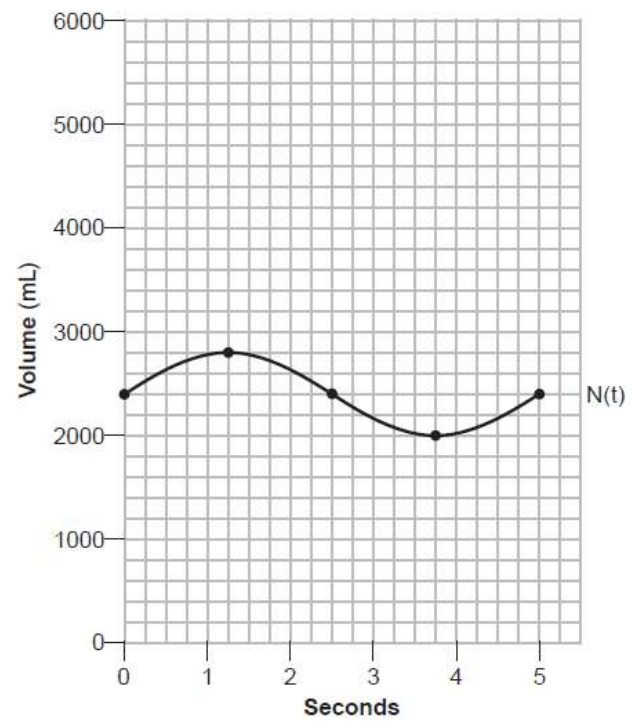
8.



9.



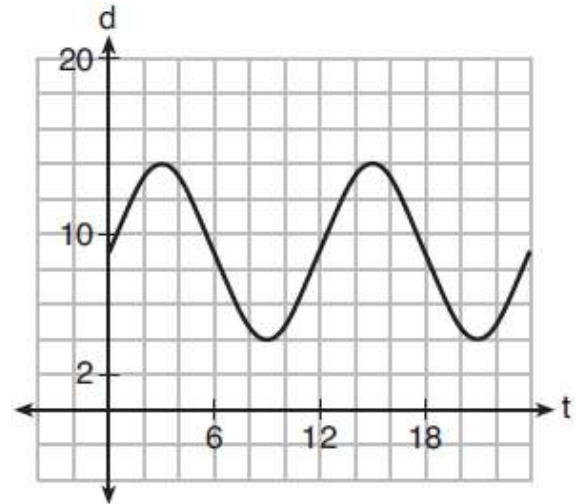
10.



11. The depth of the water at a marker 20 feet from the shore in a bay is depicted in the graph below.

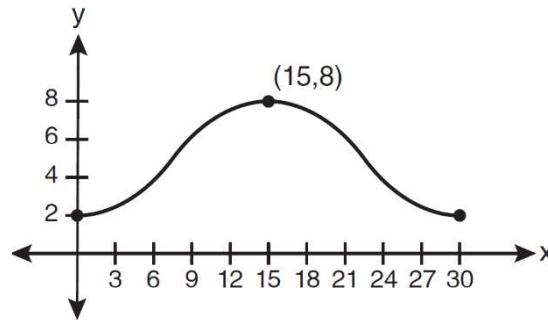
If the depth,  $d$ , is measured in feet and time,  $t$ , is measured in hours since midnight, what is an equation for the depth of the water at the marker?

- 1)  $d = 5 \cos\left(\frac{\pi}{6}t\right) + 9$
- 2)  $d = 9 \cos\left(\frac{\pi}{6}t\right) + 5$
- 3)  $d = 9 \sin\left(\frac{\pi}{6}t\right) + 5$
- 4)  $d = 5 \sin\left(\frac{\pi}{6}t\right) + 9$



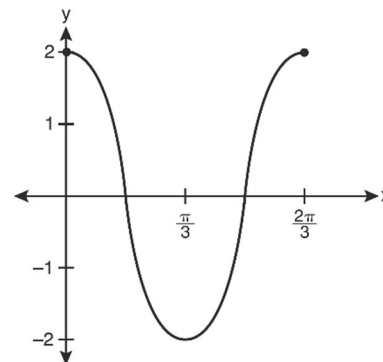
12. Which equation is graphed in the diagram below?

- 1)  $y = 3 \cos\left(\frac{\pi}{30}x\right) + 8$
- 2)  $y = 3 \cos\left(\frac{\pi}{15}x\right) + 5$
- 3)  $y = -3 \cos\left(\frac{\pi}{30}x\right) + 8$
- 4)  $y = -3 \cos\left(\frac{\pi}{15}x\right) + 5$



13. Which equation is represented by the graph below?

- 1)  $y = 2 \cos 3x$
- 2)  $y = 2 \sin 3x$
- 3)  $y = 2 \cos \frac{2\pi}{3}x$
- 4)  $y = 2 \sin \frac{2\pi}{3}x$



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## Sinusoidal Applications

1. Which statement is *incorrect* for the graph of the function  $y = -3 \cos\left[\frac{\pi}{3}(x-4)\right] + 7$ ?

- 1) The period is 6.
- 2) The amplitude is 3.
- 3) The range is  $[4, 10]$ .
- 4) The midline is  $y = -4$ .

2. Which function's graph has a period of 8 and reaches a maximum height of 1 if at least one full period is graphed?

- 1)  $y = -4 \cos\left(\frac{\pi}{4}x\right) - 3$
- 2)  $y = -4 \cos\left(\frac{\pi}{4}x\right) + 5$
- 3)  $y = -4 \cos(8x) - 3$
- 4)  $y = -4 \cos(8x) + 5$

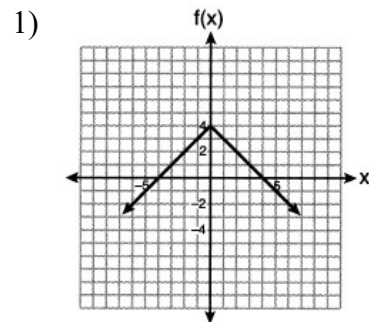
3. The equation below can be used to model the height of a tide in feet,  $H(t)$ , on a beach at  $t$  hours.

$$H(t) = 4.8 \sin\left(\frac{\pi}{6}(t+3)\right) + 5.1$$

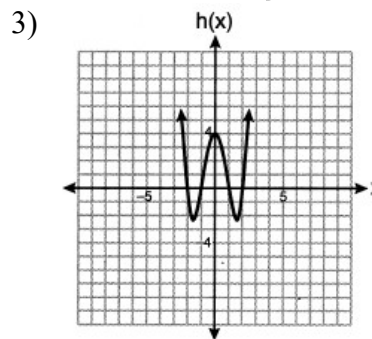
Using this function, the amplitude of the tide is

- 1)  $\frac{\pi}{6}$
- 2) 4.8
- 3) 3
- 4) 5.1

4. Which function has a maximum  $y$ -value of 4 and a midline of  $y = 1$ ?



2)  $g(x) = -3 \cos(x) + 1$



4)  $j(x) = 4 \sin(x) + 1$

5. The depth of the water,  $d(t)$ , in feet, on a given day at Thunder Bay,  $t$  hours after midnight is modeled by  $d(t) = 5 \sin\left(\frac{\pi}{6}(t-5)\right) + 7$ . Which statement about the Thunder Bay tide is *false*?

- |  |   |
|--|---|
| 1) A low tide occurred at 2 a.m.               | 3) The water depth at 9 a.m. was approximately 11 feet.                     |
| 2) The maximum depth of the water was 12 feet. | 4) The difference in water depth between high tide and low tide is 14 feet. |

6. A person's lung capacity can be modeled by the function  $C(t) = 250 \sin\left(\frac{2\pi}{5}t\right) + 2450$ , where  $C(t)$  represents the volume in mL present in the lungs after  $t$  seconds. State the maximum value of this function over one full cycle, and explain what this value represents.

7. Based on climate data that have been collected in Bar Harbor, Maine, the average monthly temperature, in degrees F, can be modeled by the equation  $B(x) = 23.914 \sin(0.508x - 2.116) + 55.300$ . The same governmental agency collected average monthly temperature data for Phoenix, Arizona, and found the temperatures could be modeled by the equation  $P(x) = 20.238 \sin(0.525x - 2.148) + 86.729$ . Which statement can *not* be concluded based on the average monthly temperature models  $x$  months after starting data collection?

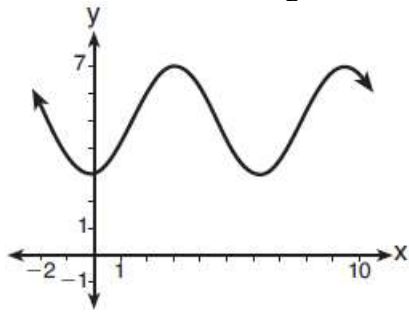
- |  |   |
|--|---|
| 1) The average monthly temperature variation is more in Bar Harbor than in Phoenix.                          | 3) The maximum average monthly temperature for Bar Harbor is $79^\circ$ F, to the nearest degree. |
| 2) The midline average monthly temperature for Bar Harbor is lower than the midline temperature for Phoenix. | 4) The minimum average monthly temperature for Phoenix is $20^\circ$ F, to the nearest degree.    |

8. Consider the function  $h(x) = 2 \sin(3x) + 1$  and the function  $q$  represented in the table below. Determine which function has the *smaller* minimum value for the domain  $[-2, 2]$ . Justify your answer.

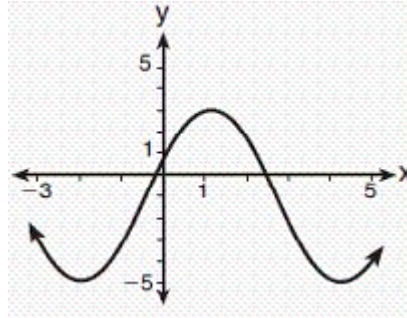
$x$	$q(x)$
-2	-8
-1	0
0	0
1	-2
2	0

9. Which sinusoid has the greatest amplitude?

1)



3)

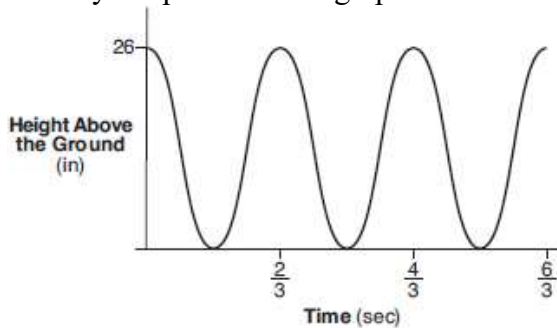


2)  $y = 3 \sin(\theta - 3) + 5$

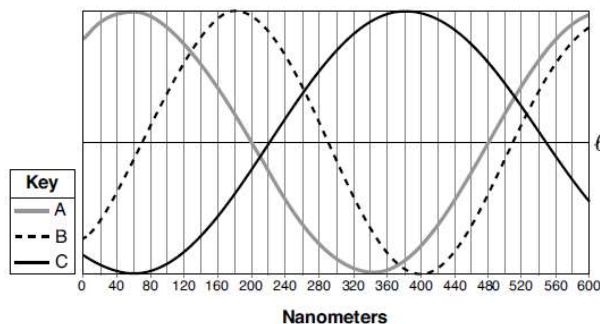
4)  $y = -5 \sin(\theta - 1) - 3$

10. The graph below represents the height above the ground,  $h$ , in inches, of a point on a triathlete's bike wheel during a training ride in terms of time,  $t$ , in seconds.

Identify the period of the graph and describe what the period represents in this context.



11. Visible light can be represented by sinusoidal waves. Three visible light waves are shown in the graph below. The midline of each wave is labeled  $\ell$ . Based on the graph, which light wave has the longest period? Justify your answer.



12. A wave displayed by an oscilloscope is represented by the equation  $y = 3 \sin x$ . What is the period of this function?

1)  $2\pi$

3) 3

2) 2

4)  $3\pi$



13. The depth of the water,  $d(t)$ , in feet, on a given day at Thunder Bay,  $t$  hours after midnight is modeled by  $d(t) = 5 \sin\left(\frac{\pi}{6}(t - 5)\right) + 7$ . What is the frequency of this function?

- 1) 12
- 2)  $\frac{1}{12}$
- 3)  $\frac{\pi}{6}$
- 4)  $\frac{6}{\pi}$

14. The Sea Dragon, a pendulum ride at an amusement park, moves from its central position at rest according to the trigonometric function  $P(t) = -10 \sin\left(\frac{\pi}{3}t\right)$ , where  $t$  represents time, in seconds. How many seconds does it take the pendulum to complete one full cycle?

- 1) 5
- 2) 6
- 3) 3
- 4) 10

15. What is the frequency of  $P(t) = -2 \sin(6\pi(t - 4)) + 3$ ?

16. Which statement is true of the function  $y = -2 \cos[3(x - 4)] + 7$ ?

- 1) The midline is  $y = -4$
- 2) The amplitude is  $-2$
- 3) The range is  $[-2, 2]$
- 4) The frequency is  $\frac{3}{2\pi}$

17. The height above ground for a person riding a Ferris wheel after  $t$  seconds is modeled by  $h(t) = 150 \sin\left(\frac{\pi}{45}t + 67.5\right) + 160$  feet. How many seconds does it take to go from the bottom of the wheel to the top of the wheel?

- 1) 10
- 2) 45
- 3) 90
- 4) 150

18. As  $\theta$  increases from  $\pi$  to  $\frac{3\pi}{2}$  radians, the graph of  $y = \sin \theta$  will

- 1) Decrease from 1 to 0
- 2) Decrease from 0 to -1
- 3) Increase from -1 to 0
- 4) Increase from 0 to 1

19. As  $\theta$  increases from  $-\frac{\pi}{2}$  to 0 radians, the graph of  $y = -\cos \theta$  will

- 1) Decrease from 1 to 0
- 2) Decrease from 0 to -1
- 3) Increase from -1 to 0
- 4) Increase from 0 to 1

20. As  $\theta$  increases from  $-\frac{\pi}{2}$  to 0 radians, the value of  $\cos \theta$  will

- 1) decrease from 1 to 0
- 2) decrease from 0 to -1
- 3) increase from -1 to 0
- 4) increase from 0 to 1

21. Given  $p(\theta) = 3 \sin\left(\frac{1}{2}\theta\right)$  on the interval  $-\pi < \theta < \pi$ , the function  $p$

- 1) decreases, then increases
- 2) increases, then decreases
- 3) decreases throughout the interval
- 4) increases throughout the interval

22. As  $x$  increases from 0 to  $\frac{\pi}{2}$ , the graph of the equation  $y = 2 \tan x$  will

- 1) increase from 0 to 2
- 2) decrease from 0 to -2
- 3) increase without limit
- 4) decrease without limit

Name \_\_\_\_\_  
Mr. Schlansky

Date \_\_\_\_\_  
Algebra II



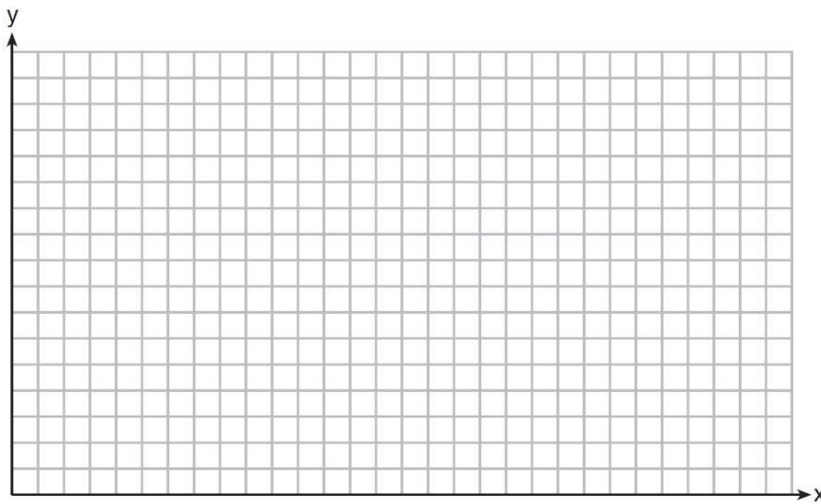
## Graphing Sinusoidal Models

1. The High Roller, a Ferris wheel in Las Vegas, Nevada, opened in March 2014. A passenger's height, in feet, above the ground after  $t$  minutes can be modeled by the equation

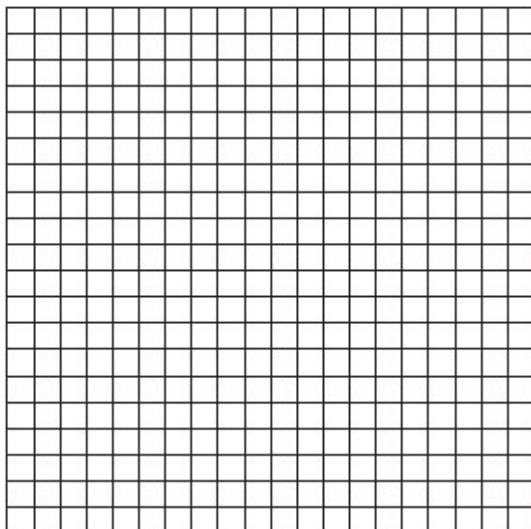
$$h(t) = -260 \cos\left(\frac{\pi}{15}t\right) + 290.$$

Graph one full cycle of  $h(t)$  on the axes provided. Identify the period

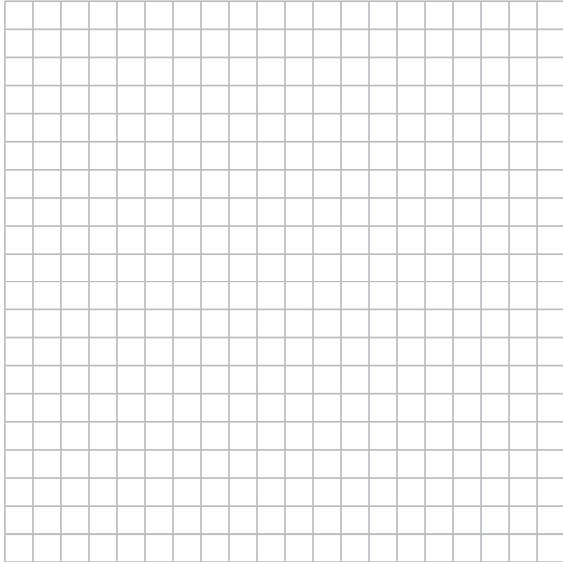
and state its meaning in the context of the problem. To the *nearest tenth of a second*, after how much time will the passenger first reach a height of 500 feet?



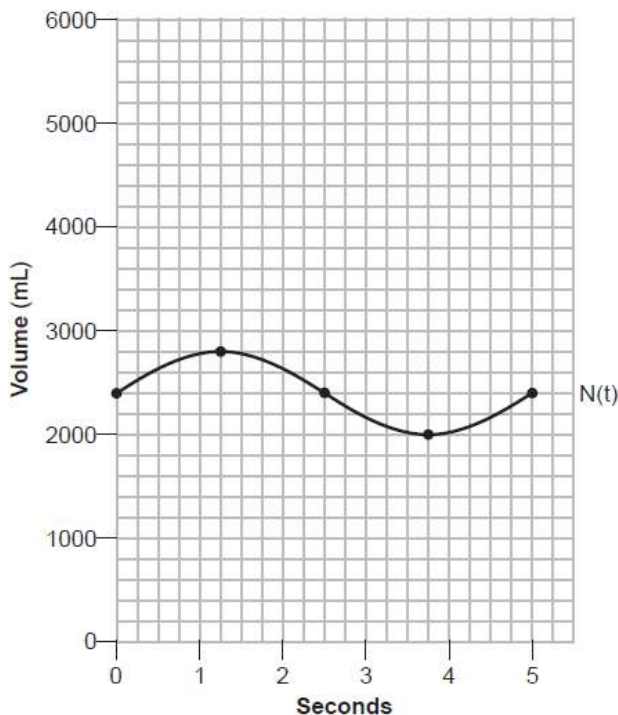
2. Griffin is riding his bike down the street in Churchville, N.Y. at a constant speed, when a nail gets caught in one of his tires. The height of the nail above the ground, in inches, can be represented by the trigonometric function  $f(t) = -13 \cos(0.8\pi t) + 13$ , where  $t$  represents the time (in seconds) since the nail first became caught in the tire. Determine the period of  $f(t)$ . Interpret what the period represents in this context. On the grid below, graph *at least one* cycle of  $f(t)$  that includes the  $y$ -intercept of the function. Does the height of the nail ever reach 30 inches above the ground? Justify your answer.



3. The ocean tides near Carter Beach follow a repeating pattern over time, which can be modeled by the equation  $h(t) = -12 \cos\left(\frac{2\pi}{13}t\right)$  where  $h(t)$  represents height above sea level and  $t$  represents hours after 8:30 AM. On the grid below, graph one cycle of this function. Determine the period and state its meaning in the context of the problem. People who fish in Carter Beach know that a certain species of fish is most plentiful when the water level is increasing. Explain whether you would recommend fishing for this species at 7:30 p.m. or 10:30 p.m. using evidence from the given context.



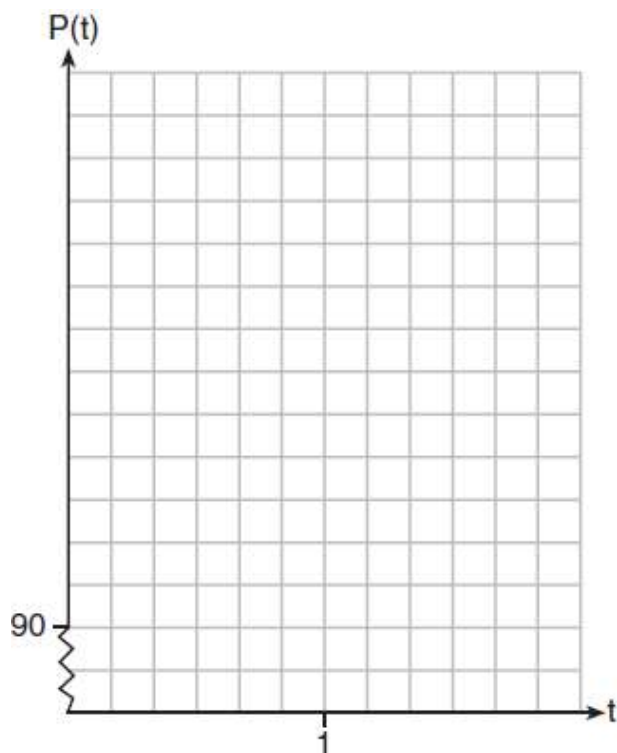
4. The volume of air in an average lung during breathing can be modeled by the graph below. Using the graph, write an equation for  $N(t)$ , in the form  $N(t) = A \sin(Bt) + C$ . That same lung, when engaged in exercise, has a volume that can be modeled by  $E(t) = 2000 \sin(\pi t) + 3200$ , where  $E(t)$  is volume in mL and  $t$  is time in seconds. Graph *at least one* cycle of  $E(t)$  on the same grid as  $N(t)$ . How many times during the 5-second interval will  $N(t) = E(t)$ ?



5. The resting blood pressure of an adult patient can be modeled by the function  $P$  below, where  $P(t)$  is the pressure in millimeters of mercury after time  $t$  in seconds.

$$P(t) = 24 \cos(3\pi t) + 120$$

On the set of axes below, graph  $y = P(t)$  over the domain  $0 \leq t \leq 2$ .



Determine the period of  $P$ . Explain what this value represents in the given context. Normal resting blood pressure for an adult is 120 over 80. This means that the blood pressure oscillates between a maximum of 120 and a minimum of 80. Adults with high blood pressure (above 140 over 90) and adults with low blood pressure (below 90 over 60) may be at risk for health disorders. Classify the given patient's blood pressure as low, normal, or high and explain your reasoning.