

real: $b^2 - 4ac \geq 0$

imaginary: $b^2 - 4ac < 0$

equal: $b^2 - 4ac = 0$

Name Schlansky
Mr. Schlansky

Date _____
Pre-Calculus

Using the Nature of the Roots

1. For what values of k is the roots of $kx^2 - 4x + 2 = 0$ real? ≥ 0

$$\begin{aligned} b^2 - 4ac &\geq 0 \\ (-4)^2 - 4(k)(2) &\geq 0 \\ 16 - 8k &\geq 0 \\ +8k &+8k \end{aligned} \quad \begin{aligned} \frac{16}{8} &\geq \frac{8k}{8} \\ 2 &\geq k \\ \boxed{k &\leq 2} \end{aligned}$$

2. For what value of k are the roots of $x^2 - 3x + k = 0$ equal? $= 0$

$$\begin{aligned} b^2 - 4ac &= 0 \\ (-3)^2 - 4(1)(k) &= 0 \\ 9 - 4k &= 0 \\ +4k &+4k \end{aligned} \quad \begin{aligned} \frac{9}{4} &= \frac{4k}{4} \\ \frac{9}{4} &= k \end{aligned}$$

3. For what values of k are the roots of $kx^2 - 4x + 7 = 0$ imaginary? < 0

$$\begin{aligned} b^2 - 4ac &< 0 \\ (-4)^2 - 4(k)(7) &< 0 \\ 16 - 28k &< 0 \\ -16 &-16 \end{aligned} \quad \begin{aligned} \frac{-16}{-28} &< \frac{-16}{-28} \\ k &> \frac{4}{7} \end{aligned}$$

4. For what value of k are the roots of $y = x^2 + 10x + k = 0$ equal? $= 0$

$$\begin{aligned} b^2 - 4ac &= 0 \\ (10)^2 - 4(1)(k) &= 0 \\ 100 - 4k &= 0 \\ -100 &-100 \end{aligned} \quad \begin{aligned} \frac{-100}{-4} &= \frac{-100}{-4} \\ k &= 25 \end{aligned}$$

5. For what values of k are the roots of $x^2 + 5x + k = 0$ are real? ≥ 0

$$b^2 - 4ac \geq 0$$

$$(5)^2 - 4(1)(k) \geq 0$$

$$25 - 4k \geq 0$$

$$\frac{-25}{-4} \geq \frac{-4k}{-4}$$

$$k \leq \frac{25}{4}$$

6. For what value of k are the roots of $-2x^2 + kx - 6 = 0$ imaginary? < 0
 1) 7 2) -7 3) 3.5 4) 9

$$b^2 - 4ac < 0$$

$$(k)^2 - 4(-2)(-6) < 0$$

$$k^2 - 48 < 0$$

$$\sqrt{k^2} = \sqrt{48}$$

$$k = \pm 6.9...$$

Convergent

7. The roots of $x^2 + kx + 7 = 0$ are real when k is equal to:
 1) 1 2) -4 3) 10 4) -5

$$b^2 - 4ac \geq 0$$

$$(k)^2 - 4(1)(7) \geq 0$$

$$k^2 - 28 \geq 0$$

$$\sqrt{k^2} = \sqrt{28}$$

$$k = \pm 5.29...$$

Divergent

8. The roots of $x^2 + bx + 8 = 0$ are imaginary when b is equal to:
 1) -6 2) 1 3) 6 4) 10

$$b^2 - 4ac < 0$$

$$b^2 - 4(1)(8) < 0$$

$$b^2 - 32 < 0$$

$$\sqrt{b^2} = \sqrt{32}$$

$$b = \pm 5.65...$$

Convergent