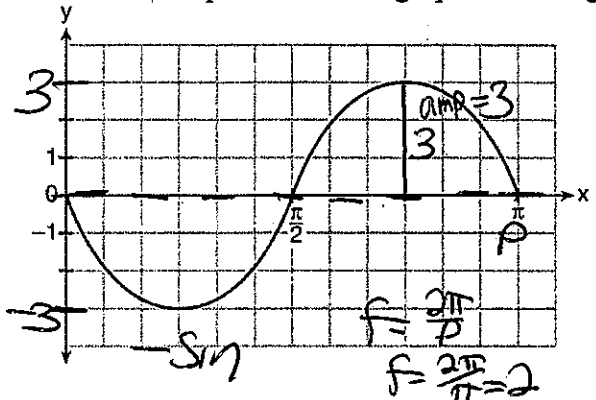


Writing Equations of Sinusoidal Graphs

1. Write an equation for the graph of the trigonometric function shown below.



$\frac{\text{min} + \text{max}}{2} = \text{midline}$
 $\frac{-3 + 3}{2} = \text{midline}$
 $\frac{0}{2} = \text{midline}$
 $0 = \text{midline}$

$y = \text{amp} \sin \text{freq} x \text{ shift}$
 $y = -3 \sin 2x$

2. The accompanying graph represents a portion of a sound wave.

Which equation best represents this graph?

(1) $y = 2 \sin \frac{1}{2} x$

(3) $y = \sin 2x$

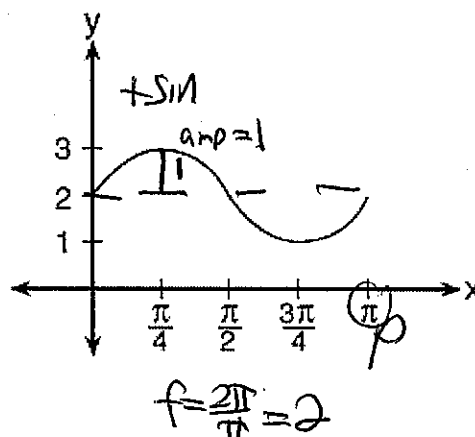
(2) $y = \sin \frac{1}{2} x + 2$

(4) $y = \sin 2x + 2$

$\text{mid} = \frac{\text{min} + \text{max}}{2}$

$\text{mid} = \frac{1+3}{2} = 2$

$y = \text{amp} \sin \text{freq} x \text{ shift}$
 $y = 1 \sin 2x + 2$



3. In physics class, Eva noticed the pattern shown in the accompanying diagram on an oscilloscope.

Which equation best represents the pattern shown on this oscilloscope?

(1) $y = \sin(\frac{1}{2} x) + 1$

(3) $y = 2 \sin x + 1$

(2) $y = \sin x + 1$

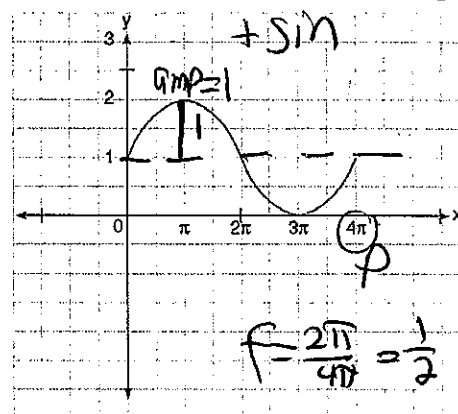
(4) $y = 2 \sin(-\frac{1}{2} x) + 1$

$\text{mid} = \frac{\text{min} + \text{max}}{2}$

$\text{mid} = \frac{0+2}{2}$

$\text{mid} = 1$

$y = \text{amp} \sin \text{freq} x \text{ shift}$
 $y = 1 \sin \frac{1}{2} x + 1$



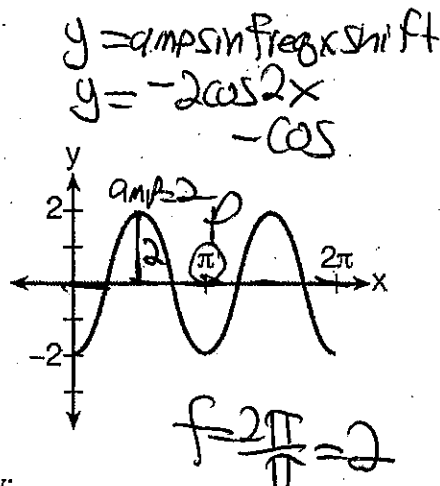
4. Which equation represents the graph below?

- 1) $y = -2 \sin 2x$
- 2) $y = -2 \sin \frac{1}{2}x$
- 3) $y = -2 \cos 2x$
- 4) $y = -2 \cos \frac{1}{2}x$

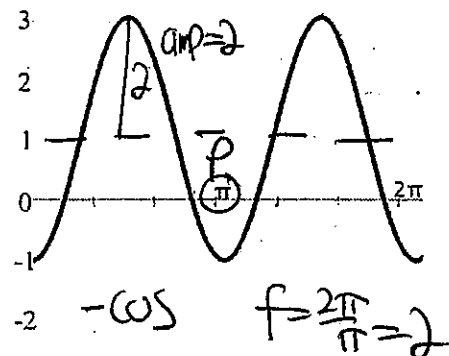
$$\text{mid} = \frac{\text{min} + \text{max}}{2}$$

$$\text{mid} = \frac{-2 + 2}{2}$$

$$\text{mid} = 0$$



5. Write the equation of the sinusoidal function shown below:



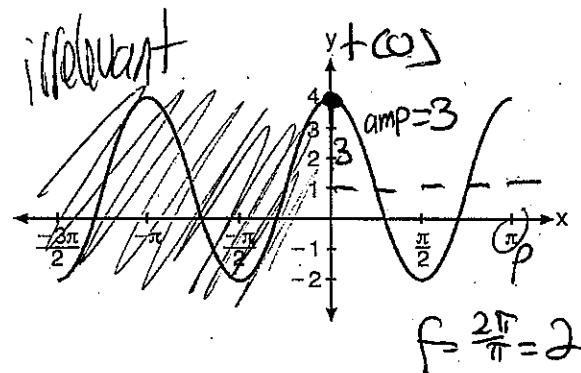
$$\text{mid} = \frac{\text{min} + \text{max}}{2}$$

$$\text{mid} = \frac{-1 + 3}{2}$$

$$\text{mid} = 1$$

$y = \text{amp} \sin \text{freq} x \text{ shift}$
 $y = -2 \cos 2x + 1$

6. What is the equation of the graph given below.



$$\text{mid} = \frac{\text{min} + \text{max}}{2}$$

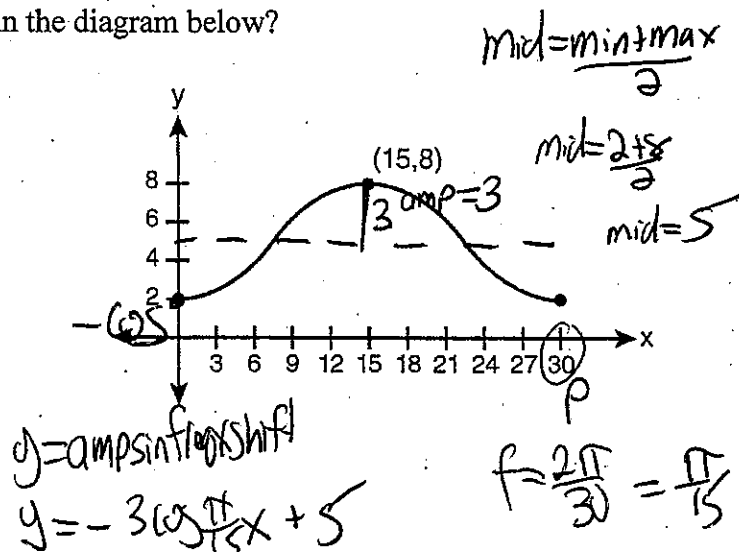
$$\text{mid} = \frac{-2 + 4}{2}$$

$$\text{mid} = 1$$

$y = \text{amp} \sin \text{freq} x \text{ shift}$
 $y = 3 \cos 2x + 1$

7. Which equation is graphed in the diagram below?

- 1) $y = 3 \cos \left(\frac{\pi}{30} x \right) + 8$
- 2) $y = 3 \cos \left(\frac{\pi}{15} x \right) + 5$
- 3) $y = -3 \cos \left(\frac{\pi}{30} x \right) + 8$
- 4) $y = -3 \cos \left(\frac{\pi}{15} x \right) + 5$



8. Which equation is represented by the graph below?

1) $y = 2 \cos 3x$

2) $y = 2 \sin 3x$

3) $y = 2 \cos \frac{2\pi}{3}x$

4) $y = 2 \sin \frac{2\pi}{3}x$

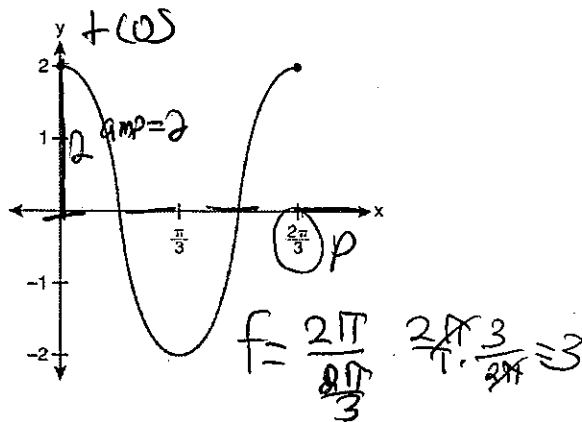
$$\text{mid} = \frac{\text{min} + \text{max}}{2}$$

$$\text{mid} = \frac{-2 + 2}{2}$$

$$\text{mid} = 0$$

$$y = \text{amp} \sin \text{freq} \times \text{shift}$$

$$y = 2 \cos 3x$$



9. The function $f(x) = a \cos bx + c$ is plotted on the graph shown below.

$$\text{mid} = \frac{\text{min} + \text{max}}{2}$$

$$\text{mid} = \frac{1 + 5}{2} = 3$$

What are the values of a , b , and c ?

1) $a = 2, b = 6, c = 3$

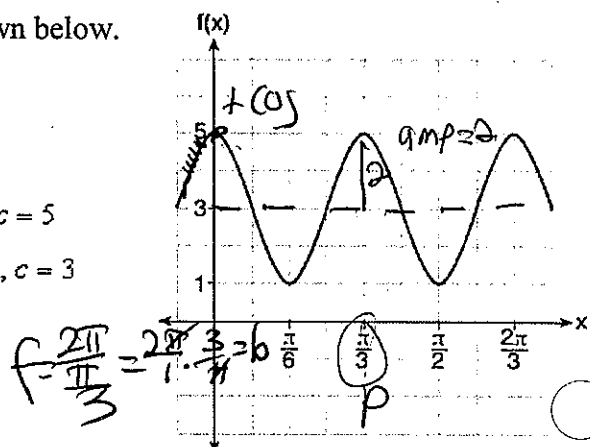
2) $a = 2, b = 3, c = 1$

$$y = \text{amp} \sin \text{freq} \times \text{shift}$$

$$y = 2 \cos 6x + 3$$

3) $a = 4, b = 6, c = 5$

4) $a = 4, b = \frac{\pi}{3}, c = 3$



10. The depth of the water at a marker 20 feet from the shore in a bay is depicted in the graph below.

If the depth, d , is measured in feet and time, t , is measured in hours since midnight, what is an equation for the depth of the water at the marker?

1) $d = 5 \cos \left(\frac{\pi}{6} t \right) + 9$

2) $d = 9 \cos \left(\frac{\pi}{6} t \right) + 5$

3) $d = 9 \sin \left(\frac{\pi}{6} t \right) + 5$

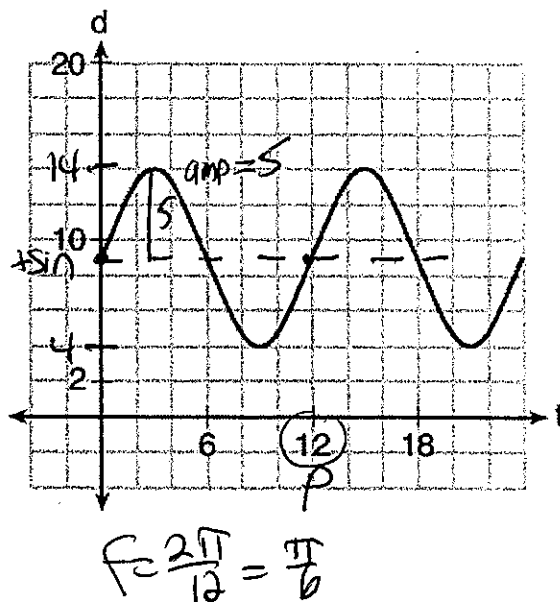
4) $d = 5 \sin \left(\frac{\pi}{6} t \right) + 9$

$$\text{mid} = \frac{\text{min} + \text{max}}{2}$$

$$\text{mid} = \frac{4 + 14}{2} = 9$$

$$y = \text{amp} \sin \text{freq} \times \text{shift}$$

$$y = 5 \sin \frac{\pi}{6} x + 9$$

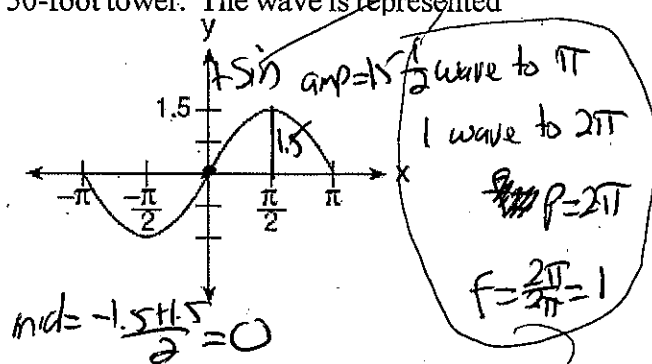


11. A radio transmitter sends a radio wave from the top of a 50-foot tower. The wave is represented by the accompanying graph.

$y = \text{amp} \sin \text{freq} \times \text{shift}$
 $y = 1.5 \sin |x| + 0$

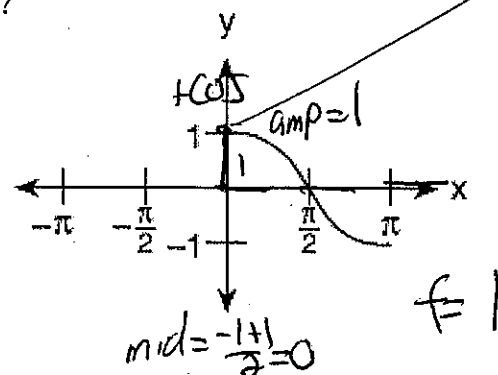
What is the equation of this radio wave?

- (1) $y = \sin x$ (3) $y = \sin 1.5x$
 (2) $y = 1.5 \sin x$ (4) $y = 2 \sin x$

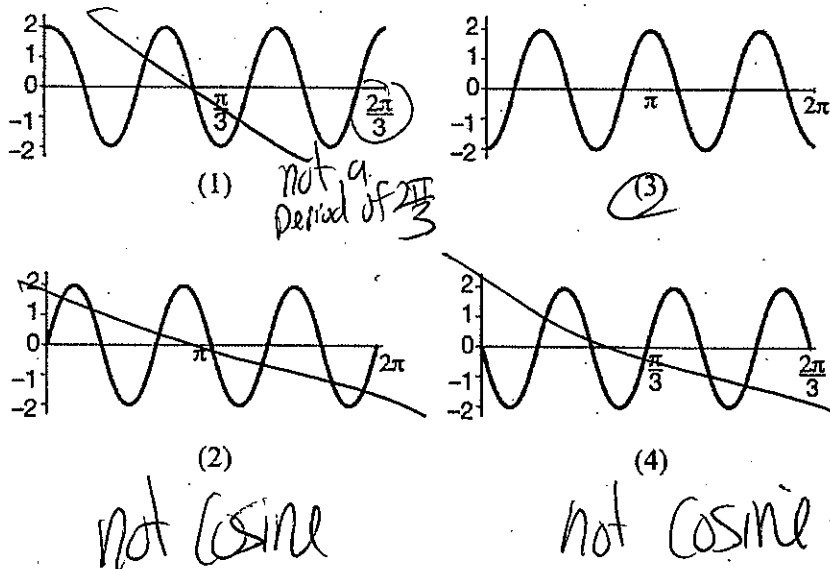


12. Which equation is represented by the accompanying graph?

- (1) $y = \cos x$ (3) $y = \cos 2x$
 (2) $y = \cos \frac{1}{2}x$ (4) $y = \frac{1}{2} \cos x$
- $y = \text{amp} \sin \text{freq} \times \text{shift}$
 $y = 1 \cos |x| + 0$



13. Which graph represents a cosine function with no horizontal shift, an amplitude of 2, and a period of $\frac{2\pi}{3}$?



if 3 waves take 2π ,
 1 wave is $\frac{2\pi}{3}$