

real: $b^2 - 4ac \geq 0$
imaginary: $b^2 - 4ac < 0$

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Using the Nature of the Roots

1. For what values of k is the roots of $kx^2 - 4x + 2 = 0$ real? ≥ 0

$$\begin{aligned} b^2 - 4ac &\geq 0 \\ (-4)^2 - 4(k)(2) &\geq 0 \\ 16 - 8k &\geq 0 \\ +8k +8k & \\ \hline 16 &\geq 8k \\ 2 &\geq k \\ \boxed{k \leq 2} & \end{aligned}$$

2. For what value of k are the roots of $x^2 - 3x + k = 0$ equal? $= 0$

$$\begin{aligned} b^2 - 4ac &= 0 \\ (-3)^2 - 4(1)(k) &= 0 \\ 9 - 4k &= 0 \\ +4k +4k & \\ \hline 9 &= 4k \\ \boxed{\frac{9}{4} = k} & \end{aligned}$$

3. For what values of k are the roots of $kx^2 - 4x + 7 = 0$ imaginary? < 0

$$\begin{aligned} b^2 - 4ac &< 0 \\ (-4)^2 - 4(k)(7) &< 0 \\ 16 - 28k &< 0 \\ -16 & \\ \hline -28 & \\ -28 & \\ \hline -28 & \\ K &> \frac{4}{7} \\ \boxed{K > \frac{4}{7}} & \end{aligned}$$

4. For what value of k are the roots of $y = x^2 + 10x + k = 0$ equal? $= 0$

$$\begin{aligned} b^2 - 4ac &= 0 \\ (10)^2 - 4(1)(k) &= 0 \\ 100 - 4k &= 0 \\ -100 & \\ \hline -4 & \\ -4 & \\ \hline -4 & \\ -4 & \\ \hline -4 & \\ K &= 25 \\ \boxed{K = 25} & \end{aligned}$$

5. For what values of k are the roots of $x^2 + 5x + k = 0$ are real? ≥ 0

$$b^2 - 4ac \geq 0$$

$$(5)^2 - 4(1)(k) \geq 0$$

$$25 - 4k \geq 0$$

$$-25 \quad -25$$

$$\frac{1-4k}{4} \geq -25$$

$$k \leq \frac{25}{4}$$

6. For what value of k are the roots of $-2x^2 + kx - 6 = 0$ imaginary? < 0

- 1) 7 2) -7 3) 3.5 4) 9

$$b^2 - 4ac < 0$$

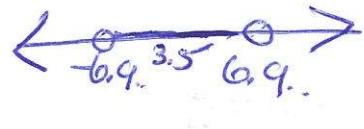
$$(k)^2 - 4(-2)(-6) < 0$$

$$k^2 - 48 < 0$$

+48 +48

$$\sqrt{k^2 - 48}$$

$$k = \pm 6.9\dots$$



7. The roots of $x^2 + kx + 7 = 0$ are real when k is equal to:

- 1) 1 2) -4 3) 10 4) -5

$$b^2 - 4ac \geq 0$$

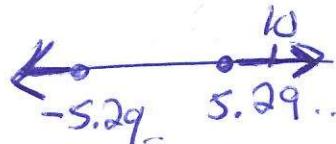
$$(k)^2 - 4(1)(7) \geq 0$$

$$k^2 - 28 \geq 0$$

+28 +28

$$\sqrt{k^2 - 28}$$

$$k = \pm 5.29\dots$$



8. The roots of $x^2 + bx + 8 = 0$ are imaginary when b is equal to: < 0

- 1) -6 2) 1 3) 6 4) 10

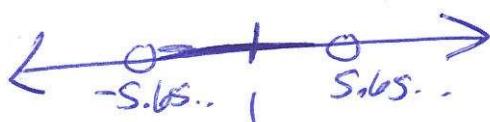
$$b^2 - 4ac < 0$$

$$b^2 - 4(1)(8) < 0$$

$$b^2 - 32 < 0$$

+32 +32

$$b = \pm 5.65\dots$$



$$\sqrt{b^2 - 32}$$

(unreal)