

Put both sides into standard form using operations with Polynomials!

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Algebra II

Proving Expressions are Equal

Prove the following expressions are equal

1. $4k^2 - 49 = (2k + 7)(2k - 7)$

	$2k$	$+7$
$2k$	$4k^2$	$+14k$
-7	$-14k$	-49

$4k^2 - 49 = 4k^2 - 49$

2. $2x^2 + 7x + 3 = (x + 3)(2x + 1)$

	x	$+3$
$2x$	$2x^2$	$+6x$
$+1$	$+1x$	$+3$

$2x^2 + 7x + 3 = 2x^2 + 7x + 3$

2. $a^3 - 8b^3 = (a - 2b)(a^2 + 2ab + 4b^2)$

	a^2	$+2ab$	$+4b^2$
a	a^3	$2a^2b$	$4ab^2$
$-2b$	$-2ab$	$-4b^2$	$-8b^3$

$a^3 - 8b^3 = a^3 - 8b^3$

4. $2x^2 + 6x - 36 = 2(x - 3)(x + 6)$

$2x^2 + 6x - 36 = (2x - 6)(x + 6)$

	$2x$	-6
x	$2x^2$	$-6x$
$+6$	$+12x$	-36

$2x^2 + 6x - 36 = 2x^2 + 6x - 36$

5. ~~$-4(x^2 + x - 5) = 2x^2 - 2(3x^2 + 2x - 6)$~~

~~$-4x^2 - 4x + 20 = 2x^2 - 6x^2 - 4x + 12$~~

~~$-4x^2 - 4x + 20 = -4x^2 - 4x + 12$~~

~~$-4(x^2 + x - 5) = 2x^2 - 2(3x^2 + 2x - 6)$~~

~~$-4x^2 - 4x + 20 = 2x^2 - 6x^2 - 4x + 12$~~

~~$-4x^2 - 4x + 20 = -4x^2 - 4x + 12$~~

6. $3(x - 6)^2 - 1 = 3x^2 - 36x + 107$

square binomial
(x-6)² theorem

~~$3(x^2 - 12x + 36) - 1 = 3x^2 - 36x + 107$~~

~~$3x^2 - 36x + 108 - 1 = 3x^2 - 36x + 107$~~

~~$3x^2 - 36x + 107 = 3x^2 - 36x + 107$~~

→ square binomial theorem

$$7. (x+2)^2 + 2(x+2) - 8 = (x+6)x$$

$$x^2 + 4x + 4 + 2x + 4 - 8 = x^2 + 6x$$

$$x^2 + 6x = x^2 + 6x$$

$$8. m^5 + m^3 - 6m = m(m^2 + 3)(m^2 - 2)$$

$$m^5 + m^3 - 6m = (m^3 + 3m)(m^2 - 2)$$

	$m^3 + 3m$	
m^2	m^5	$+3m^3$
-2	$-2m^3$	$-6m$

$$m^5 + m^3 - 6m = m^5 + m^3 - 6m$$

$$9. t^3 + 5t^2 + 6t + t^2 + 5t + 6 = (t+1)(t+2)(t+3)$$

$$t^3 + 6t^2 + 11t + 6$$

	t	$+1$
t	t^2	$+t$
$+2$	$2t$	$+2$

$$(t^2 + 3t + 2)(t + 3)$$

	t^2	$+3t$	$+2$
t	t^3	$+3t^2$	$+2t$
$+3$	$3t^2$	$+9t$	$+6$

$$t^3 + 6t^2 + 11t + 6 = t^3 + 6t^2 + 11t + 6$$

→ square binomial theorem

$$10. 2d(d+3)^2(d-3) = 2d^4 + 6d^3 - 18d^2 - 54d$$

$$2d(d^2 + 6d + 9)(d-3) = 2d^4 + 6d^3 - 18d^2 - 54d$$

$$(2d^3 + 12d^2 + 18d)(d-3) = 2d^4 + 6d^3 - 18d^2 - 54d$$

	$2d^3$	$+12d^2$	$+18d$
d	$2d^4$	$+12d^3$	$+18d^2$
-3	$-6d^3$	$-36d^2$	$-54d$

$$2d^4 + 6d^3 - 18d^2 - 54d = 2d^4 + 6d^3 - 18d^2 - 54d$$